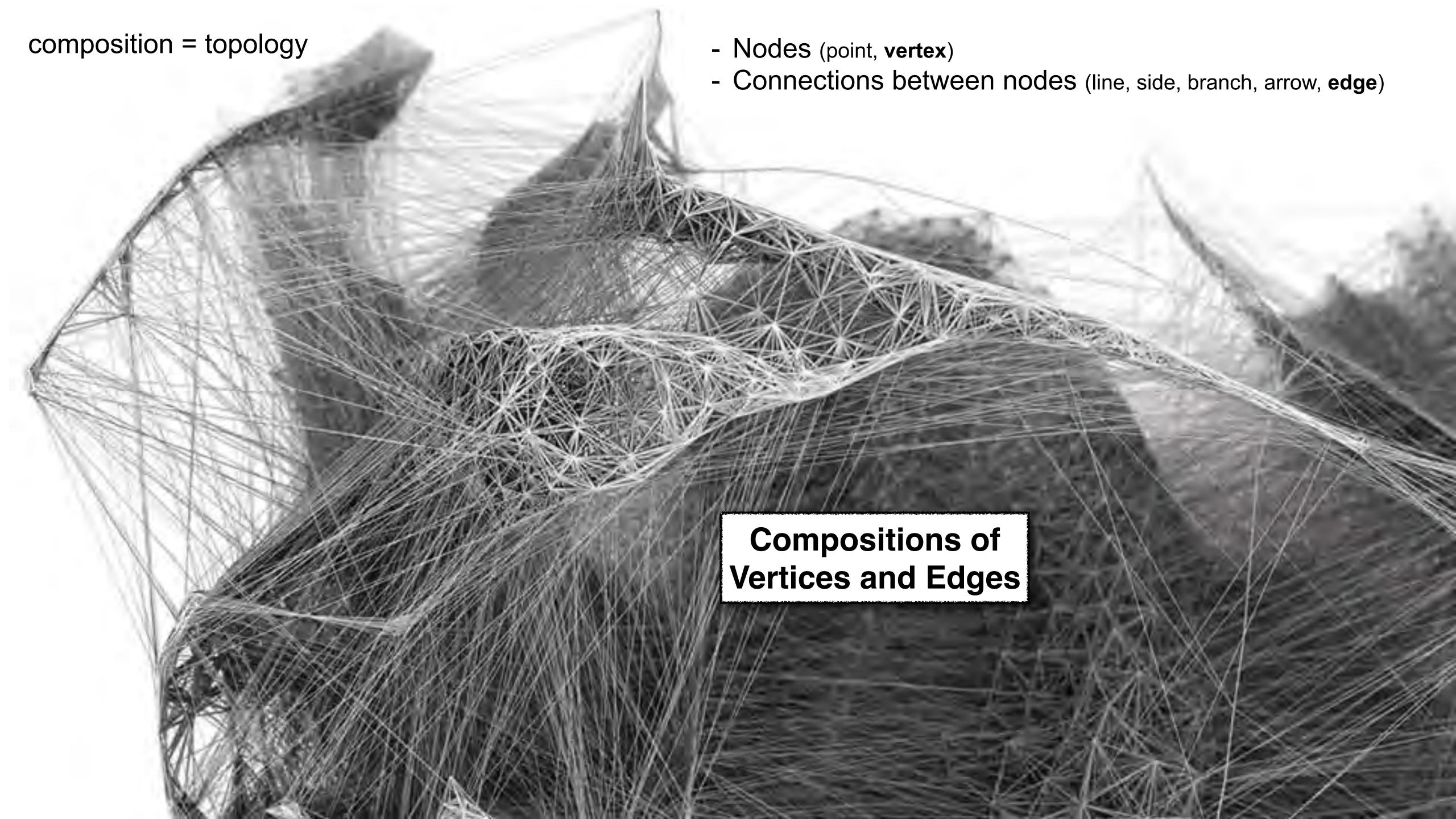
# **Complexity Methods For Behavioural Science**

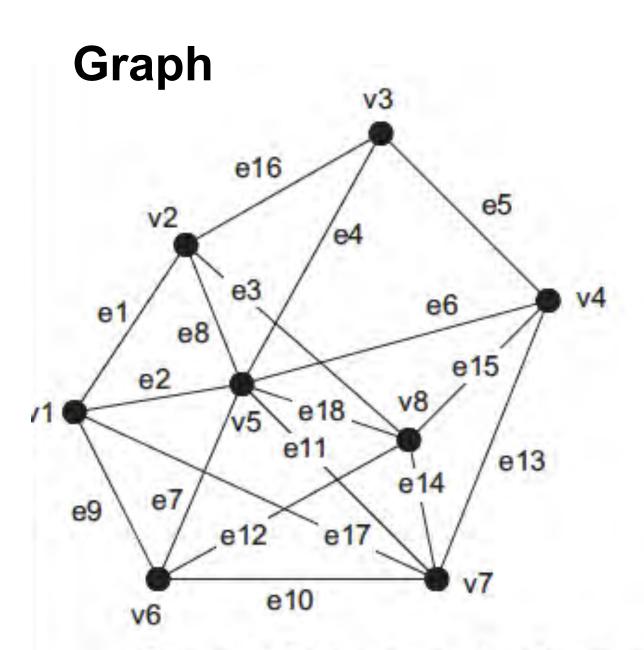
Graph theory
Complex Networks
Symptom Networks

Networks of (Networks of) Complex Systems





- Graph Theory: Compositions of edges and vertices
- Complexe network: Many vertices and edges
- Statistical netwerk models



### **Formal**

$$V(G) = \{v_1, \dots, v_8\}$$

$$E(G) = \{e_1, \dots, e_{18}\}$$

$$e_1 = \langle v_1, v_2 \rangle \quad e_{10} = \langle v_6, v_7 \rangle$$

$$e_2 = \langle v_1, v_5 \rangle \quad e_{11} = \langle v_5, v_7 \rangle$$

$$e_3 = \langle v_2, v_8 \rangle \quad e_{12} = \langle v_6, v_8 \rangle$$

$$e_4 = \langle v_3, v_5 \rangle \quad e_{13} = \langle v_4, v_7 \rangle$$

$$e_5 = \langle v_3, v_4 \rangle \quad e_{14} = \langle v_7, v_8 \rangle$$

$$e_6 = \langle v_4, v_5 \rangle \quad e_{15} = \langle v_4, v_8 \rangle$$

$$e_7 = \langle v_5, v_6 \rangle \quad e_{16} = \langle v_2, v_3 \rangle$$

$$e_8 = \langle v_2, v_5 \rangle \quad e_{17} = \langle v_1, v_7 \rangle$$

$$e_9 = \langle v_1, v_6 \rangle \quad e_{18} = \langle v_5, v_8 \rangle$$

Figure 2.1: An example of a graph with eight vertices and 18 edges.

# **Adjacency matrix**

1	D GU		- MA T-1				KEALA	
	v1	v2	<b>v</b> 3	<b>v</b> 4	v5	v6	<b>v7</b>	<b>v8</b>
v1	0	1	0	0	1	1	1	0
v2	1	0	1	0	1	0	0	1
v3	0	1	0	1	1	0	0	0
v4	0	0	1	0	1	0	1	1
v5	1	1	1	1	0	1	1	1
v6	1	0	0	0	1	0	1	1
<b>v7</b>	1	0	0	1	1	1	0	1
v8	0	1	0	1	1	1	1	0



# undirected graph

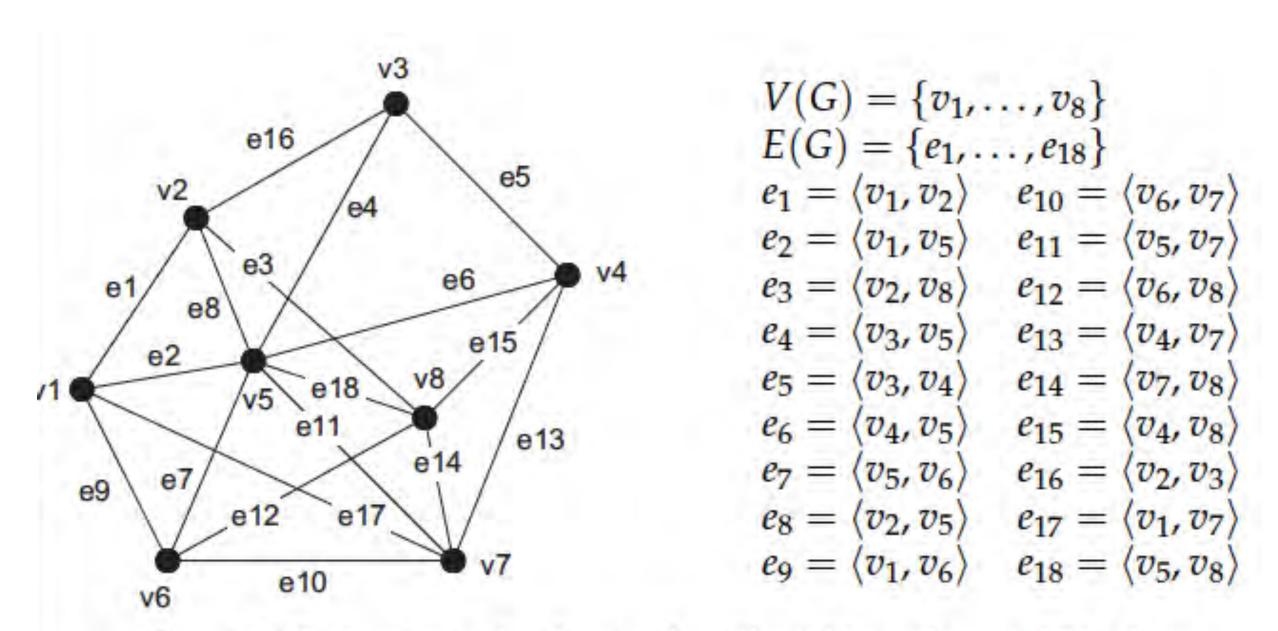
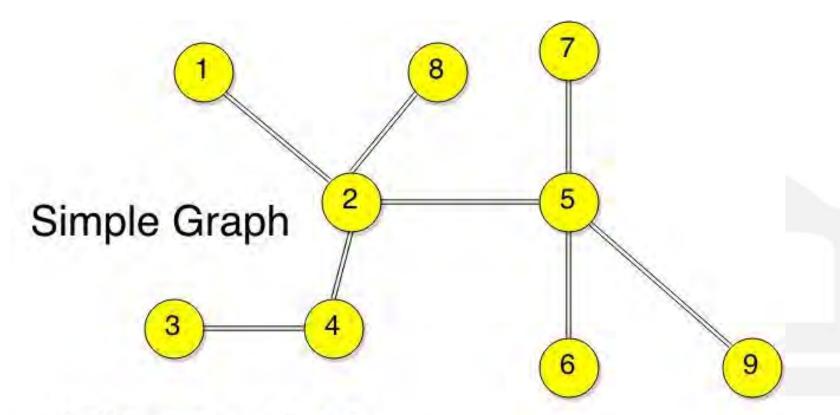


Figure 2.1: An example of a graph with eight vertices and 18 edges.



## Adjacency Matrix

	Vertex 1	Vertex 2	Vertex 3	Vertex 4	Vertex 5	Vertex 6	Vertex 7	Vertex 8	Vertex 9
Vertex 1	0	1	0	0	0	0	0	0	0
Vertex 2	1	0	0	1	1	0	0	1	0
Vertex 3	0	0	0	1	0	0	0	0	0
Vertex 4	0	1	1	0	0	0	0	0	0
Vertex 5	0	1	0	0	0	1	1	0	1
Vertex 6	0	0	0	0	1	0	0	0	0
Vertex 7	0	0	0	0	1	0	0	0	0
Vertex 8	0	1	0	0	0	0	0	0	0
Vertex 9	0	0	0	0	1	0	0	0	0

http://theoryofprogramming.com/tag/adjacency-matrix/

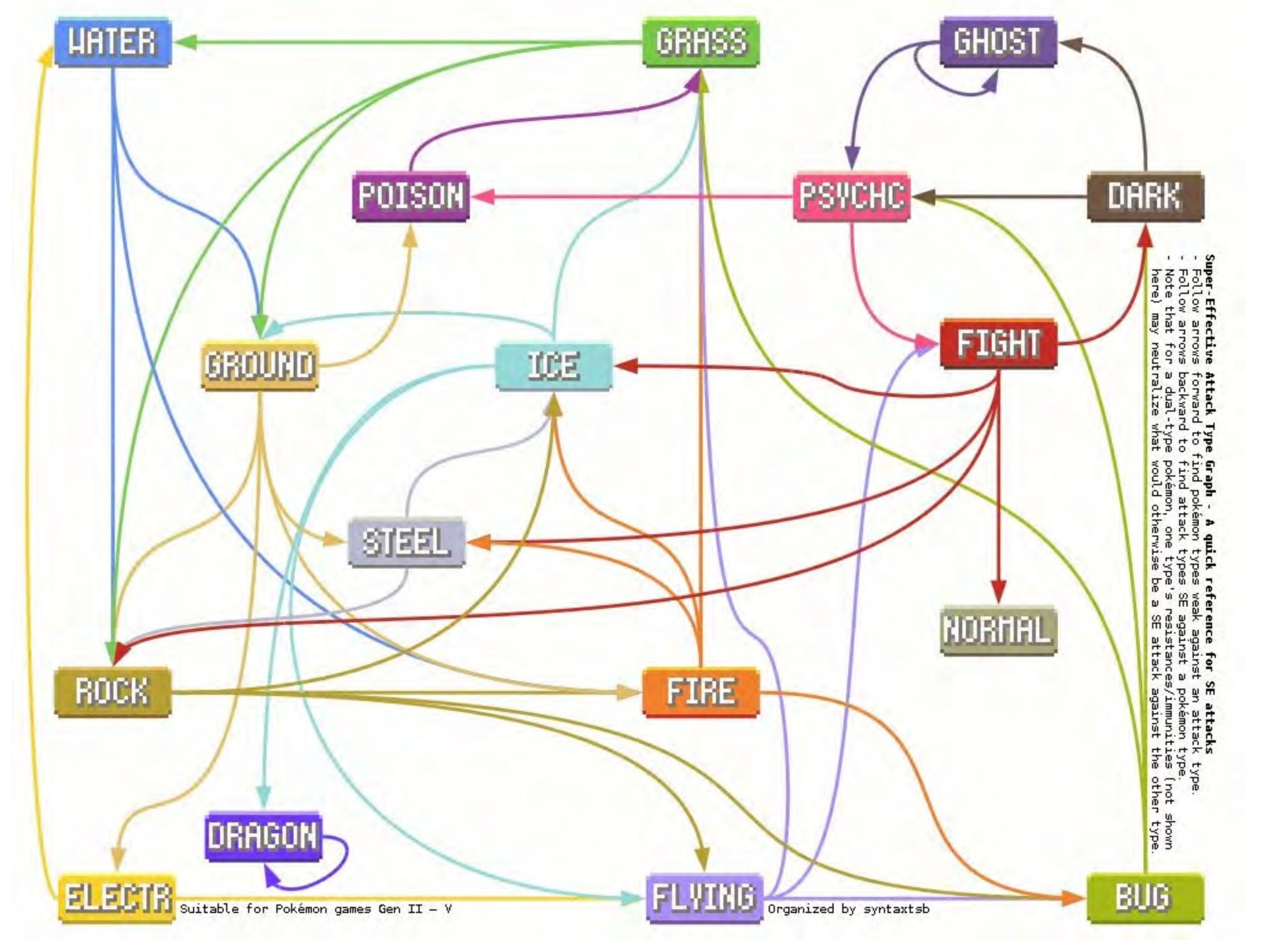


# directed graph (digraph)

# v2 a4 a3 a6 v4

# With loops en arcs

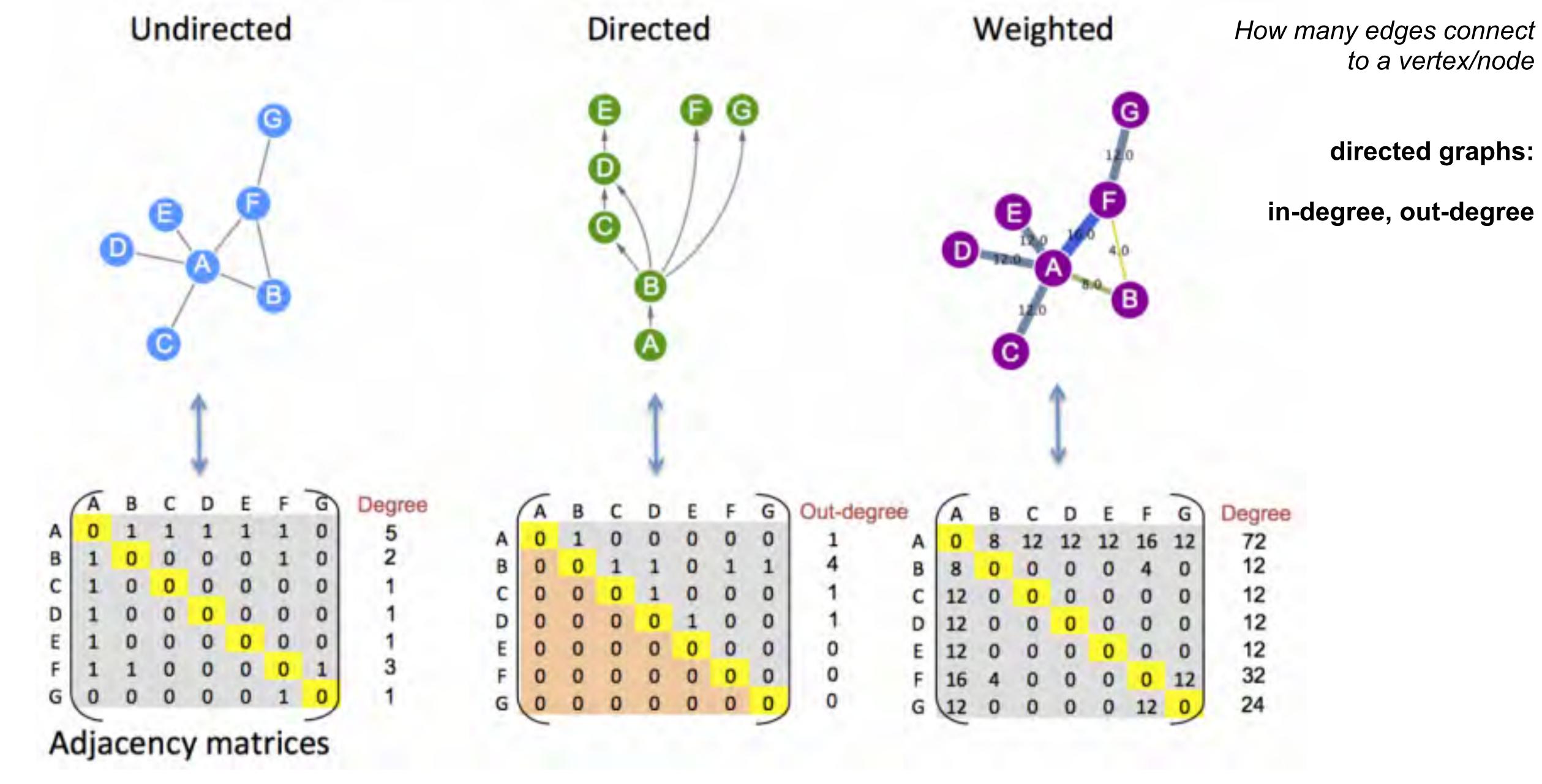
					OUT
	V1	V2	V3	$V_4$	Σ
V <sub>1</sub>	1	1	0	0	2
V <sub>2</sub>	0	0	1	0	1
V3	1	1	0	0	2
$V_4$	0	0	1	1	2
INΣ	2	2	2	1	7



# directed network

Effectivity of Pokemon attacks By species

## Degree:



# Weighted Directed Graph

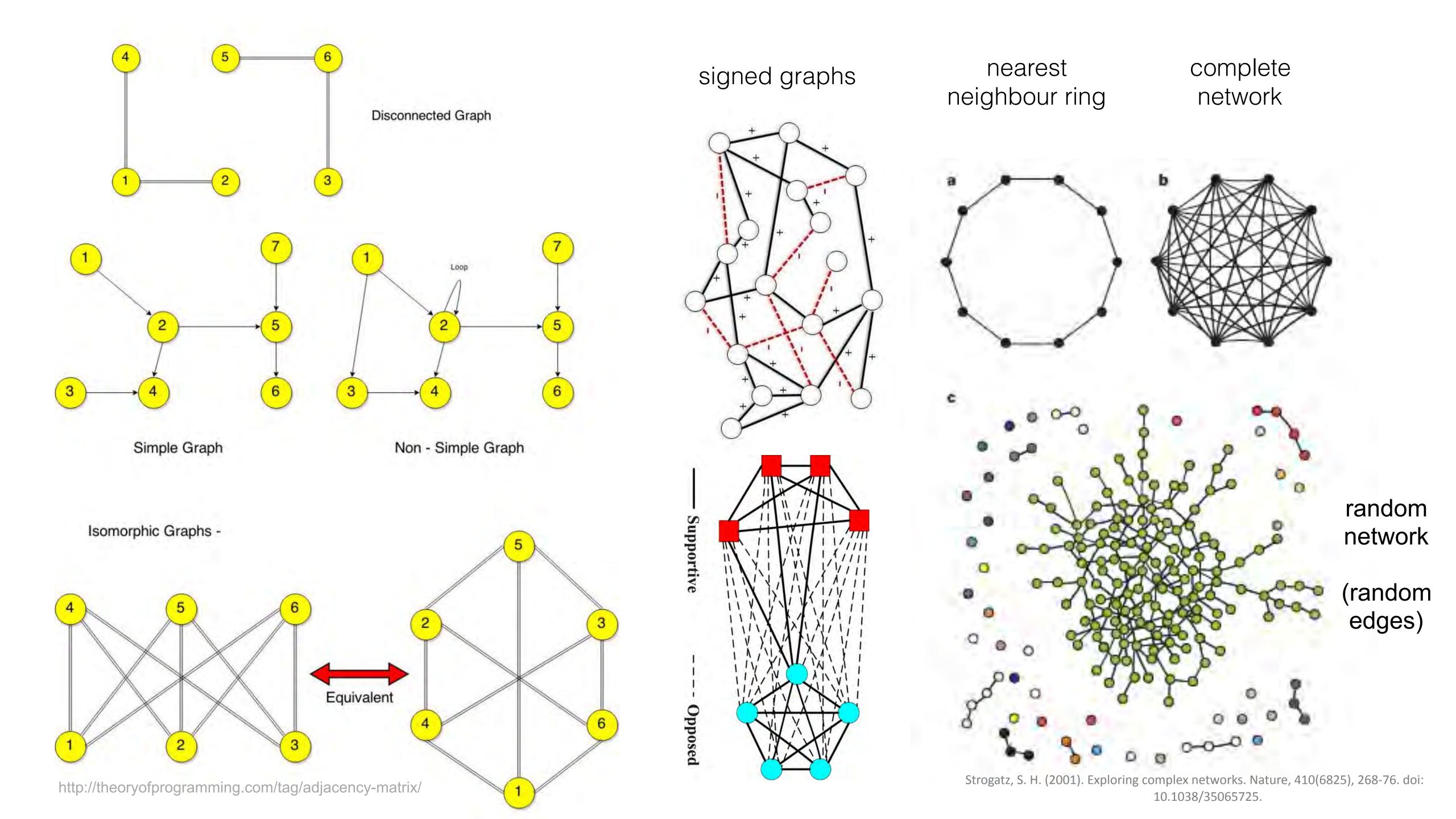


# Adjacency Matrix

to	Vertex 1	Vertex 2	Vertex 3	Vertex 4	Vertex 5	Vertex 6	Vertex 7	Vertex 8	Vertex 9
Vertex 1	0	7	0	0	0	0	0	0	0
Vertex 2	0	0	0	5	9	0	0	1	0
Vertex 3	0	0	0	4	0	0	0	0	0
Vertex 4	0	0	0	0	0	0	0	0	0
Vertex 5	0	0	0	0	0	2	0	0	3
Vertex 6	0	0	0	0	0	0	0	0	0
Vertex 7	0	0	0	0	6	0	0	0	0
Vertex 8	0	0	0	0	0	0	0	0	0
Vertex 9	0	0	0	0	0	0	0	0	0

# weighted directed graph



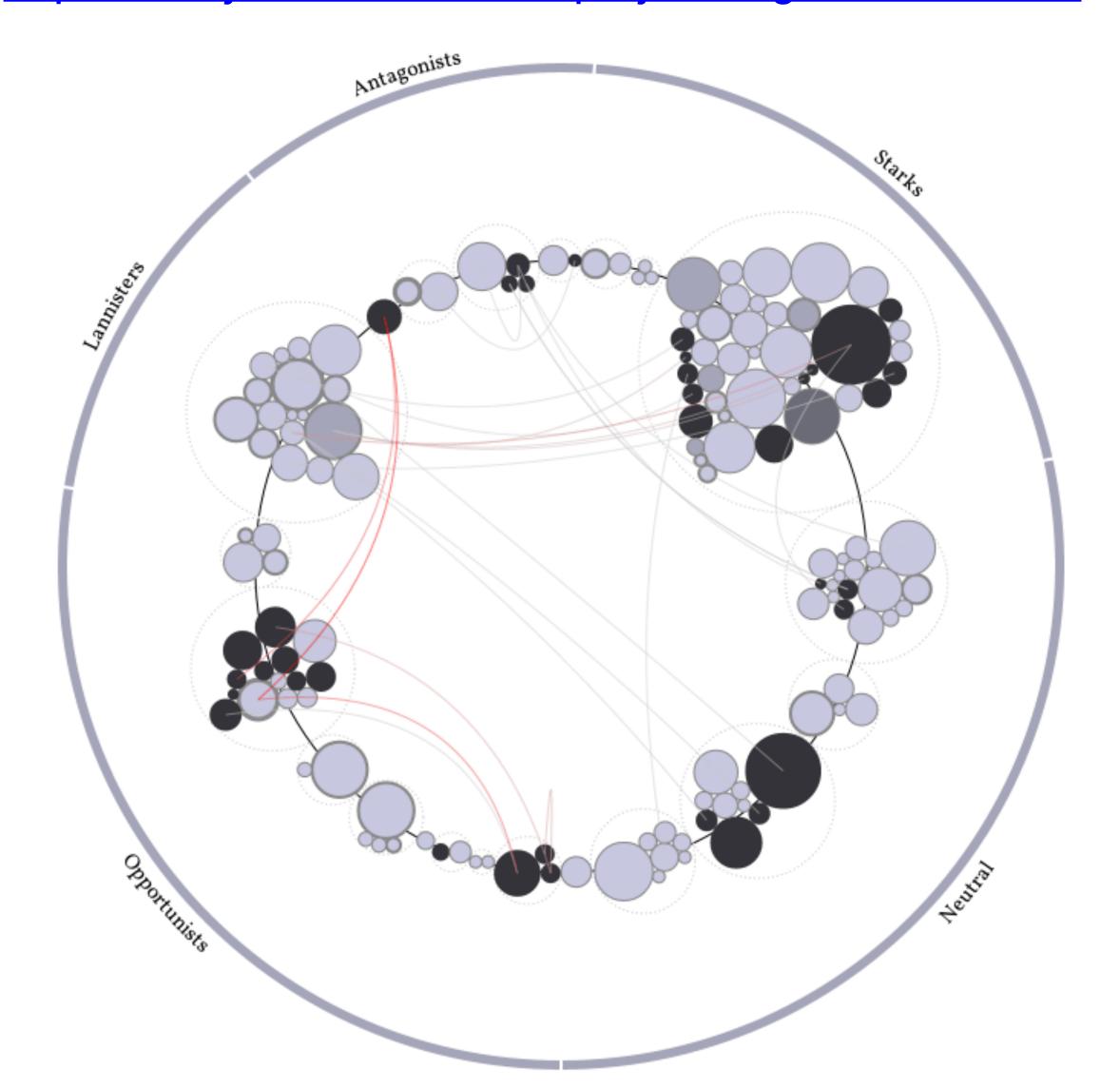


Netwerk that helps you find new beers based on your taste preference



"Relation" between Game of Thrones characters

http://www.jeromecukier.net/projects/agot/events.html

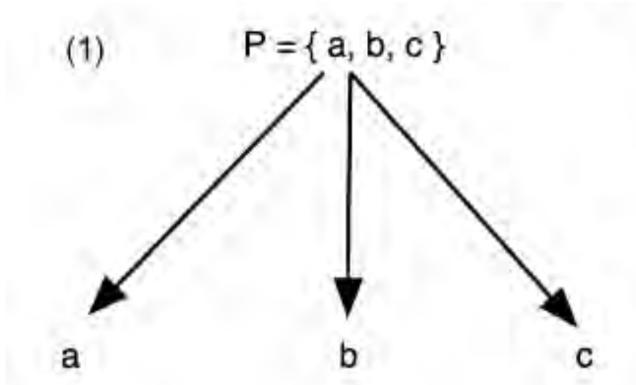


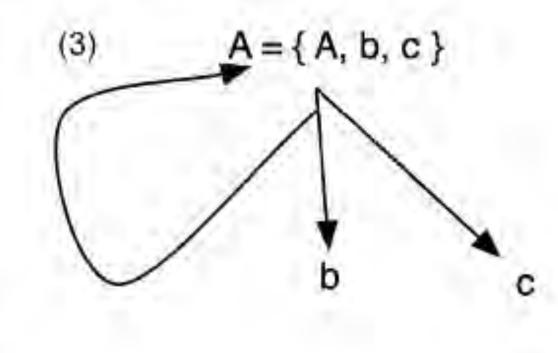
# Hyperset theory + Graph theory = Hyperset Graphs (Impredicative Logic)

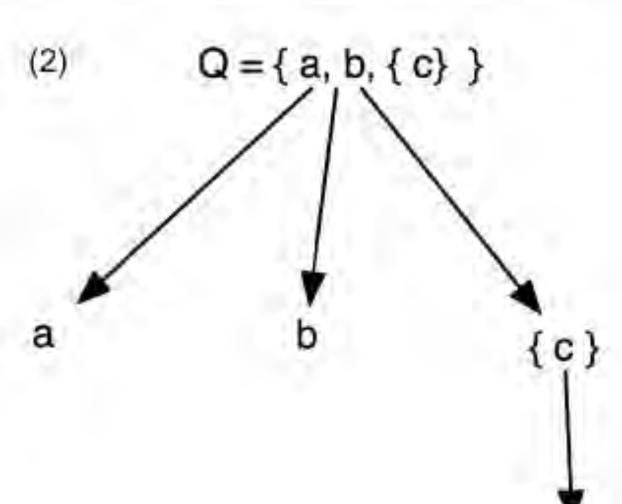
Aczel's Anti-Foundation Axiom (1988) (hyperset theory, circular causality, complexity analysis)

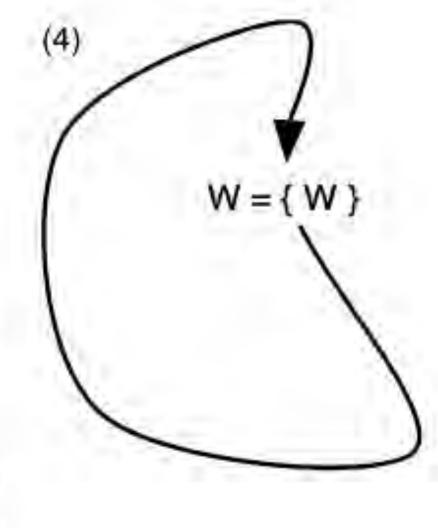


Definition of a set can contain itself









Hyperset theory + Graph theory = Hyperset Graphs

(Impredicative Logic)

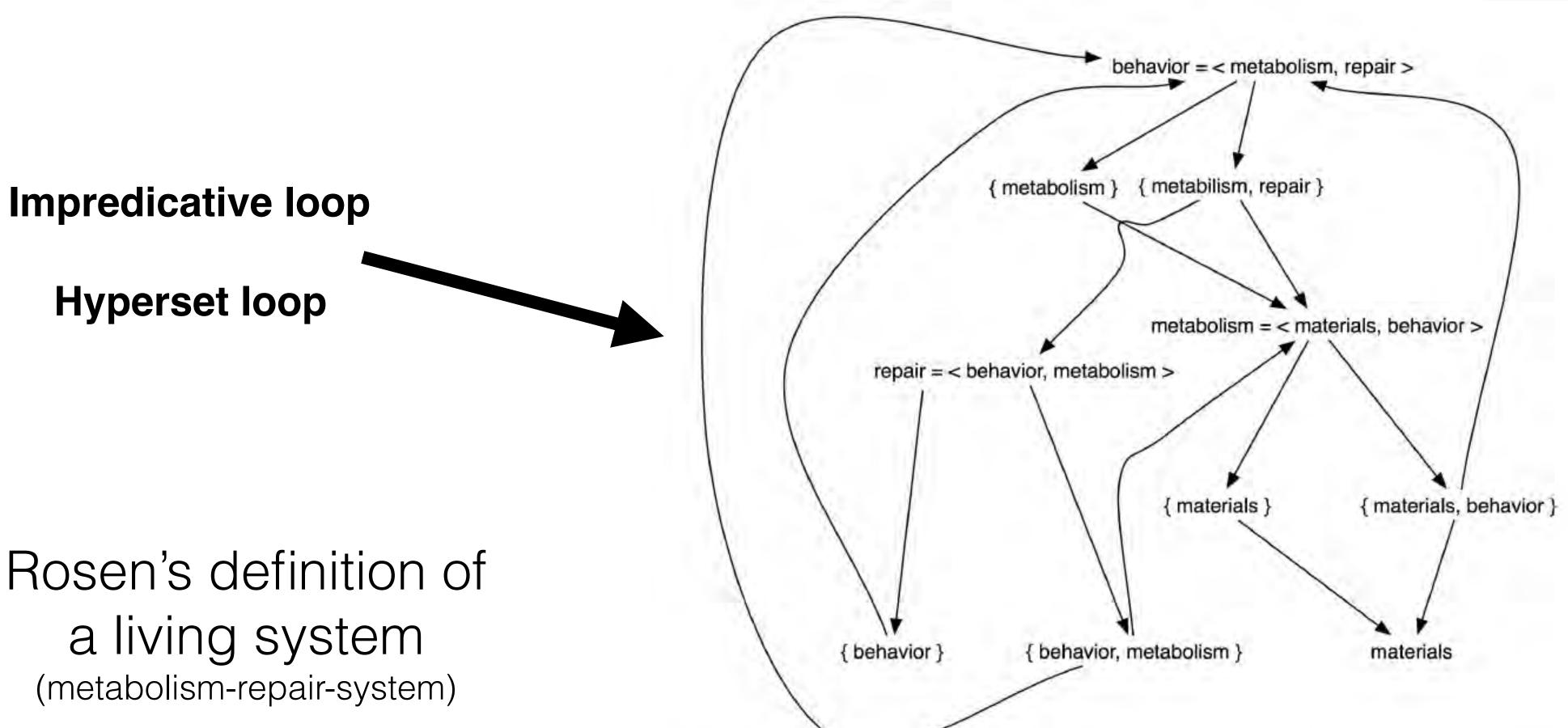


Fig. 6. Hyperset diagram of Rosen's metabolism-repair system. Functions are represented as ordered pairs containing their domain and range. So f(a) = b is represented as  $f = \langle a, b \rangle$ .

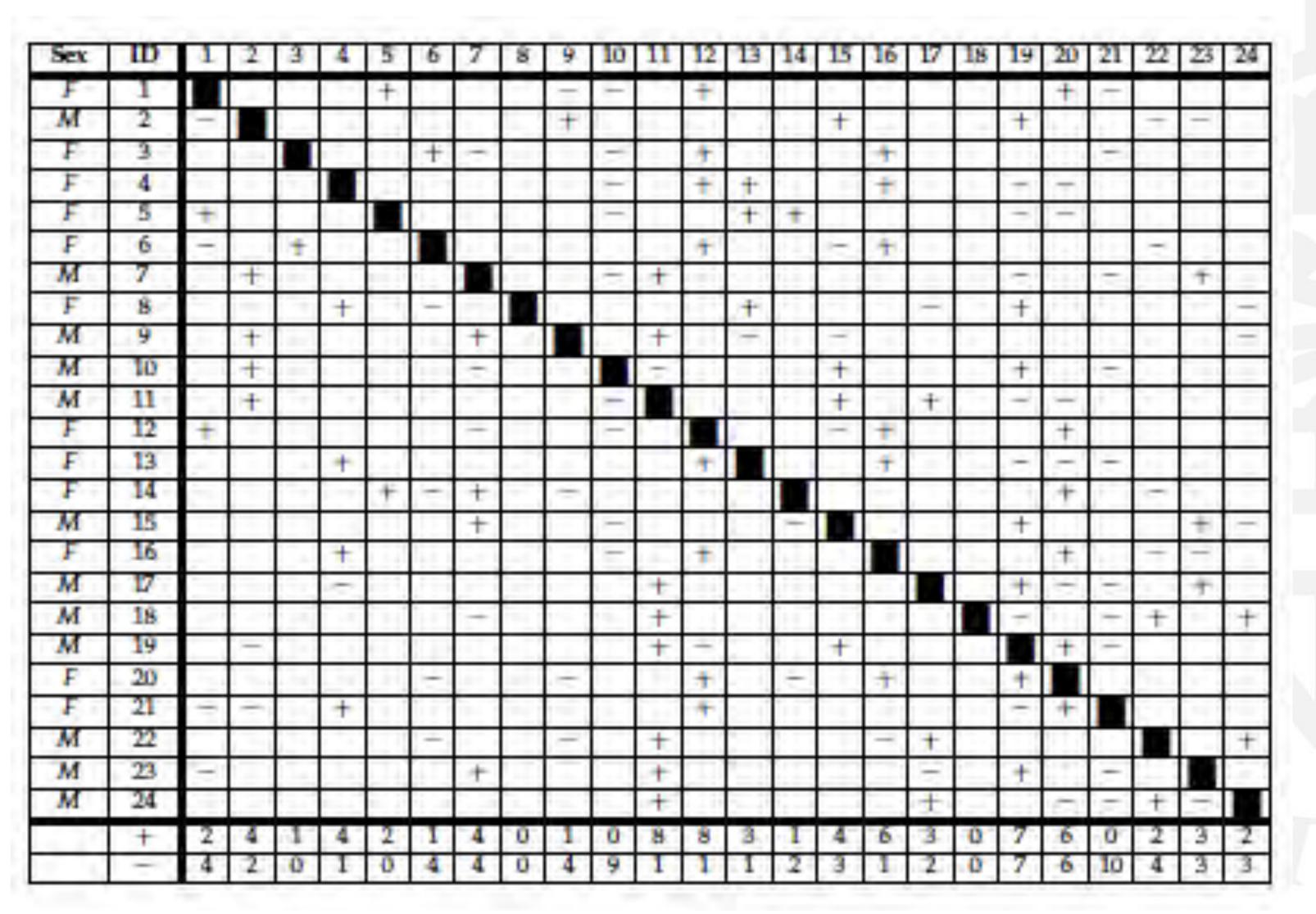


# Social networks

Moreno, 1930

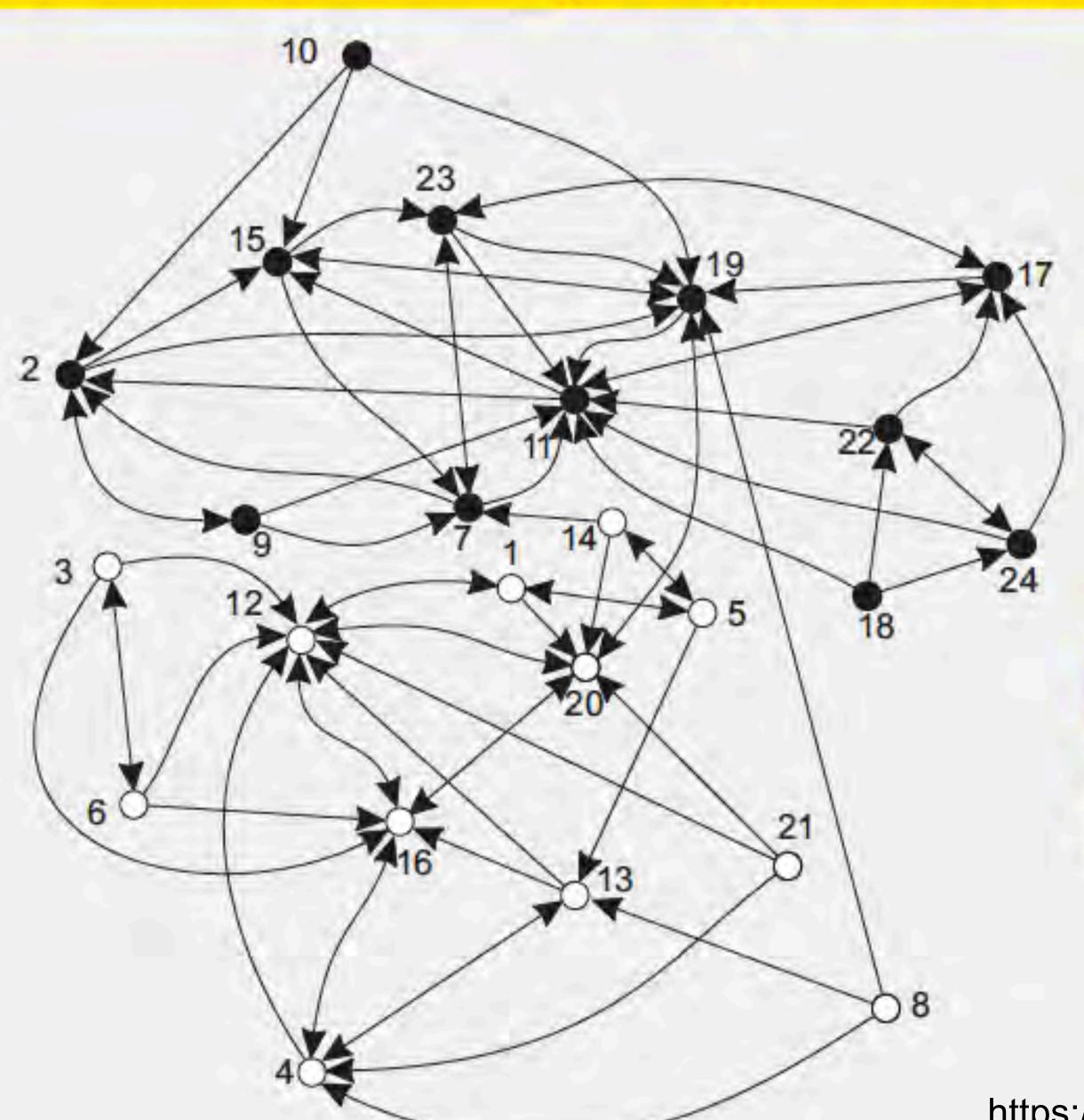
sociogram

3 "most liked" 3 "most disliked"





# Classroom example - positive nominations



- Clear distinction between boys ("•") and girls ("o")
- Relation between 19 and 20 is important
- There are a few "isolated" children (8 & 10)

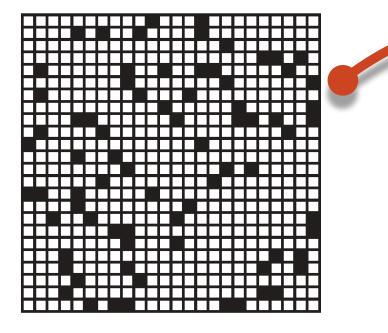
# Issue

Can we discover these properties mathematically?

Degree, Centrality, Closeness, Eccentricity, Betweenness,

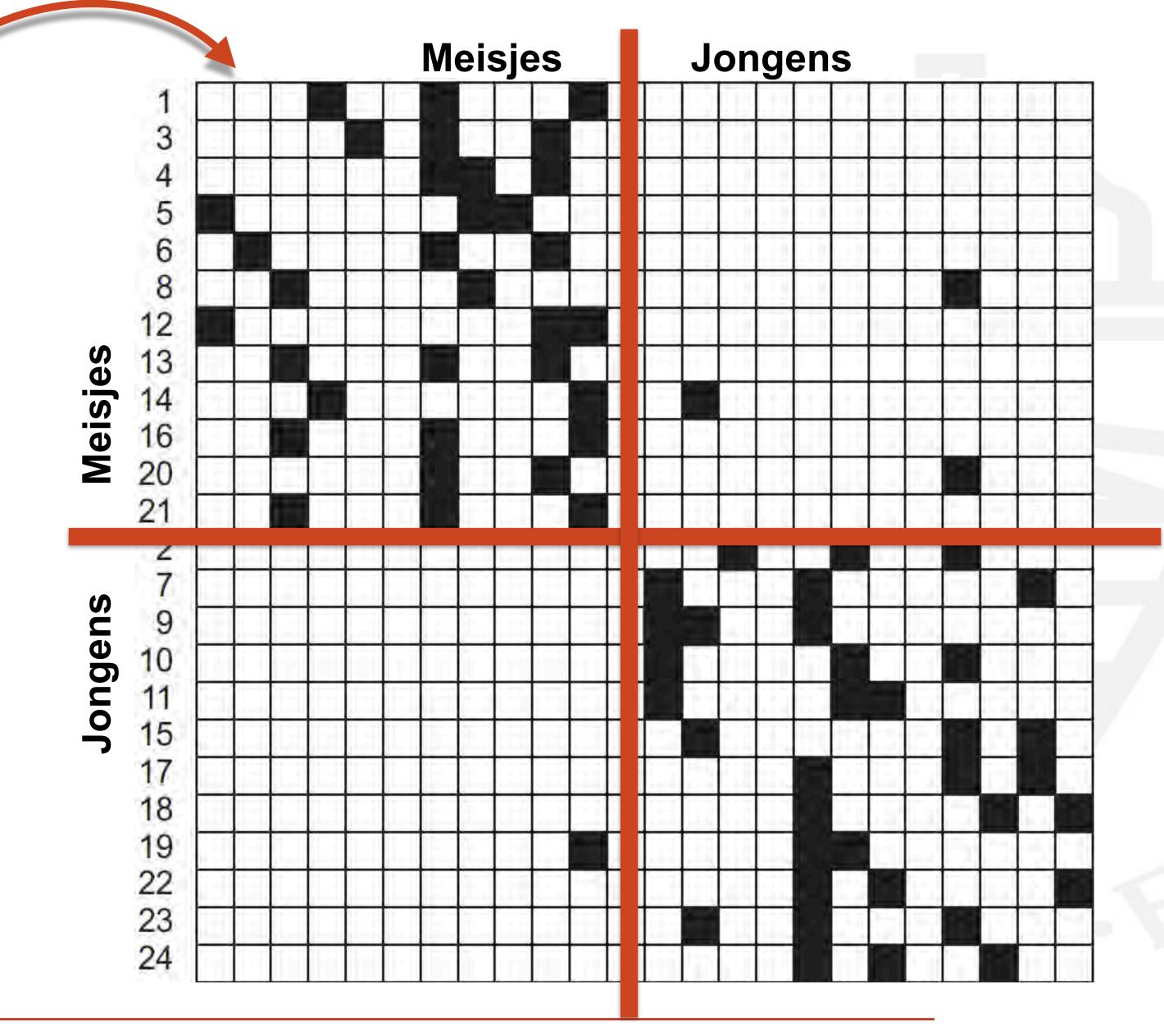
https://www.distributed-systems.net/index.php/books/gtcn/

# Sociale networks



Clusters (communities, subgraphs, modules)

"hubs"

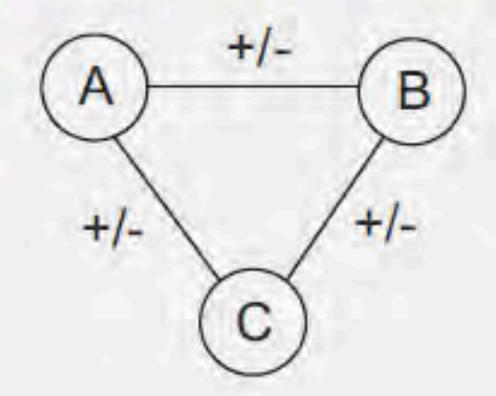


# Structural balance

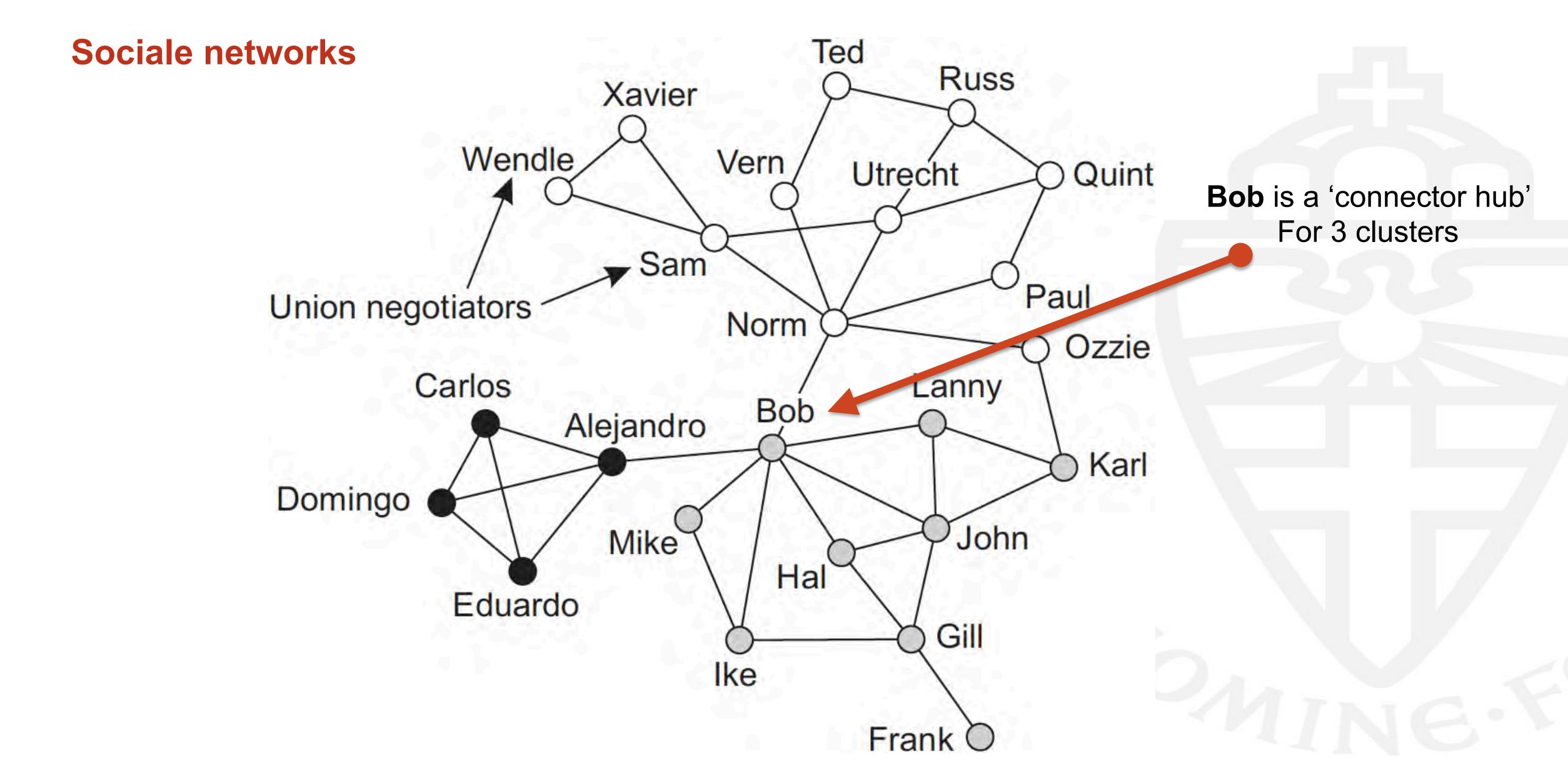
# Basic idea

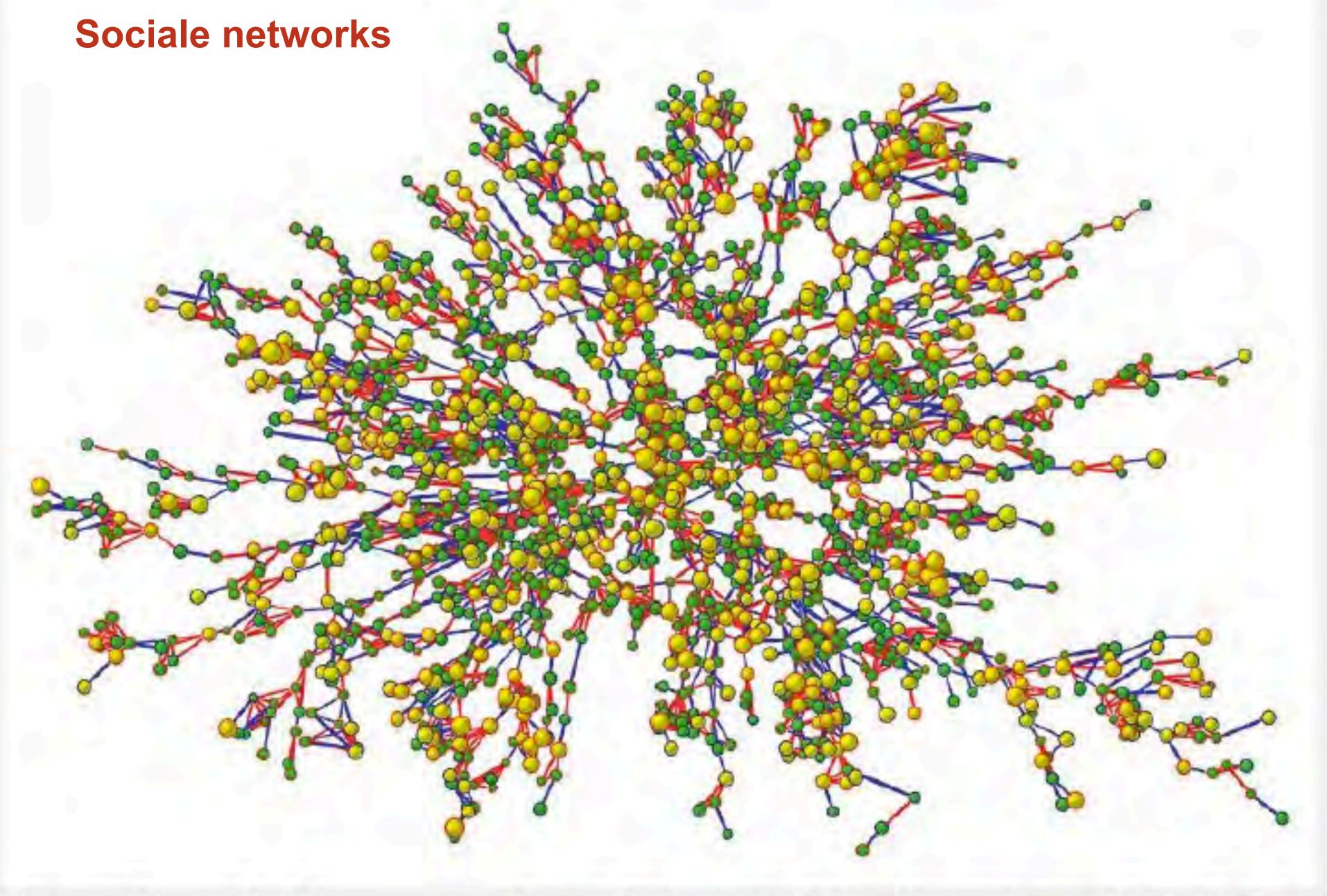
Consider **triads**: potential relationships between triples of social entities, and label every relationship as positive or negative. We then consider **balanced** triads.

# Motifs (signed) Motieven



A-B	B-C	A-C	B/I	Description			
+	+	+	В	Everyone likes each other			
+	+	-	1	like A–C stresses relation B has with either of them			
+		+	1	Dislike B-C stresses relation A has with either of them			
+	-	-	В	A and B like each other, and both dislike C			
181	+	+	1	Dislike A-B stresses relation C has with either of them			
-	+	-	В	B and C like each other, and both dislike A			
1300	3-63	+	В	A and C like each other, and both dislike B			
-	-	:3/	1	Nobody likes each other			



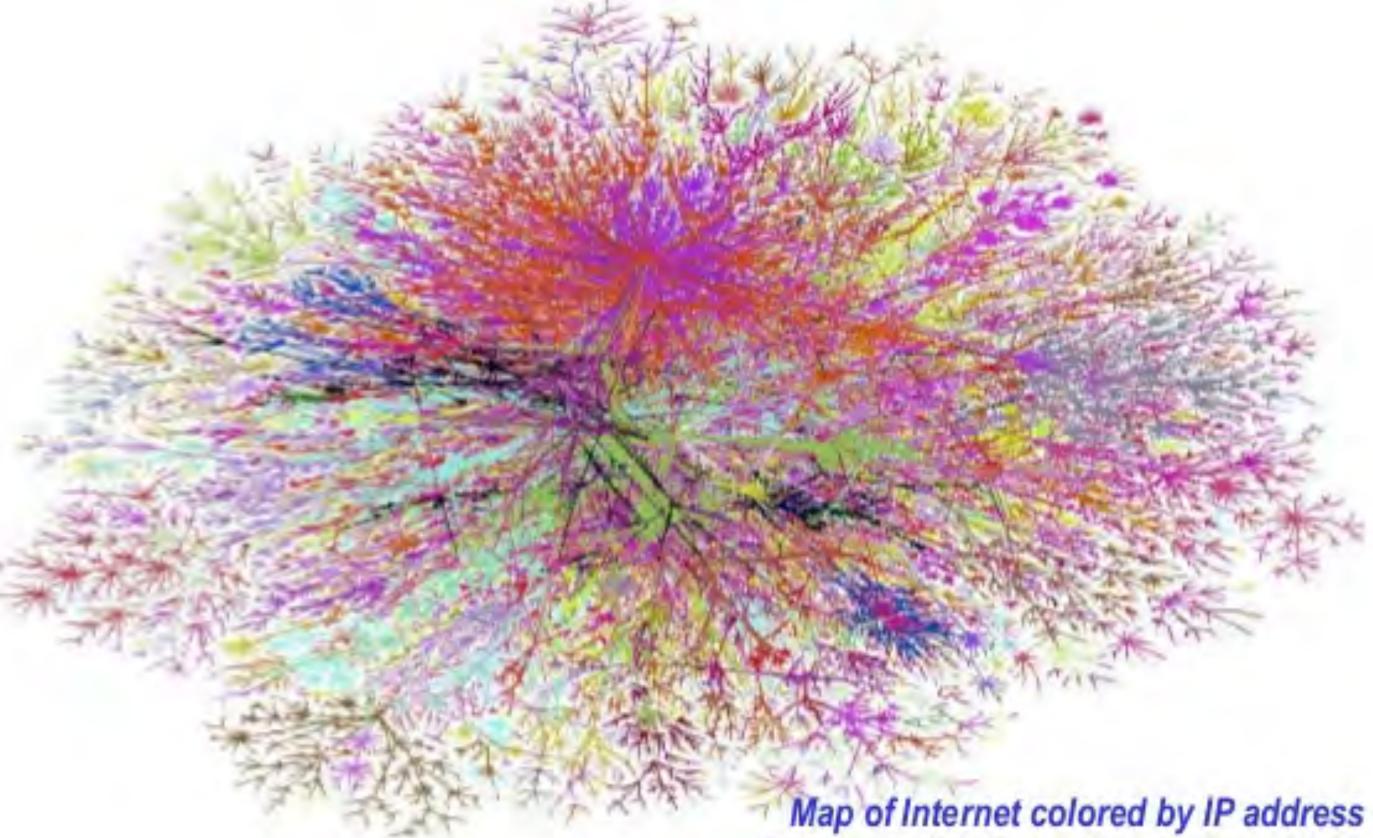


Yellow: obese | Green: nonobese | Purple: friend/marriage | Red: family

# Complexe 'sociale' networks

# Complex networks

Case studies: Internet

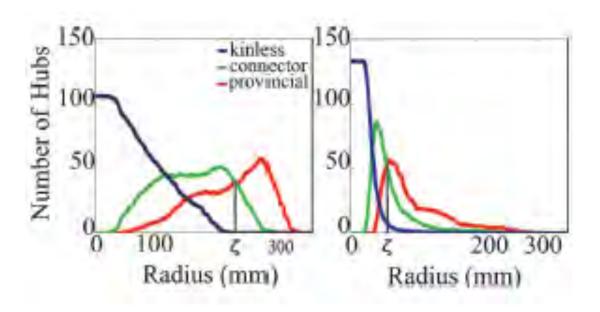


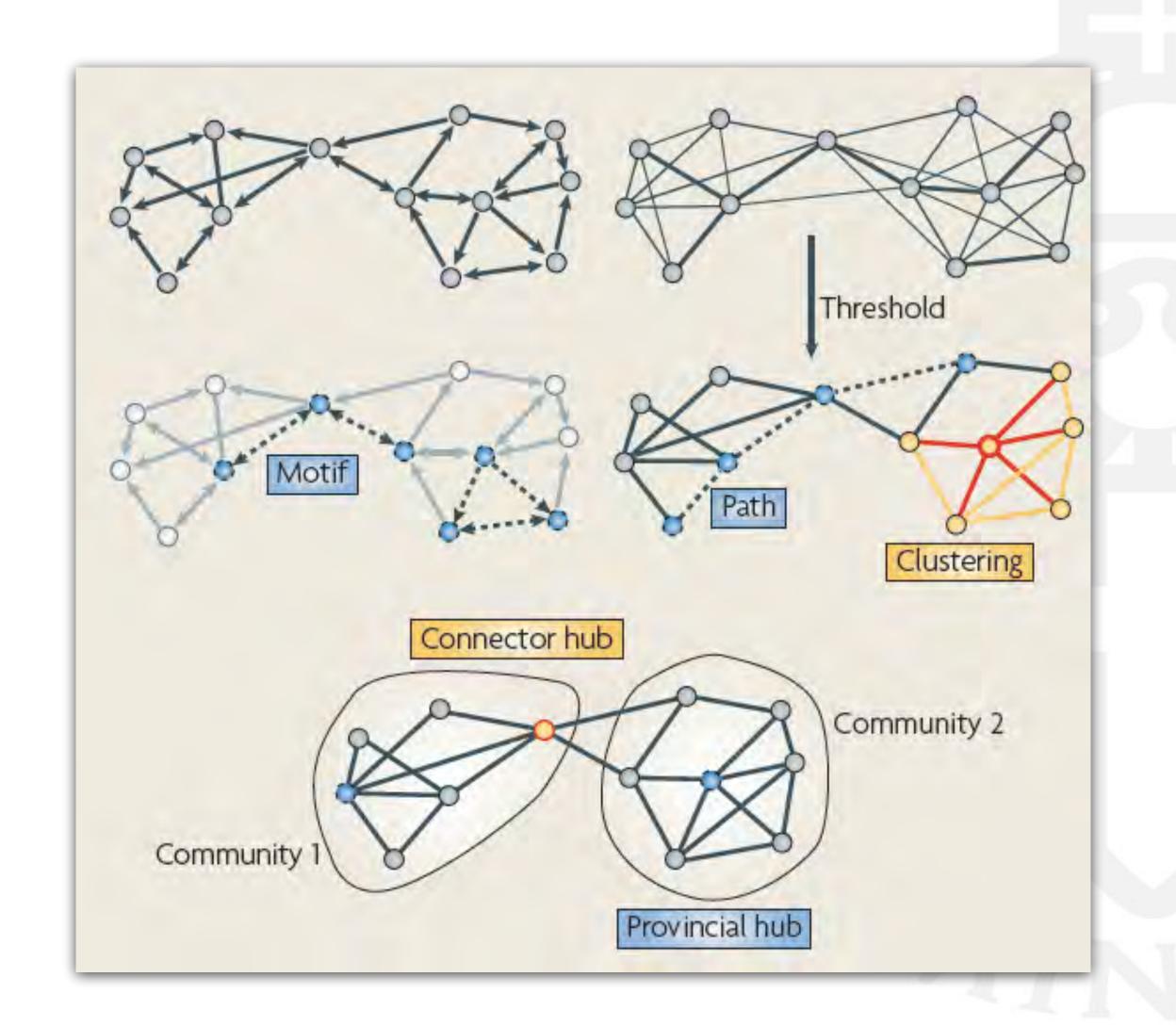
(Bill Cheswick & Hal Burch, http://research.lumeta.com/ches/map)



# A brand new zoo of complexity measures!

- Node degree
- Degree distribution
- Assortativity
- Clustering coefficient
- Motifs
- Path length
- Path efficiency
- Connection density or cost
- ●Hubs
- Centrality
- Robustness
- Modularity







Measure	Binary and undirected definitions	Weighted and directed definitions
Modularity	Modularity of the network (Newman, 2004b), $Q = \sum_{u \in M} \left[ e_{uu} - \left( \sum_{v \in M} e_{uv} \right)^2 \right],$ where the network is fully subdivided into a set of nonoverlapping modules $M$ , and $e_{uv}$ is the proportion of all links that connect nodes in module $u$ with nodes in module $v$ . An equivalent alternative formulation of the modularity (Newman, 2006) is given by $Q = \frac{1}{l} \sum_{ij \in N} \left( a_{ij} - \frac{k_i k_j}{l} \right) \delta_{m_i, m_j}$ , where $m_i$ is the module containing node $i$ , and $\delta_{m_i, m_j} = 1$ if $m_i = m_j$ , and $0$ otherwise.	Weighted modularity (Newman, 2004), $Q^{w} = \frac{1}{l^{w}} \sum_{i,j \in N} \left[ w_{ij} - \frac{k_{i}^{w} k_{j}^{w}}{l^{w}} \right] \delta_{m_{i},m_{j}}.$ Directed modularity (Leicht and Newman, 2008), $Q^{\rightarrow} = \frac{1}{l} \sum_{i,j \in N} \left[ a_{ij} - \frac{k_{i}^{out} k_{j}^{in}}{l} \right] \delta_{m_{i},m_{j}}.$
Measures of centrality Closeness centrality	Closeness centrality of node $i$ (e.g. Freeman, 1978), $L_i^{-1} = \frac{n-1}{\sum_{j\in N, j\neq i} d_{ij}}.$	Weighted closeness centrality, $(L_i^{w})^{-1} = \frac{n-1}{\sum_{j \in N, j \neq i} d_{ij}^{w}}$ . Directed closeness centrality, $(L_i^{\rightarrow})^{-1} = \frac{n-1}{\sum_{j \in N, j \neq i} d_{ij}^{w}}$ .
Betweenness centrality	Betweenness centrality of node $i$ (e.g., Freeman, 1978), $b_i = \frac{1}{(n-1)(n-2)} \sum_{\substack{h,j \in N \\ h \neq j, h \neq i, j \neq i,}} \frac{\rho_{hj}(i)}{\rho_{hj}}.$	Betweenness centrality is computed equivalently on weighted and directed networks, provided that path lengths are computed on respective weighted or directed paths.
Within-module degree z-score	where $\rho_{hj}$ is the number of shortest paths between $h$ and $j$ , and $\rho_{hj}$ ( $i$ ) is the number of shortest paths between $h$ and $j$ that pass through $i$ . Within-module degree $z$ -score of node $i$ (Guimera and Amaral, 2005), $z_i = \frac{k_i(m_i) - \overline{k}(m_i)}{\sigma^{k(m_i)}},$	Weighted within-module degree z-score, $z_i^{w} = \frac{k_i^{w}(m_i) - \overline{k}^{w}(m_i)}{\sigma^{k^{w}(m_i)}}$ . Within-module out-degree z-score, $z_i^{out} = \frac{k_i^{out}(m_i) - \overline{k}^{out}(m_i)}{\sigma^{k^{out}}(m_i)}$ . Within-module in-degree z-score, $z_i^{in} = \frac{k_i^{in}(m_i) - \overline{k}^{in}(m_i)}{\sigma^{k^{out}}(m_i)}$ .
	where $m_i$ is the module containing node $i$ , $k_i$ ( $m_i$ ) is the within-module degree of $i$ (the number of links between $i$ and all other nodes in $m_i$ ), and $\overline{k}(m_i)$ and $\sigma^{k(m_i)}$ are the respective mean and standard deviation of the within-module $m_i$ degree distribution.	



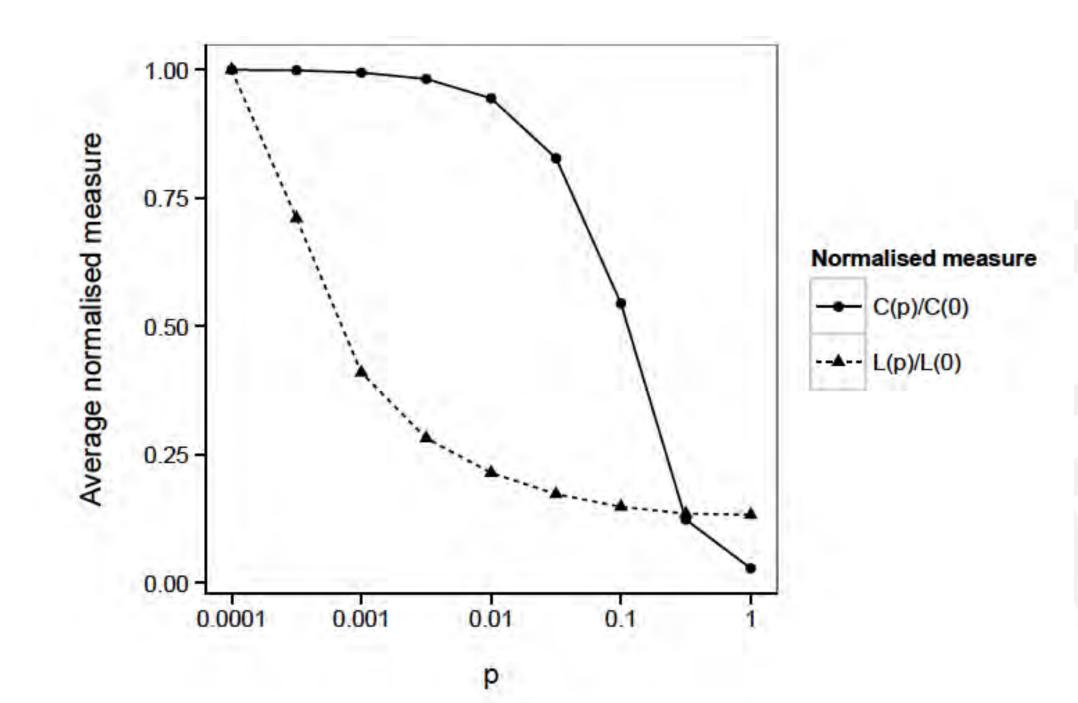
# Network / Graph topology: It's a Small World After All

### "small-world" test:

Average path length (L)

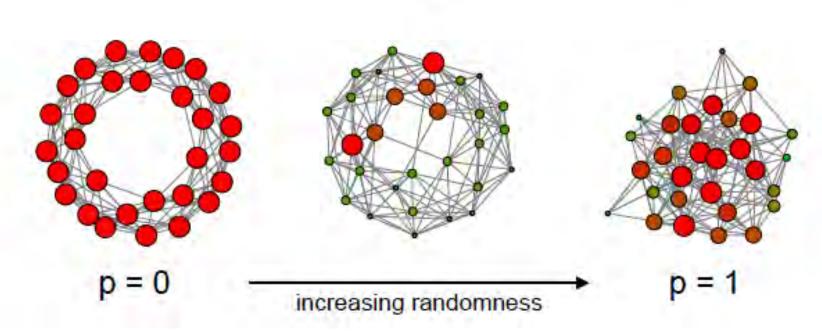
Clustering coefficient (C)

Compare to randomly rewired version



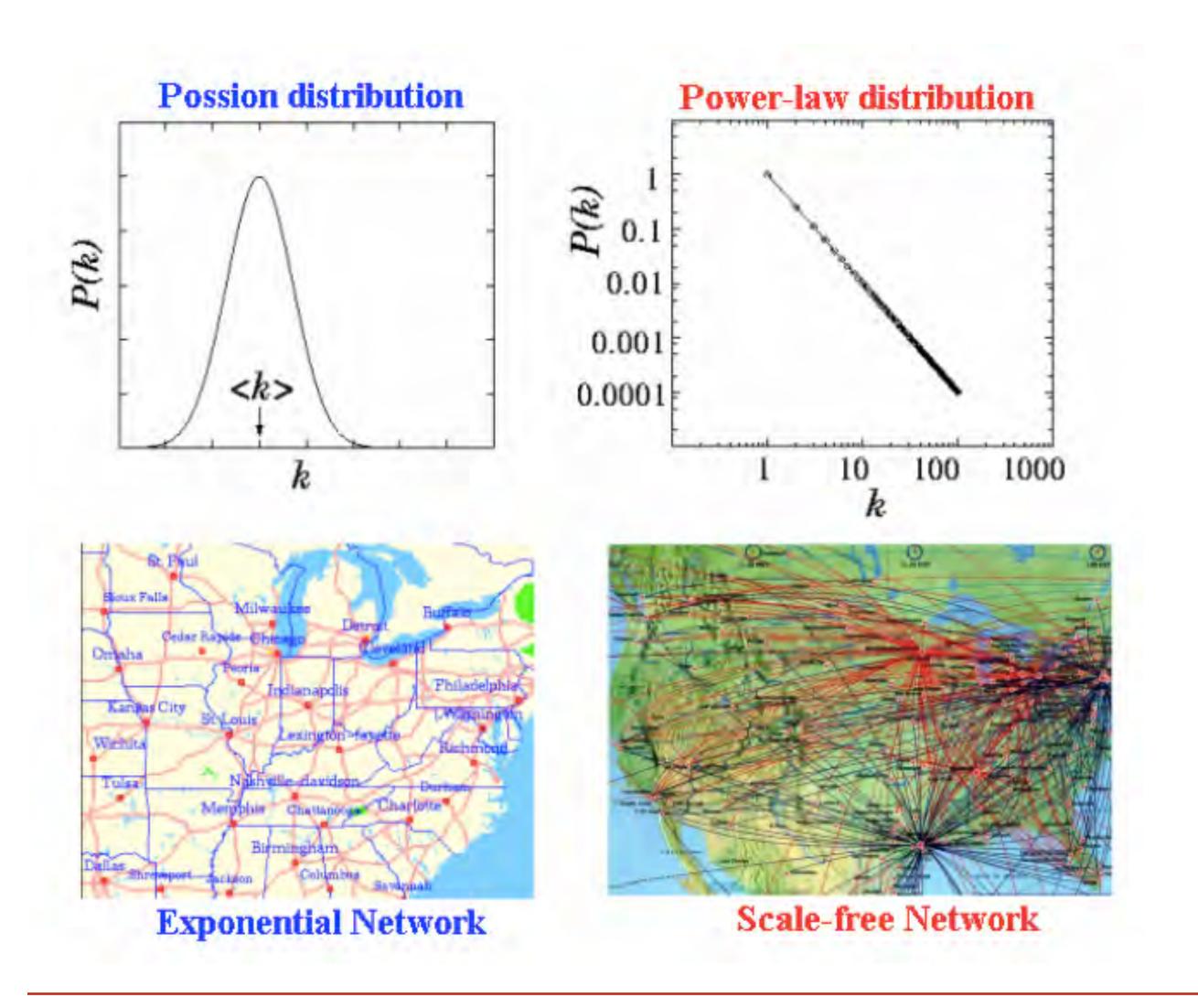
# Sound familiar?

In between fully ordered & completely random = optimal





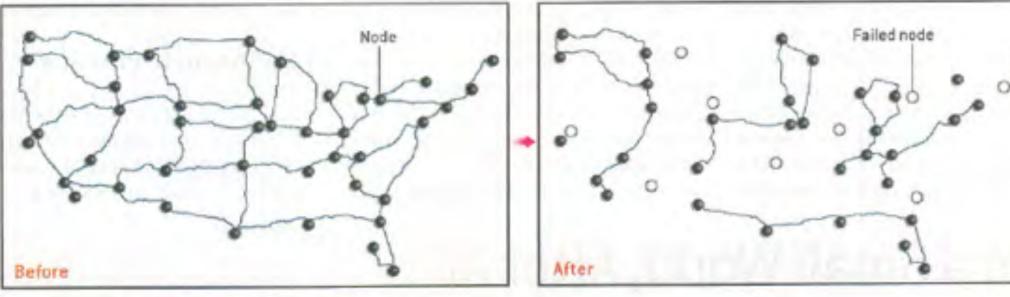
# Network / Graph topology: It's a Scale Free World After All



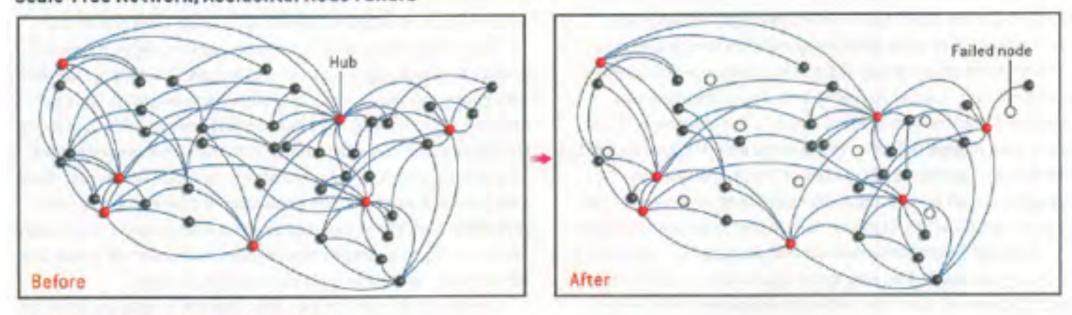
Number of connections a node in the network has: degree (δ)

Scale-free network: degree distribution is a power law!

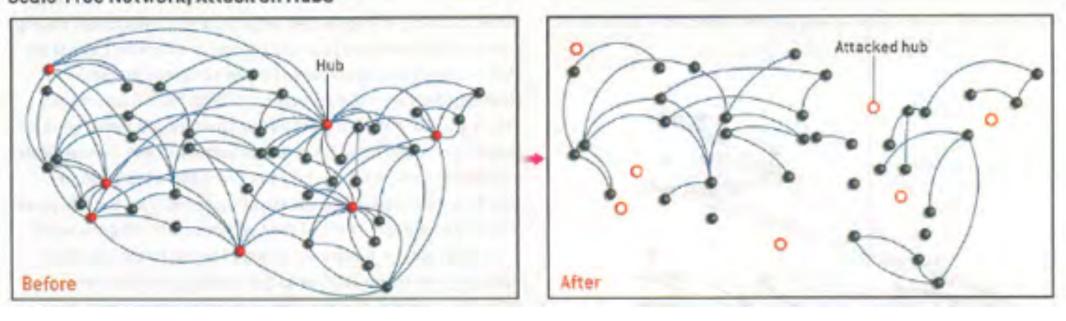
### Random Network, Accidental Node Failure



Scale-Free Network, Accidental Node Failure



Scale-Free Network, Attack on Hubs



Scale free networks are resilient to random attacks on nodes or node failures (cf. internet on 9/11)

when more hub nodes fail though....

targeted attack!

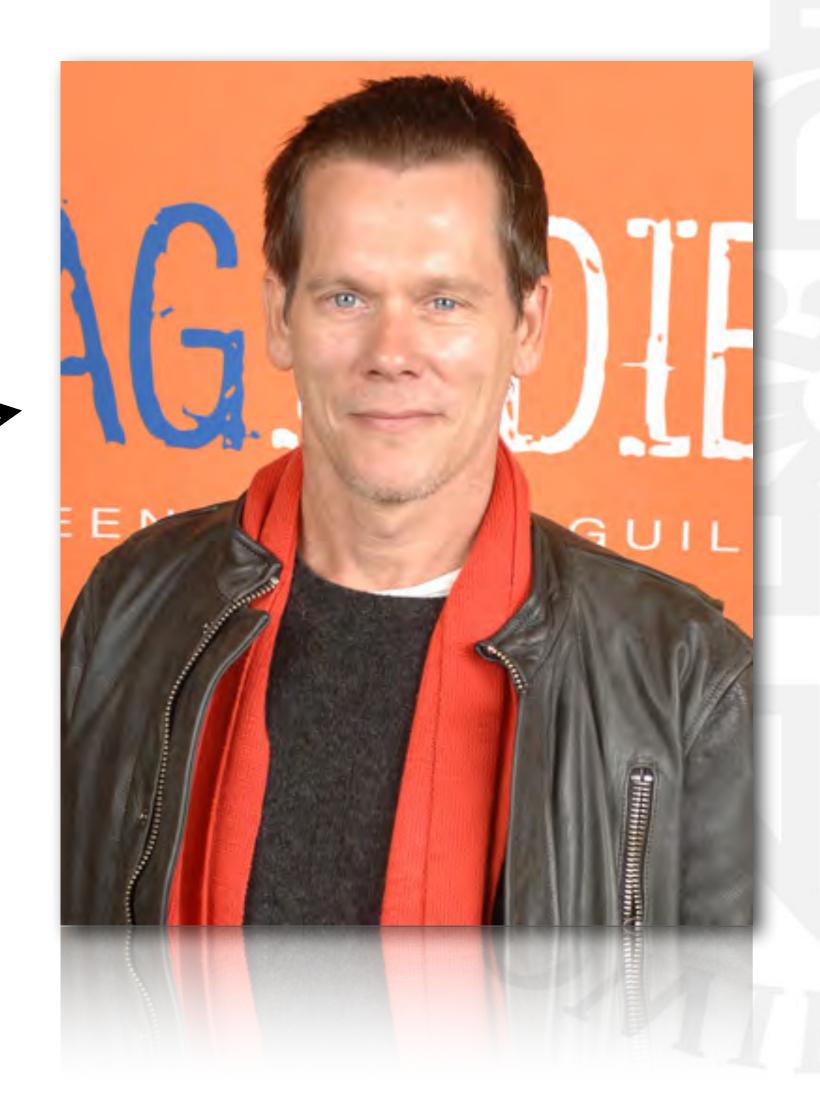
# Effectiveness / Connectivity: 6 degrees of separation

# Kevin Bacon number (Erdős number)

- Node degree
- Degree distribution
- Assortativity
- Clustering coefficient
- Motifs
- Path length
- Path efficiency
- Connection density or cost
- Hubs
- Centrality
- Robustness
- Modularity

Degree of separation (from Kevin Bacon)

'6 degrees of separation'



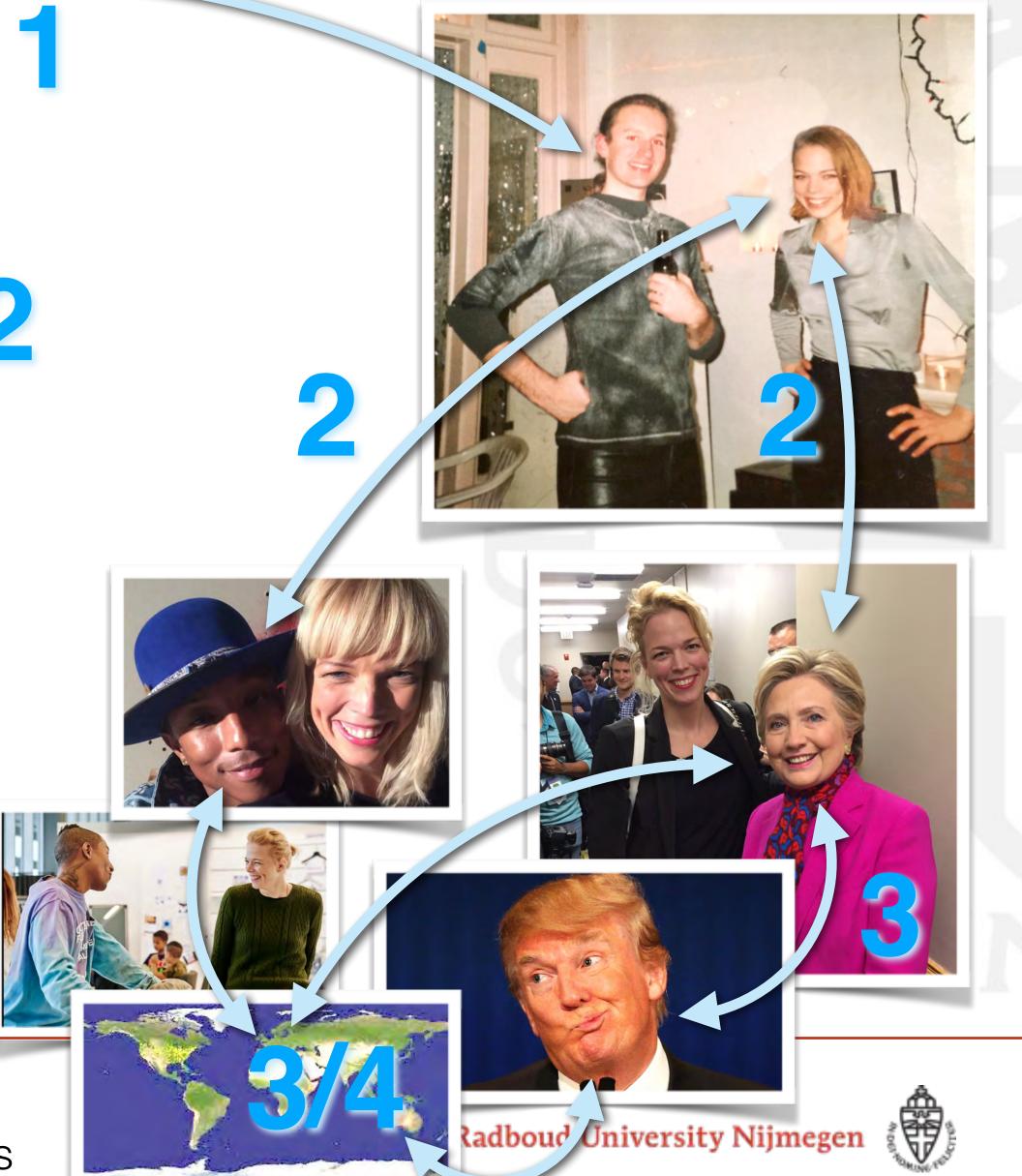
# Effectiveness / Connectivity: 6 degrees of separation

# Your degree of separation from:

Nobel Laureate 1/2

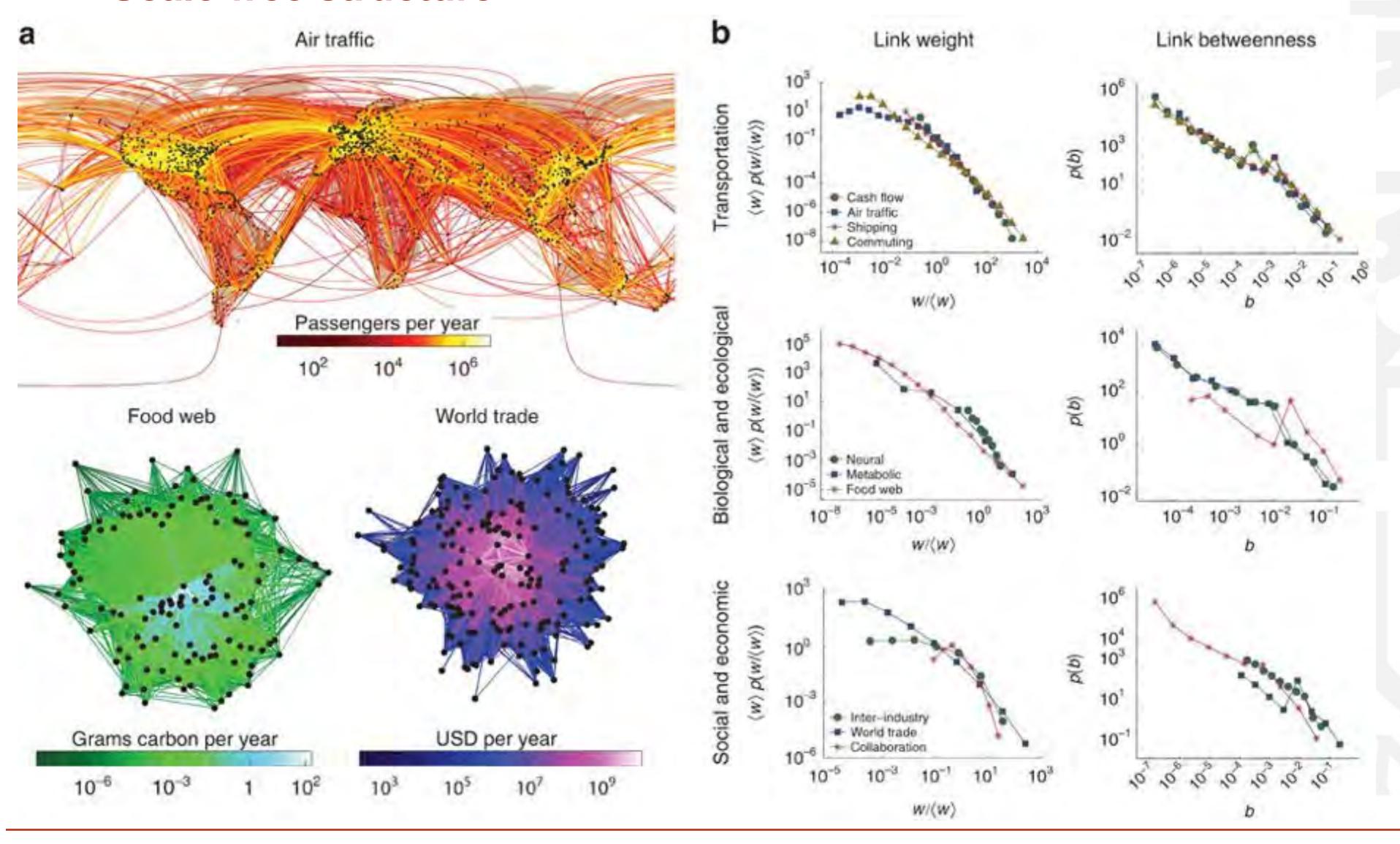
Pharrell Williams

Hillary Clinton
Donald Trump



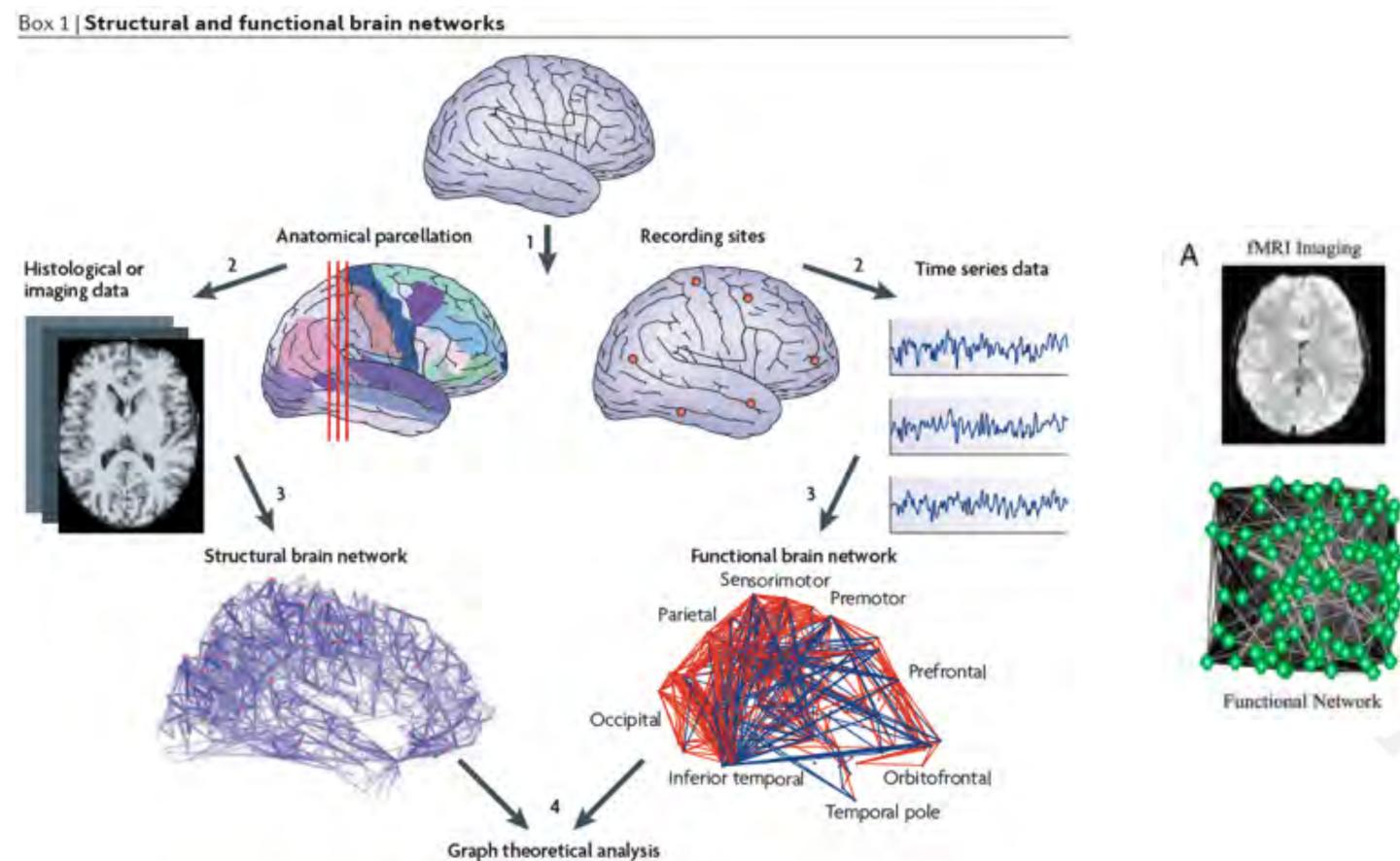
http://en.wikipedia.org/wiki/ Bacon\_number#Bacon\_numbers

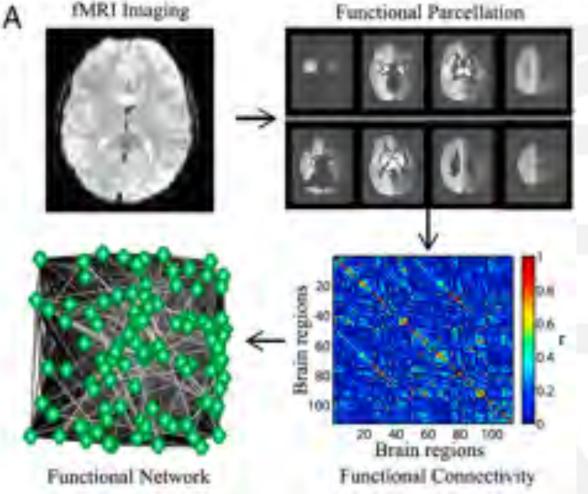
# **Scale-free structure**



# **Network / Graph topology**

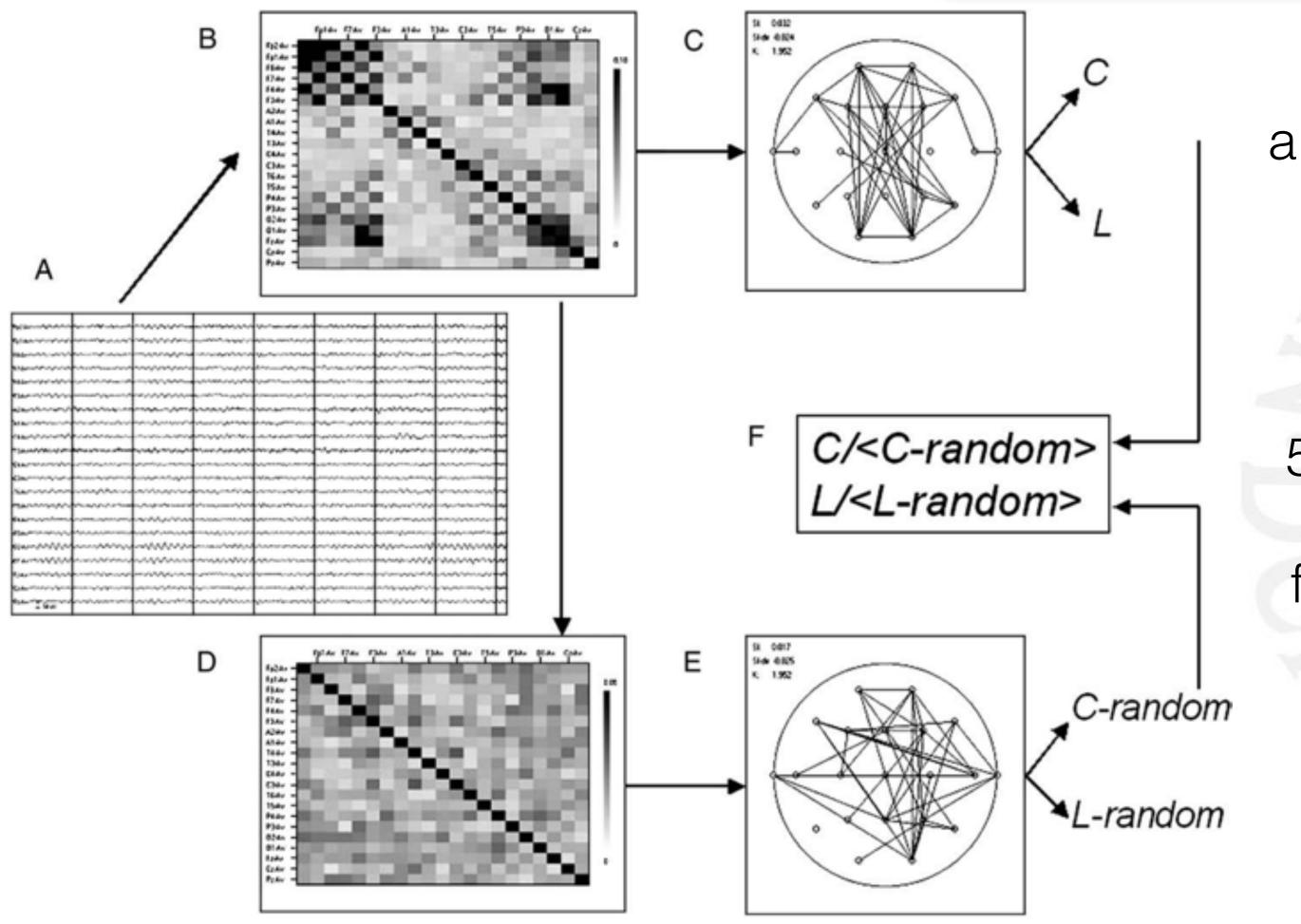
# Functional vs. Structural networks





# **Network / Graph topology**

# How to get the matrices

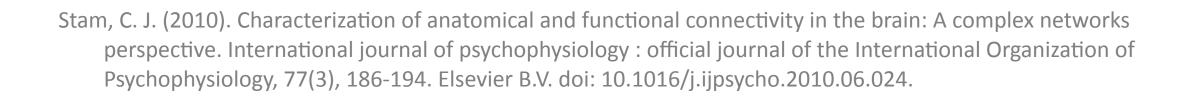


Adjacency matrix and weighted graph can be extracted from resting state recordings:

5 min. eyes closed

find 4096 samples without artefacts

That's about 6-7 seconds!

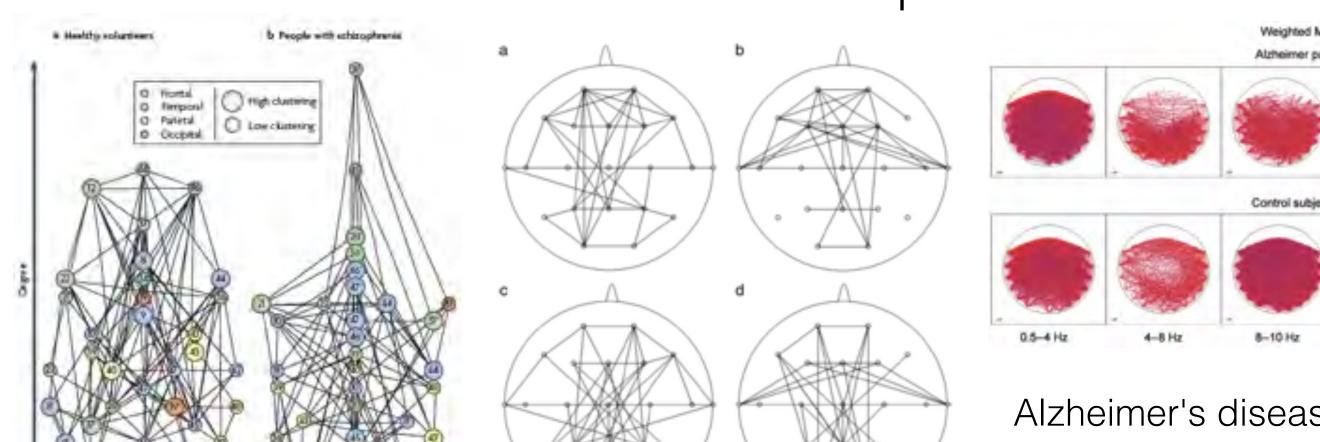




# **Network / Graph topology**

# Pathology studies

Based on a few samples we can distinguish healthy subjects from patients:



Alzheimer's disease: Targeted attack on hubs!

Schizophrenia

Absence seizure

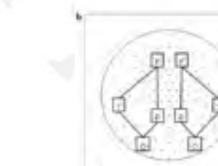
Bartolomei, F., Bosma, I., Klein, M., Baayen, J. C., Reijneveld, J. C., Postma, T. J., et al. (2006). Disturbed functional connectivity in brain tumour patients: evaluation by graph analysis of synchronization matrices. Clinical neurophysiology, 117(9), 2039-49. doi: 10.1016/j.clinph.2006.05.018.

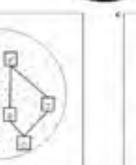
Ponten, S. C., Douw, L., Bartolomei, F., Reijneveld, J. C., & Stam, C. J. (2009). Indications for network regularization during absence seizures: weighted and unweighted graph theoretical analyses. Experimental neurology, 217(1), 197-204. Elsevier Inc. doi: 10.1016/j.expneurol.2009.02.001.

Stam, C. J., Haan, W. de, Daffertshofer, a, Jones, B. F., Manshanden, I., Cappellen van Walsum, a M. van, et al. (2009). Graph theoretical analysis of magnetoencephalographic functional connectivity in Alzheimer's disease. Brain: a journal of neurology, 132(Pt 1), 213-24. doi: 10.1093/brain/awn262.

Stam, C. J. (2010). Use of magnetoencephalography (MEG) to study functional brain networks in neurodegenerative disorders. Journal of the neurological sciences, 289(1-2), 128-34. Elsevier B.V. doi: 10.1016/j.jns.2009.08.028.

Parkinson's





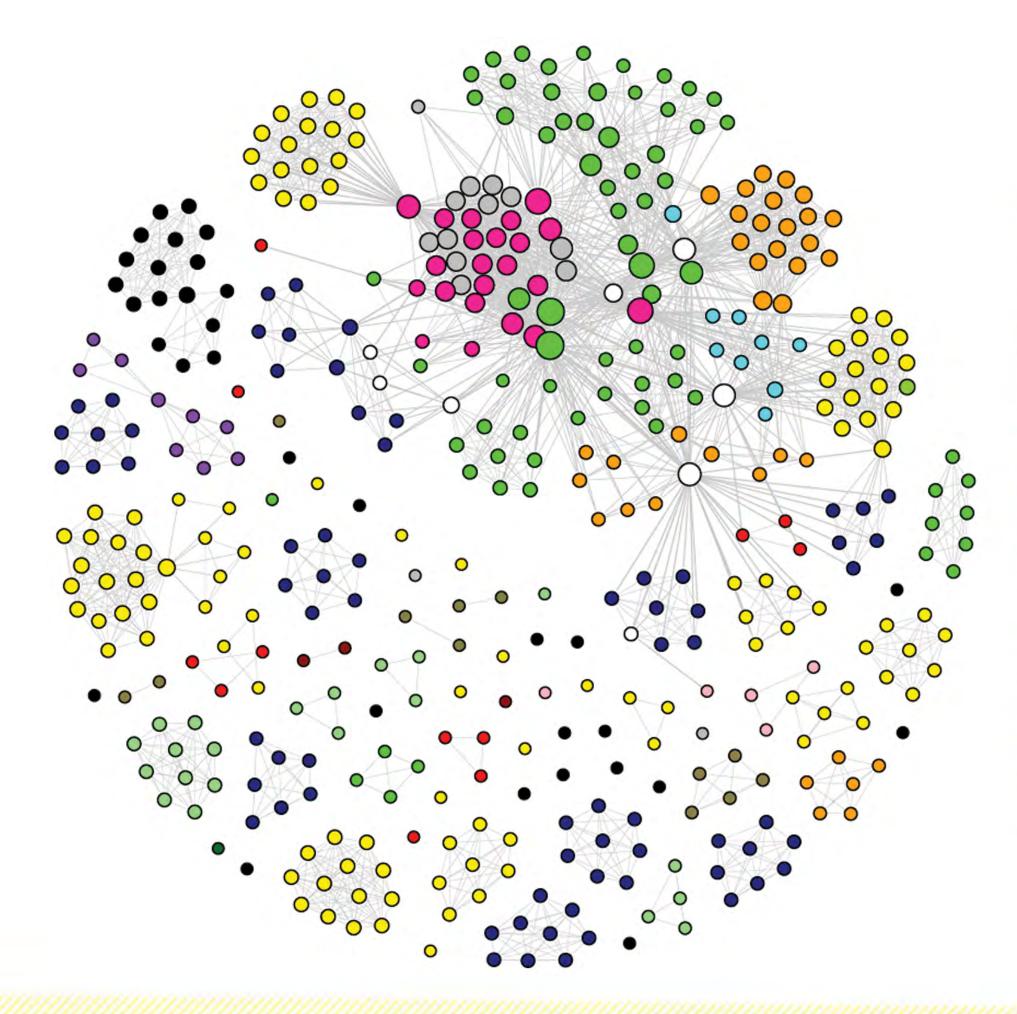


Epilepsy

brain tumor patients



# Symptom networks Small-world of DSM-IV

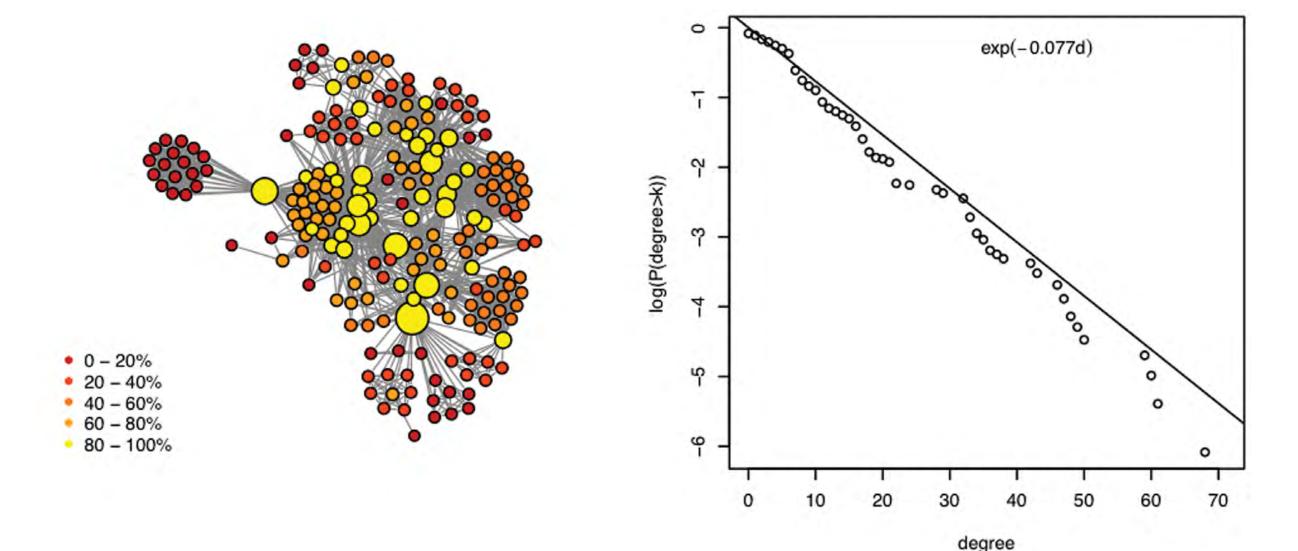


## Problemen met het medisch model by psychopathologie:

- geen unieke veroorzaker voor symptomen, zoals griepvirus
- symptomen zijn vaak de diagnose en oorzaak tegelijk
- Disorders usually first diagnosed in infancy, childhood or adolescence
- Delirium, dementia, and amnesia and other cognitive disorders
- Mental disorders due to a general medical condition
- Substance-related disorders
- Schizophrenia and other psychotic disorders
- Mood disorders
- Anxiety disorders
- Somatoform disorders
- Facitious disorders
- Dissociative disorders
- Sexual and gender identity disorders
- Eating disorders
- Sleep disorders
- Impulse control disorders not elsewhere classified
- Adjustment disorders
- Personality disorders
- Symptom is featured equally in multiple chapters



# Symptom networks



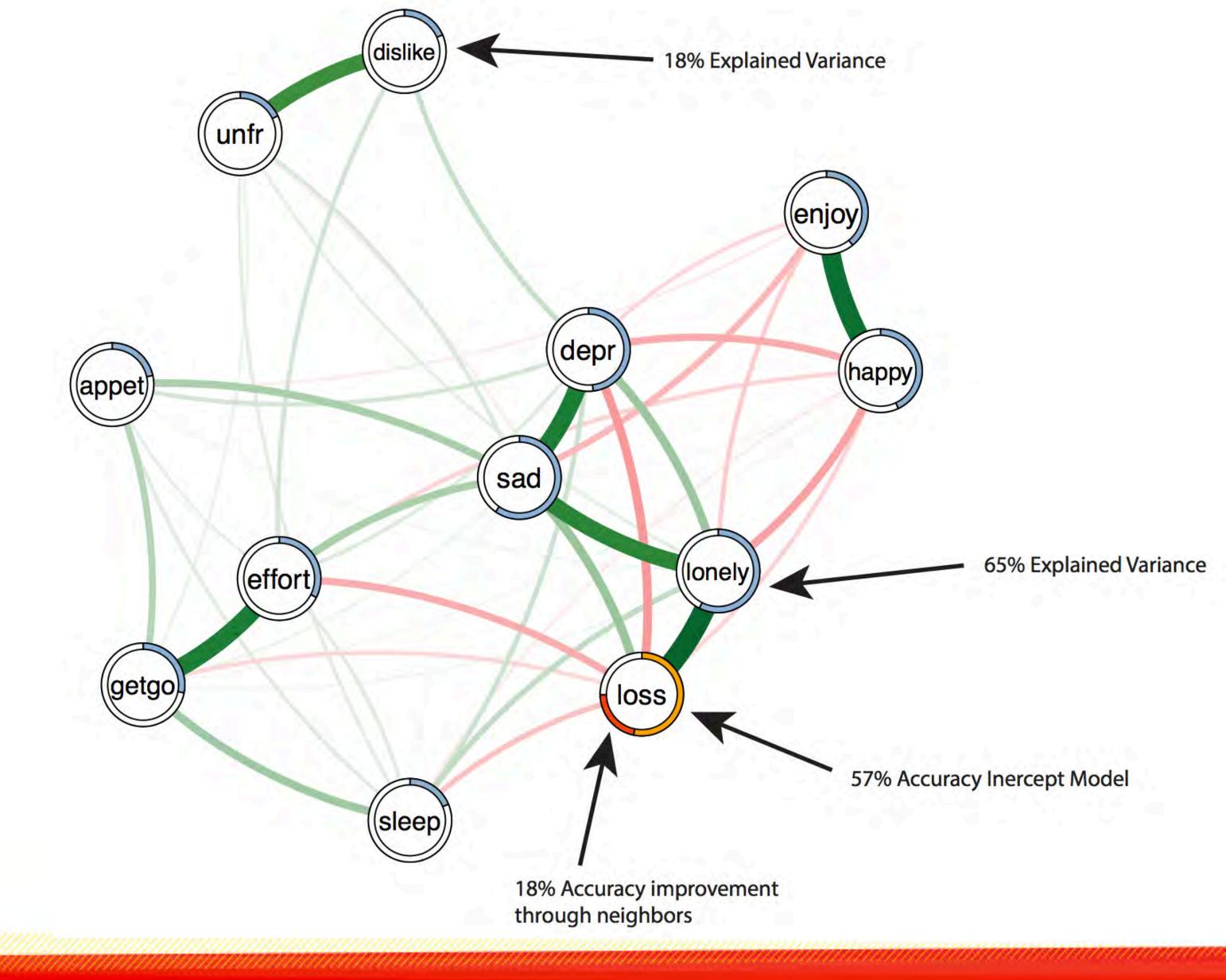
### We show that

- a) half of the symptoms in the DSM-IV network are connected,
- b) the architecture of these connections conforms to a small world structure, featuring a high degree of clustering but a short average path length, and
- c) distances between disorders in this **structure predict empirical comorbidity rates**. Network simulations of Major Depressive Episode and Generalized Anxiety Disorder show that the model faithfully reproduces empirical population statistics for these disorders.

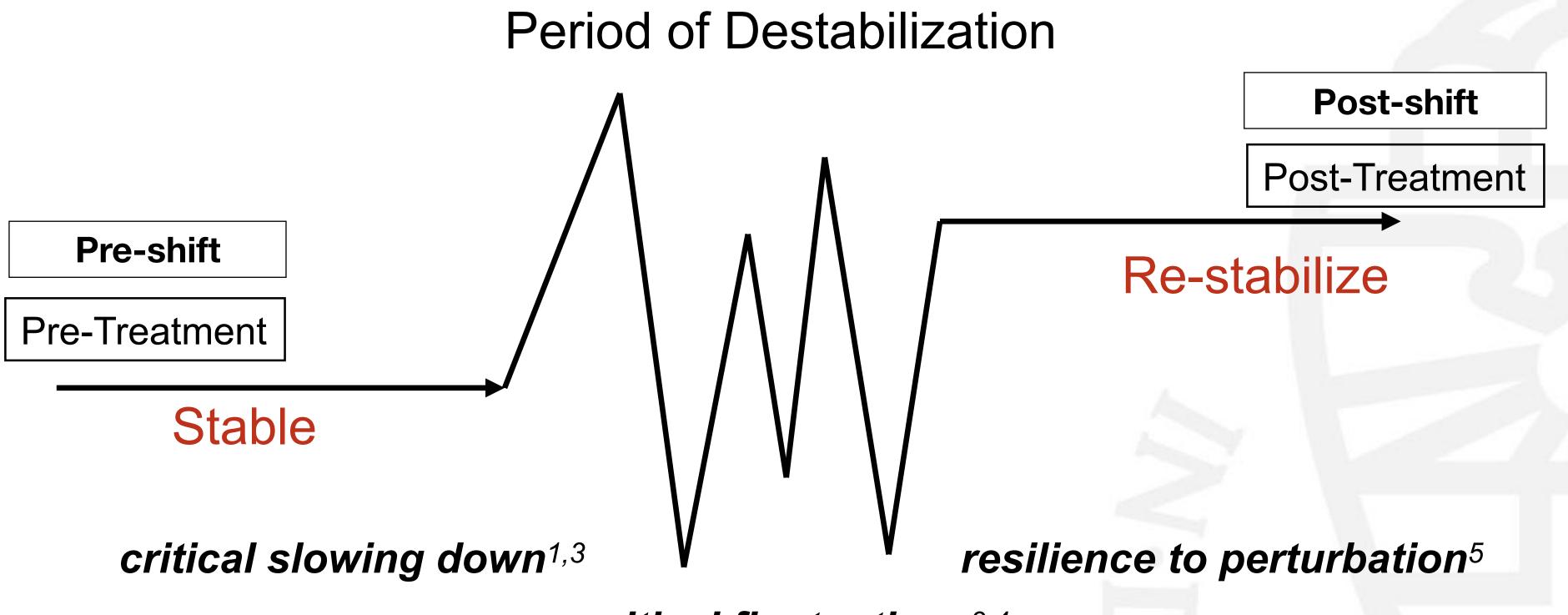


# Symptom netwerken

psychosystems.org







- critical fluctuations<sup>3,4</sup>
- increase in recovery and switching time after perturbation
- increase in variance, autocorrelation, long-range dependence
  - increase in occurrence and diversity of unstable states
- increase in the entropy of the distribution of state occurrences

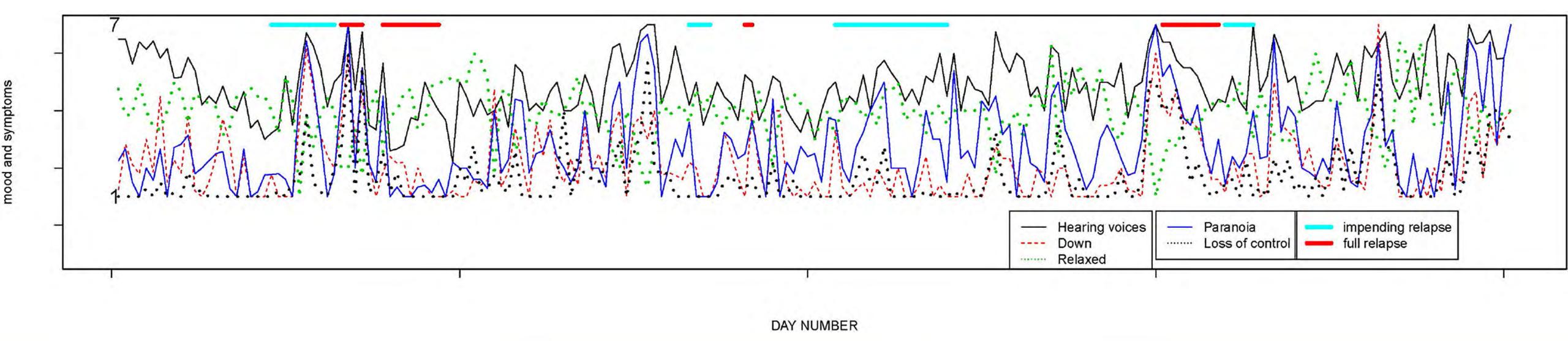
<sup>&</sup>lt;sup>1</sup>Scholz JP, Kelso JAS, Schöner G. (1987). Nonequilibrium phase transitions in coordinated biological motion: critical slowing down and switching time. *Physics Letters A 123*, 390–394.

<sup>&</sup>lt;sup>2</sup>Scheffer M, Bascompte J, Brock W A, Brovkin V, Carpenter SR, Dakos V, Held H, van Nes EH, Rietkerk M, Sugihara G. (2009). Early-warning signals for critical transitions. *Nature* 461, 53–9.

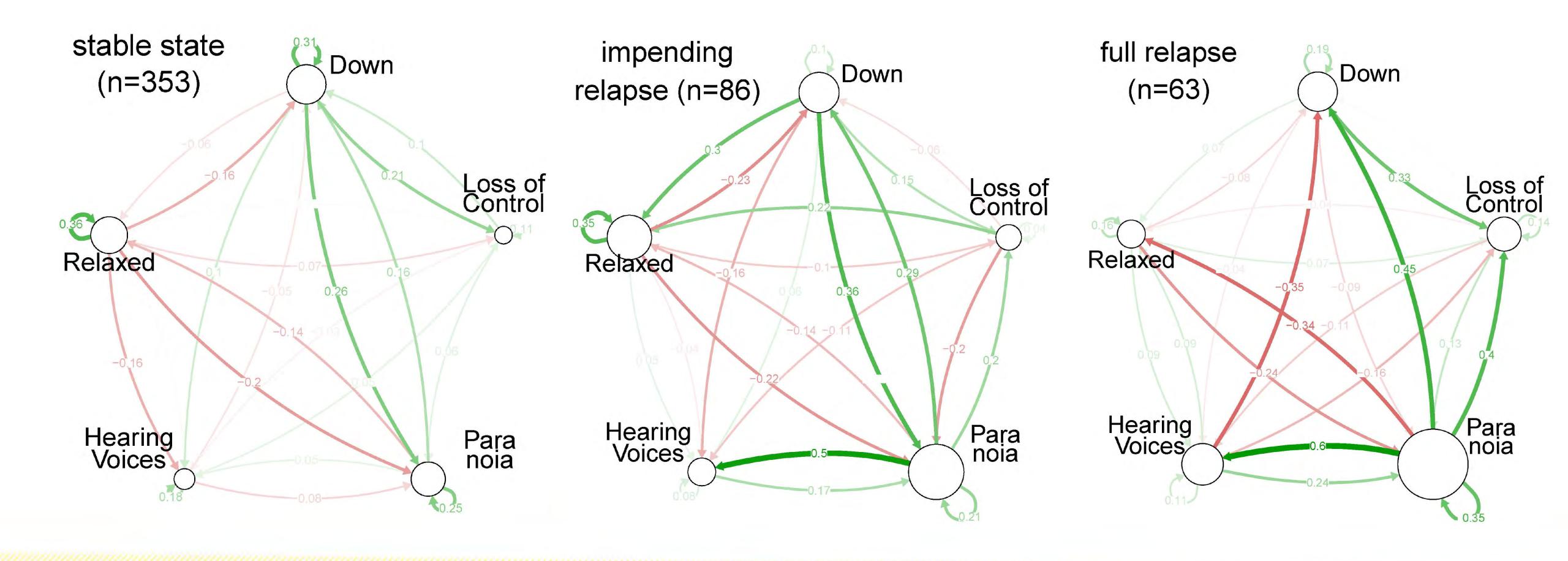
<sup>&</sup>lt;sup>3</sup>Stephen DG, Dixon JA, Isenhower RW. (2009). Dynamics of representational change: Entropy, Action and Cognition. *JEP: Human Perception and Performance 35*, 1811–1832. <sup>4</sup>Schiepek G, Strunk G. (2010). The identification of critical fluctuations and phase transitions in short term and coarse-grained time series ... *Biological cybernetics 102*,197–207.

# An n=1 Clinical Network Analysis of Symptoms and Treatment in Psychosis

variation in 'hearing voices', 'down', 'paranoia', 'loss of control' and 'relaxed' (range 1-7) during a year



# An n=1 Clinical Network Analysis of Symptoms and Treatment in Psychosis



## An n=1 Clinical Network Analysis of Symptoms and Treatment in Psychosis

	Betweenness	Closeness	Inward degree	Outward degree	Node strength
Stable state					
'Down'	5	0.032	0.78	0.92	1.70
Loss of control'	0	0.015	0.45	0.31	0.76
Paranoia'	4	0.026	0.87	0.62	1.48
Hearing Voices'	0	0.015	0.51	0.39	0.90
Relaxed'	1	0.036	0.61	0.98	1.59
mpending relapse					
Down'	2	0.056	0.74	1.07	1.81
Loss of control'	0	0.040	0.51	0.64	1.15
Paranoia'	7	0.058	1.16	1.34	2.49
Hearing Voices'	0	0.026	0.90	0.35	1.25
Relaxed'	0	0.039	1.05	0.95	2.00
Full Relapse state					
Down'	1	0.025	1.08	0.72	1.80
Loss of control'	3	0.027	1.12	0.44	1.56
Paranoia'	7	0.109	1.04	2.18	3.22
Hearing Voices'	0	0.050	0.95	0.95	1.90
Relaxed'	0	0.041	0.69	0.59	1.28

The Spearman correlations as suggested by reviewer #1

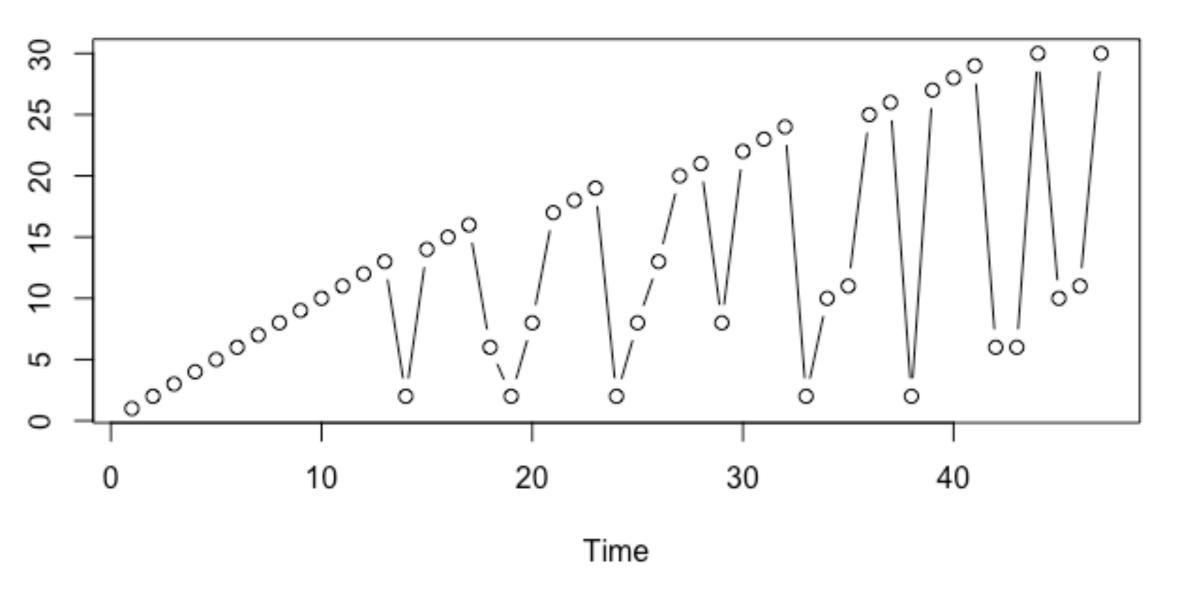
doi:10.1371/journal.pone.0162811.t002



## Recurrence Quantification Analysis: Nominale Tijdseries

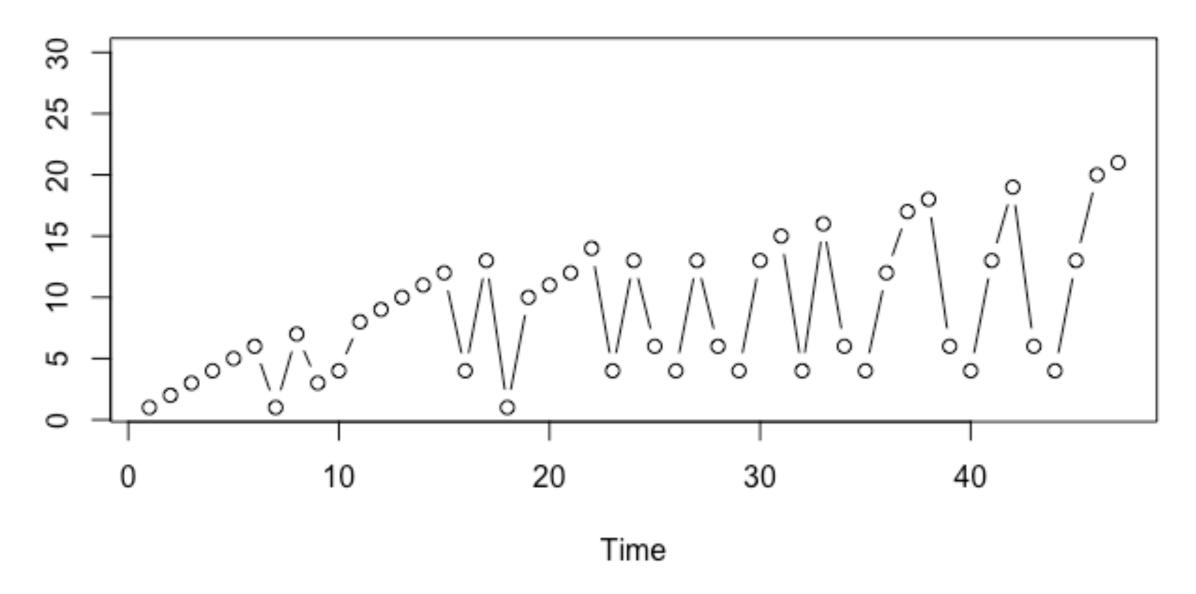
#### **VERHAAL 1**

"1 2 3 4 5 6 7 8 9 10 11 12 13 2 14 15 16 6 2 8 17 18 19 2 8 13 20 21 8 22 23 24 2 10 11 25 26 2 27 28 29 6 6 30 10 11 30"

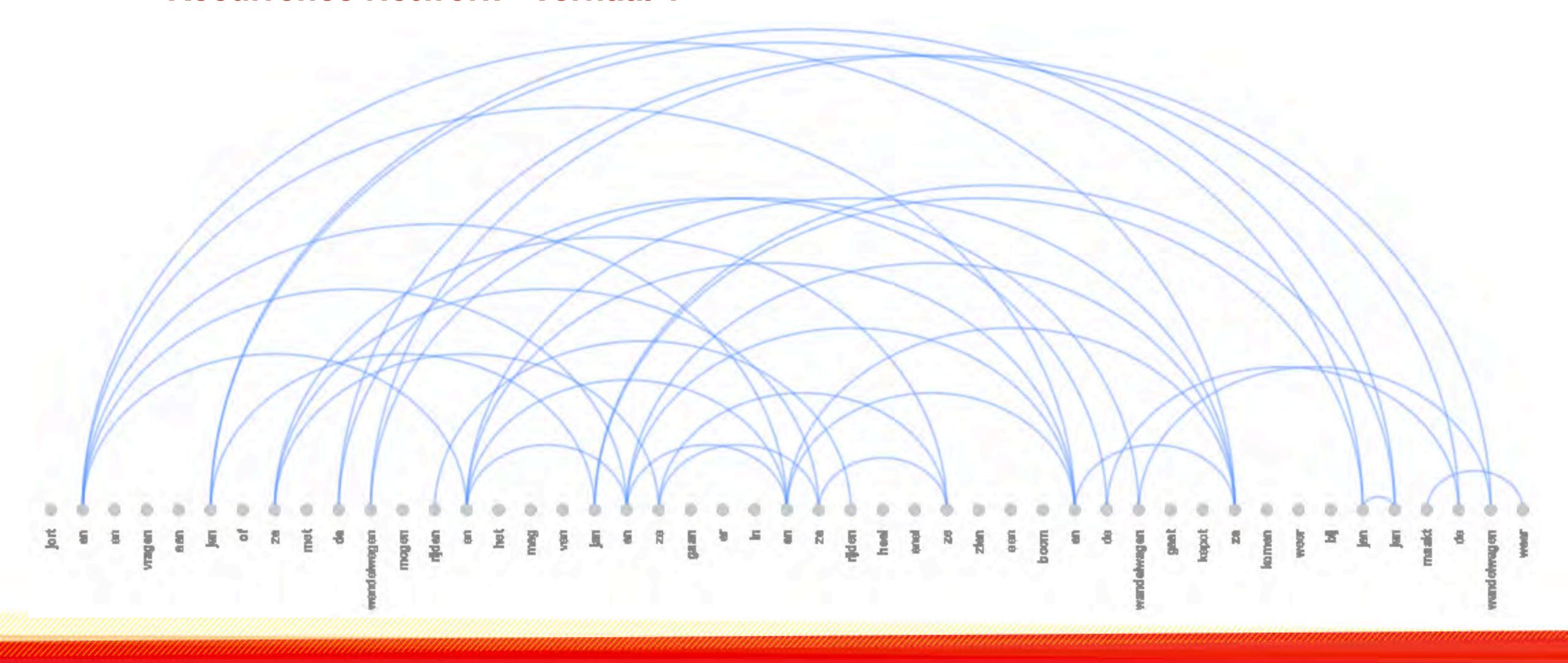


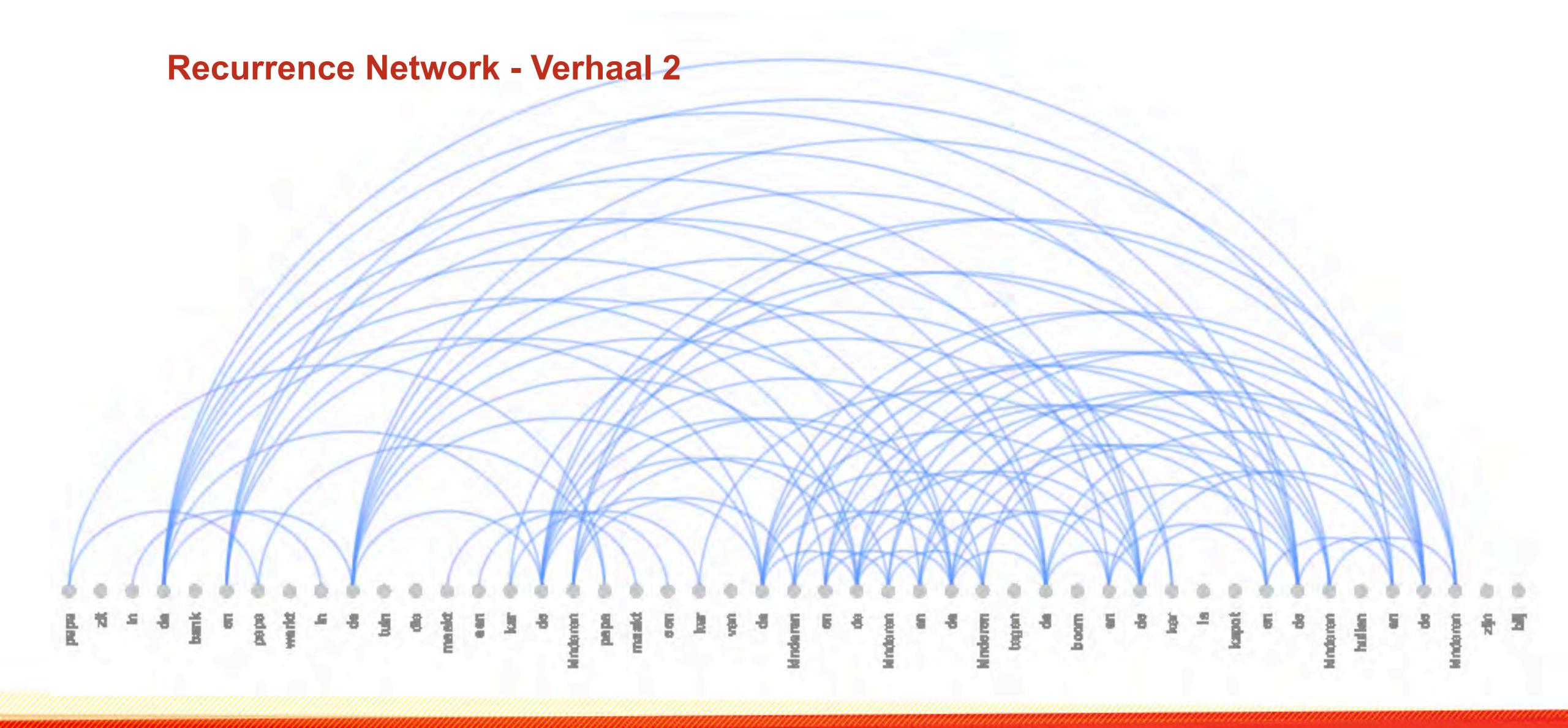
#### **VERHAAL 2**

"1 2 3 4 5 6 1 7 3 4 8 9 10 11 12 4 13 1 10 11 12 14 4 13 6 4 13 6 4 13 15 4 16 6 4 12 17 18 6 4 13 19 6 4 13 20 21"



## **Recurrence Network - Verhaal 1**





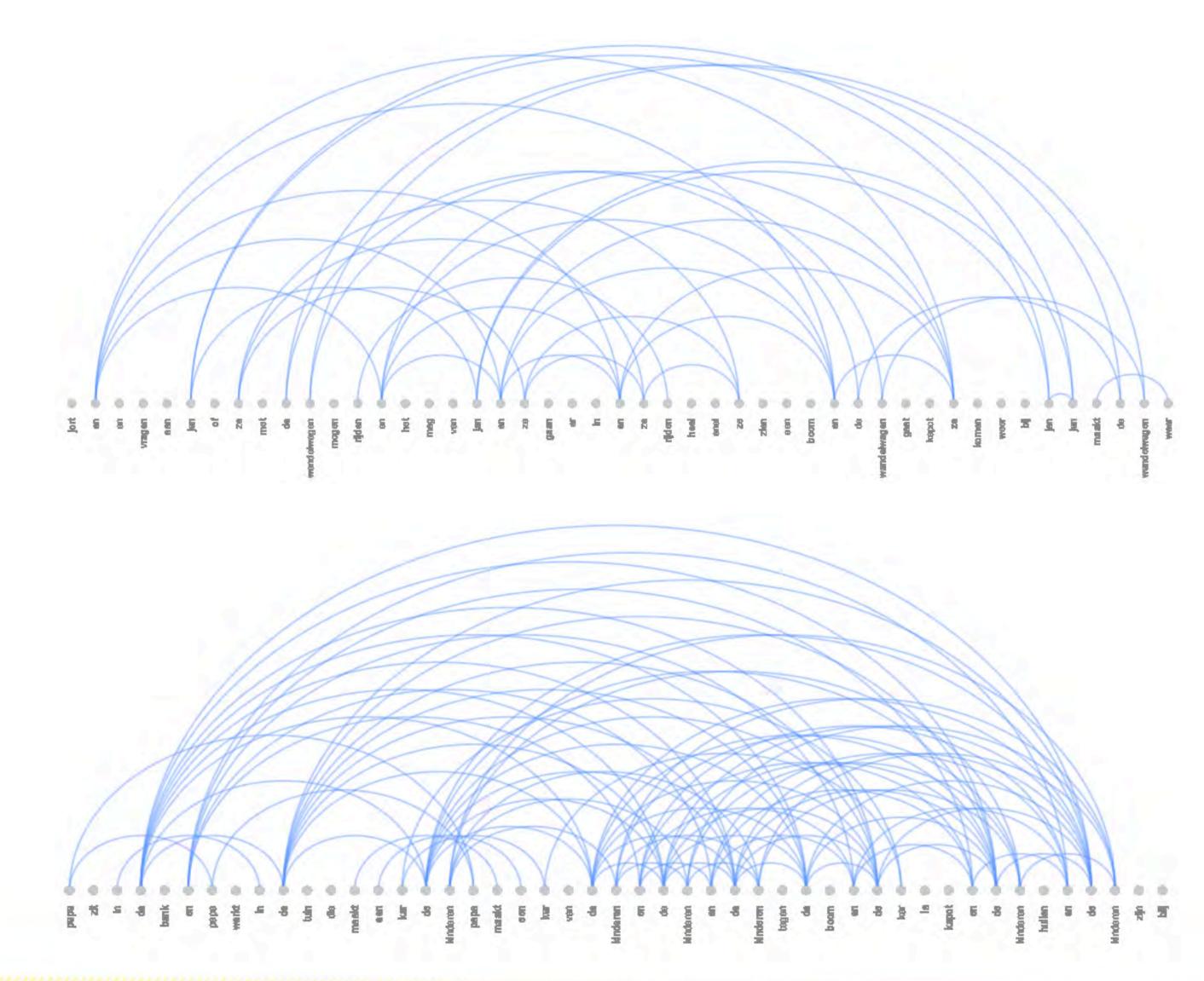
## **Recurrence Network**

**Total Degree = 70** 

verhaal 1

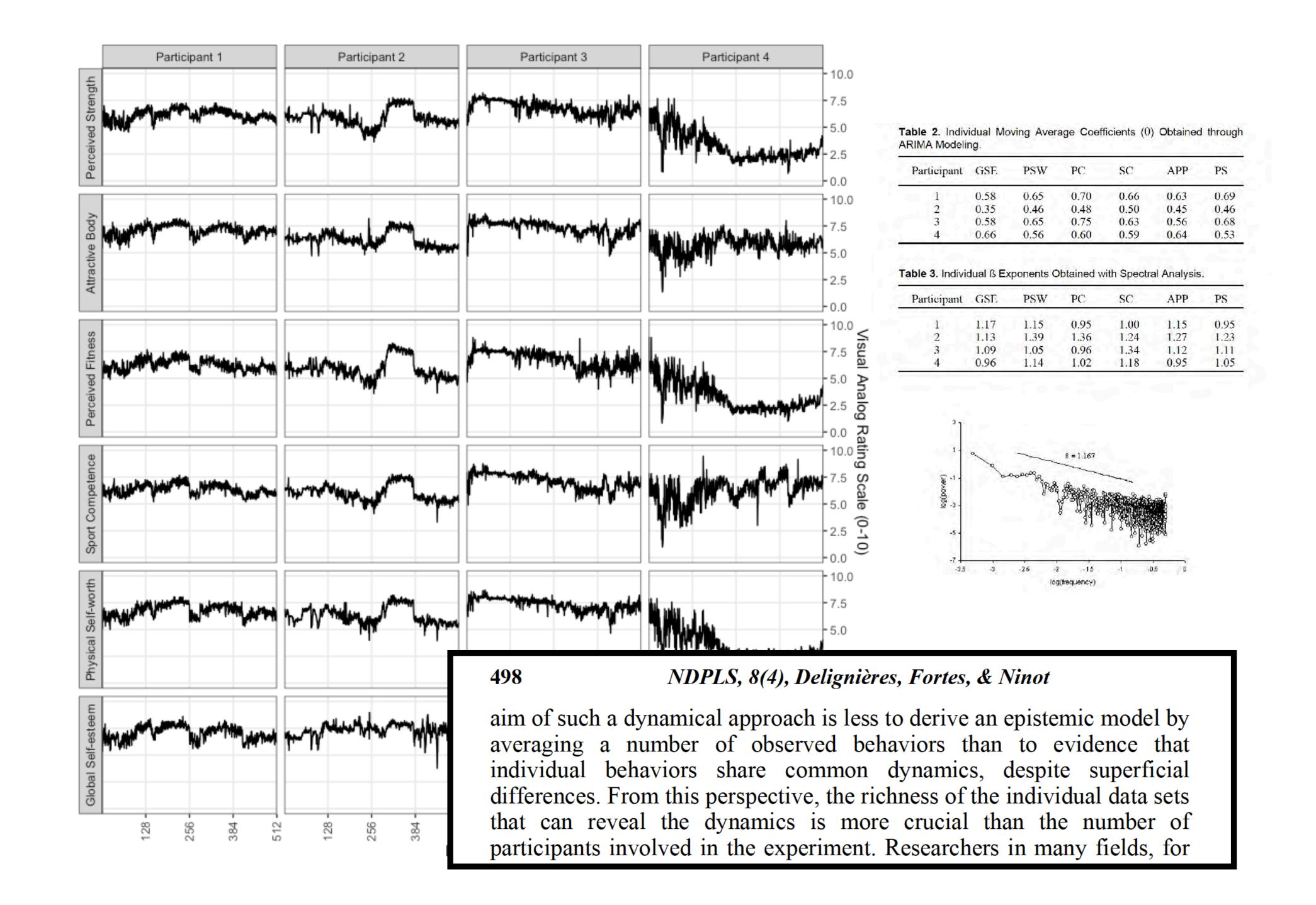


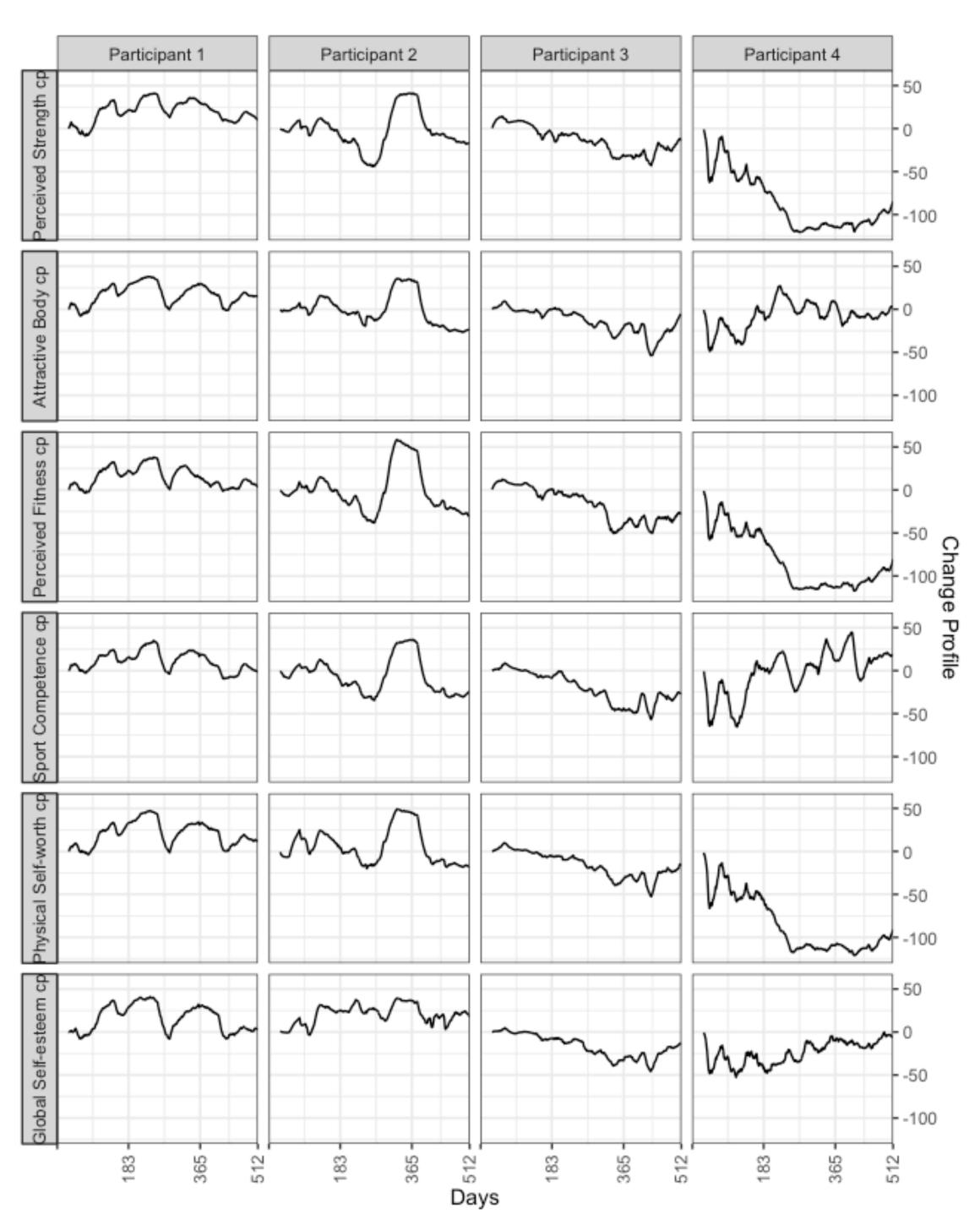
verhaal 2



# Ecological Momentary Assessment

- Measurement is considered to be like classical physical measurement:
  - ➡It is very problematic to interpret measurement outcomes as properties of the theoretical object of measurement (interaction between instrument and object, by merely asking to rate "I feel happy today")
  - → Measurement invariance, monotonicity, etc. do not hold



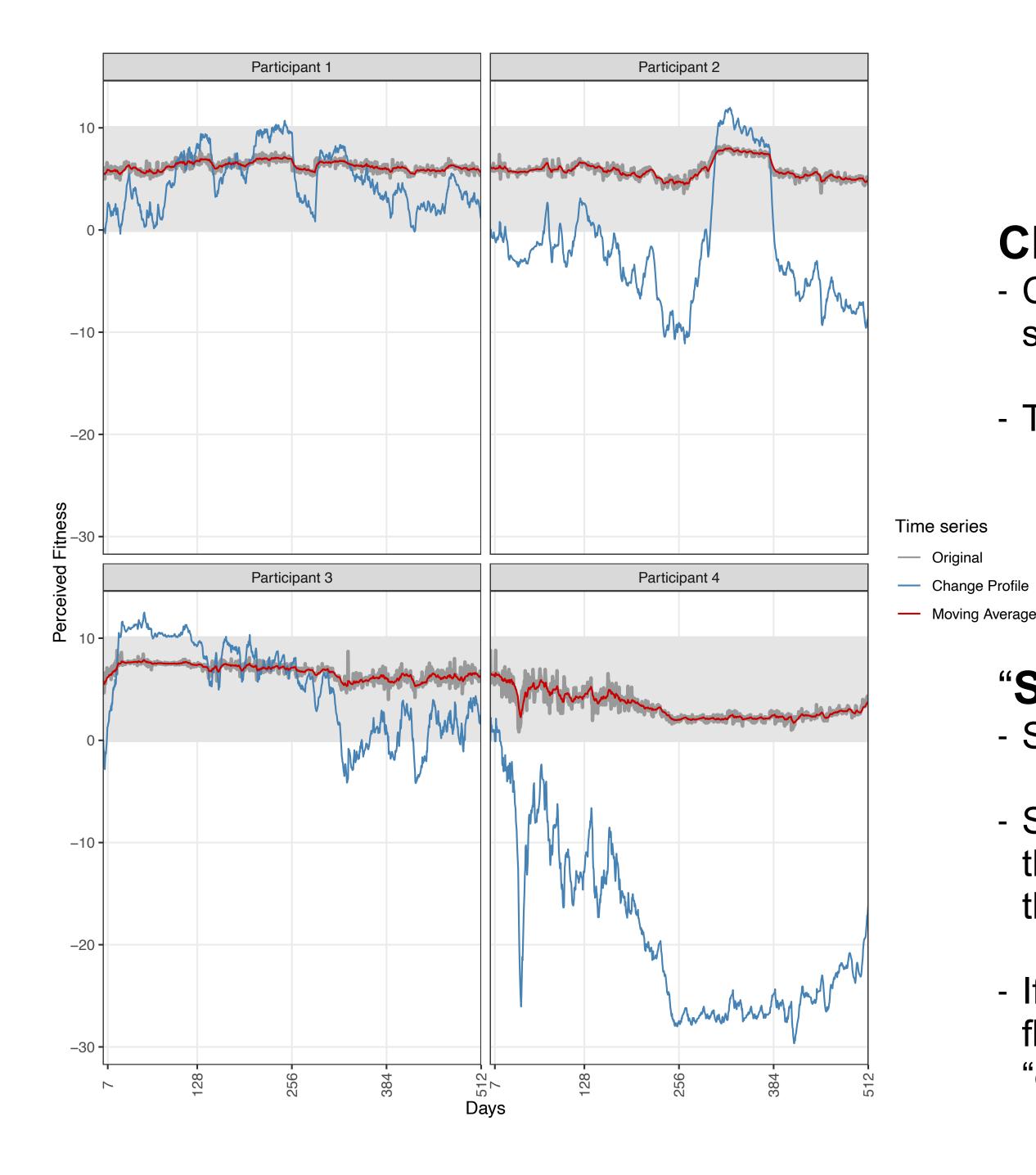


## **Change Profiles:**

- Center on a moving average in a sliding window
- Take the cumulative sum

### "Solves" some concerns:

- Scale is irrelevant/relative
- Small fluctuations are added in the cum. sum but, don't impact the shape of the overall profile
- If present, persistent levels & fluctuation patterns can be "exaggerated" (see y-scale)



## **Change Profiles:**

- Center on a moving average in a sliding window
- Take the cumulative sum

#### "Solves" some concerns:

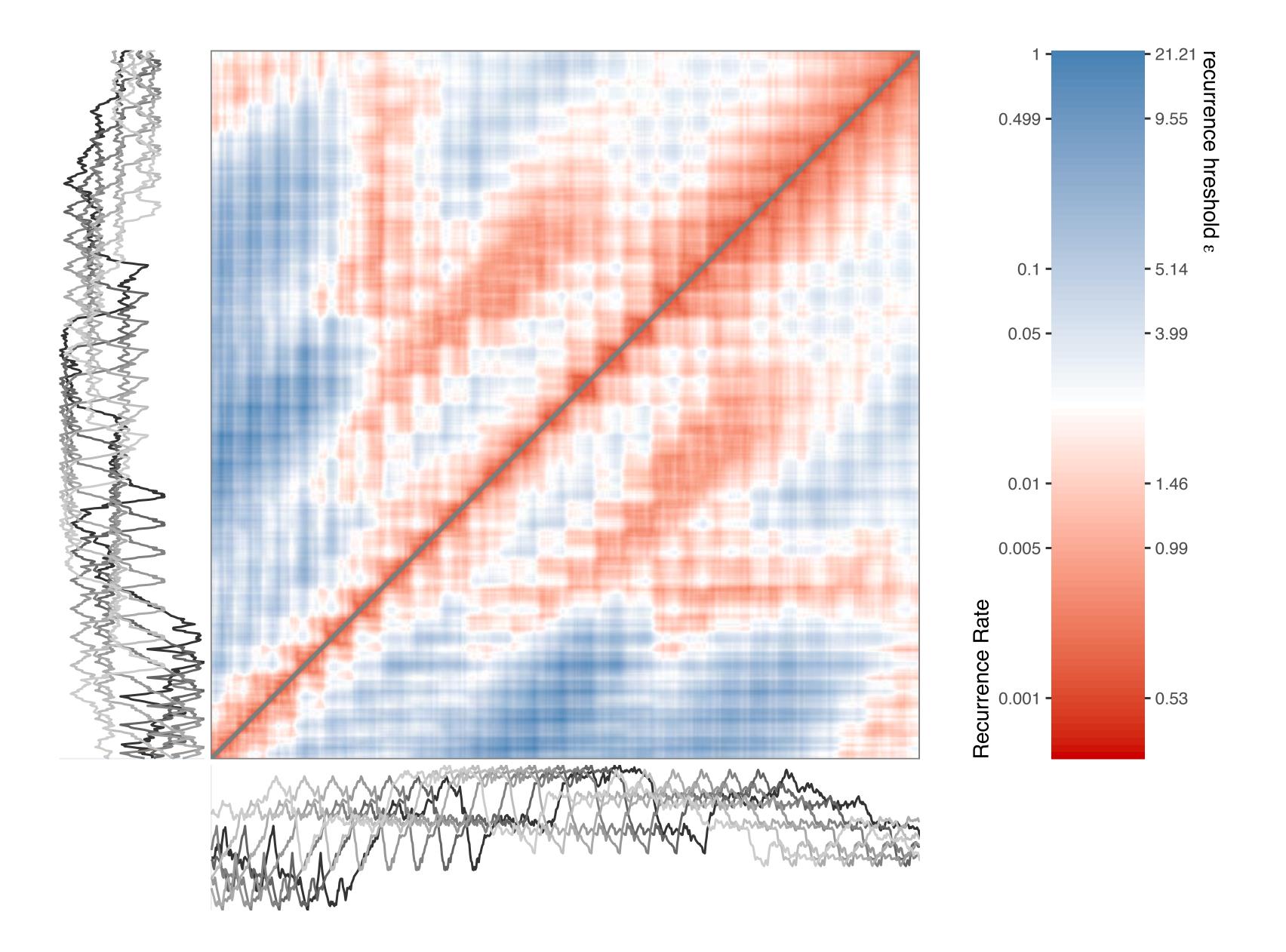
- Scale is irrelevant/relative
- Small fluctuations are added in the cum. sum but, don't impact the shape of the overall profile
- If present, persistent levels & fluctuation patterns can be "exaggerated" (see y-scale)

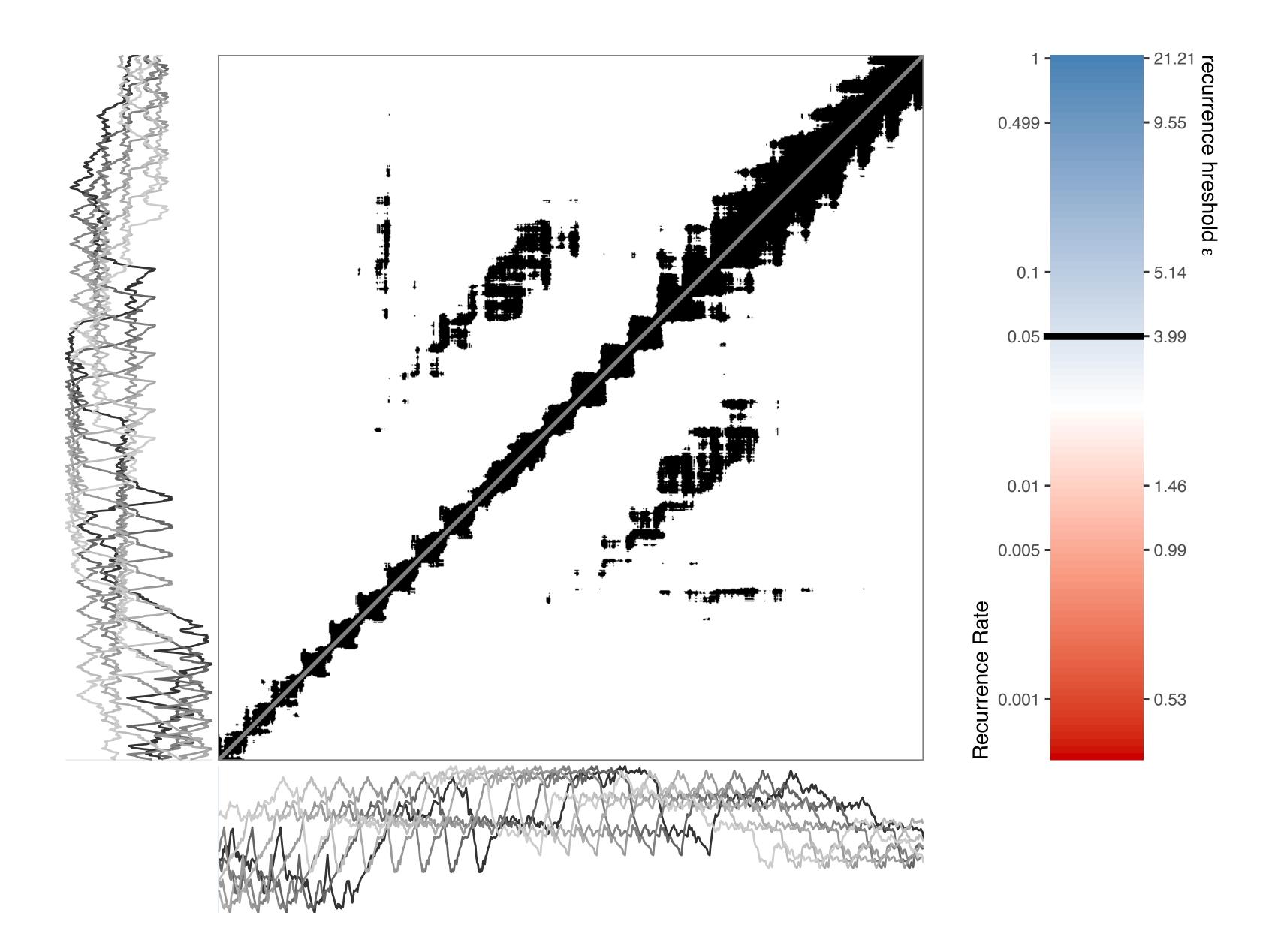
## Recurrence Based Approach

## **Quantifying State Dynamics**

- Essentially "model free"
- Few data assumptions
- Can detect and quantify nonstationarity, etc
- Recurrence Networks can deal with multivariate time series data

## Distance Matrix >> Recurrence Matrix







#### Contents lists available at ScienceDirect

#### Physics Reports





## Complex network approaches to nonlinear time series analysis



Yong Zou<sup>a,\*</sup>, Reik V. Donner<sup>b,c,\*\*</sup>, Norbert Marwan<sup>c</sup>, Jonathan F. Donges<sup>c,d</sup>, Jürgen Kurths<sup>c,e,f</sup>

- <sup>a</sup> Department of Physics, East China Normal University, Shanghai 200062, China
- <sup>b</sup> Department of Water, Environment, Construction and Safety, Magdeburg–Stendal University of Applied Sciences, Breitscheidstraße 2, 39114 Magdeburg, Germany
- <sup>c</sup> Potsdam Institute for Climate Impact Research (PIK) Member of the Leibniz Association, Telegrafenberg A31, 14473 Potsdam. Germany
- d Stockholm Resilience Centre, Stockholm University, Kräftriket 2B, 114 19 Stockholm, Sweden
- <sup>e</sup> Saratov State University, 4410012 Saratov, Russia
- <sup>1</sup> Department of Physics, Humboldt University Berlin, Newtonstraße 15, 12489 Berlin, Germany

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#### Article history: Accepted 22 October 2018 Available online 2 November 2018 Editor: I. Procaccia

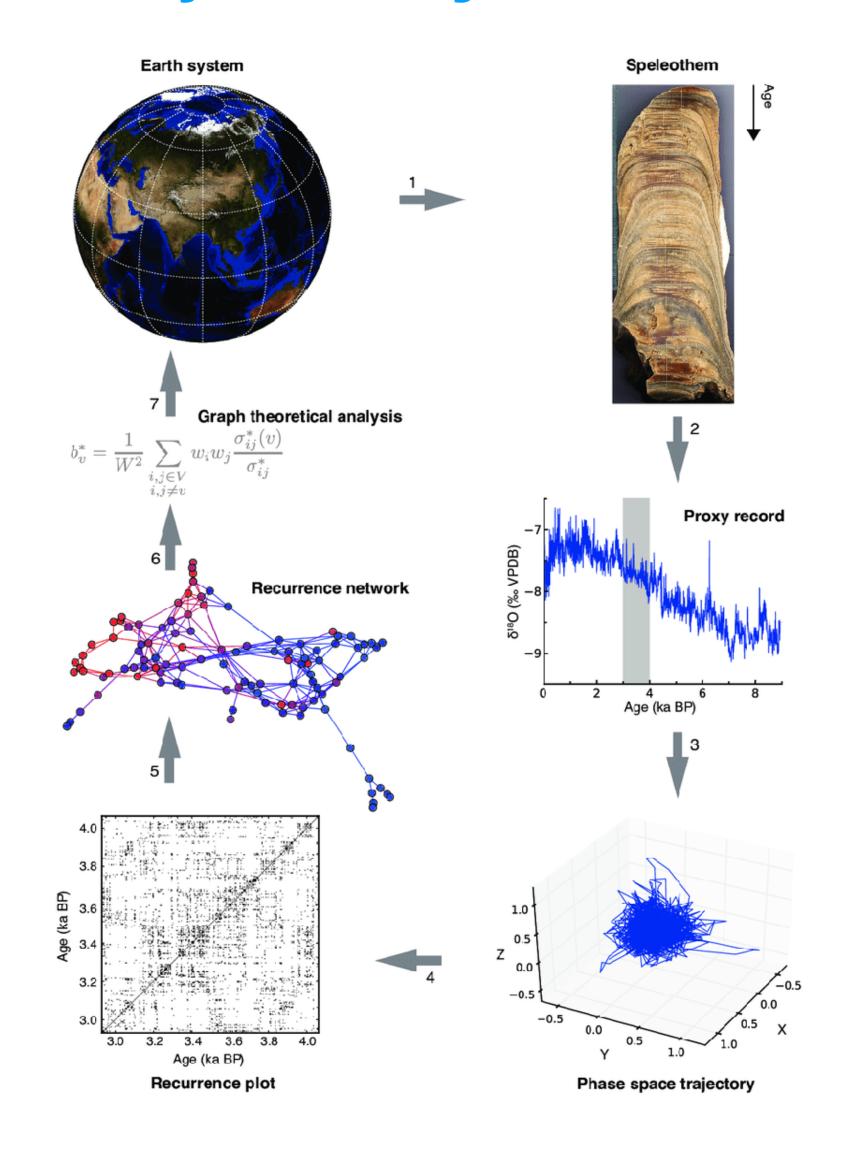
Keywords: Complex networks Nonlinear dynamics Recurrences Visibility Transition networks

#### ABSTRACT

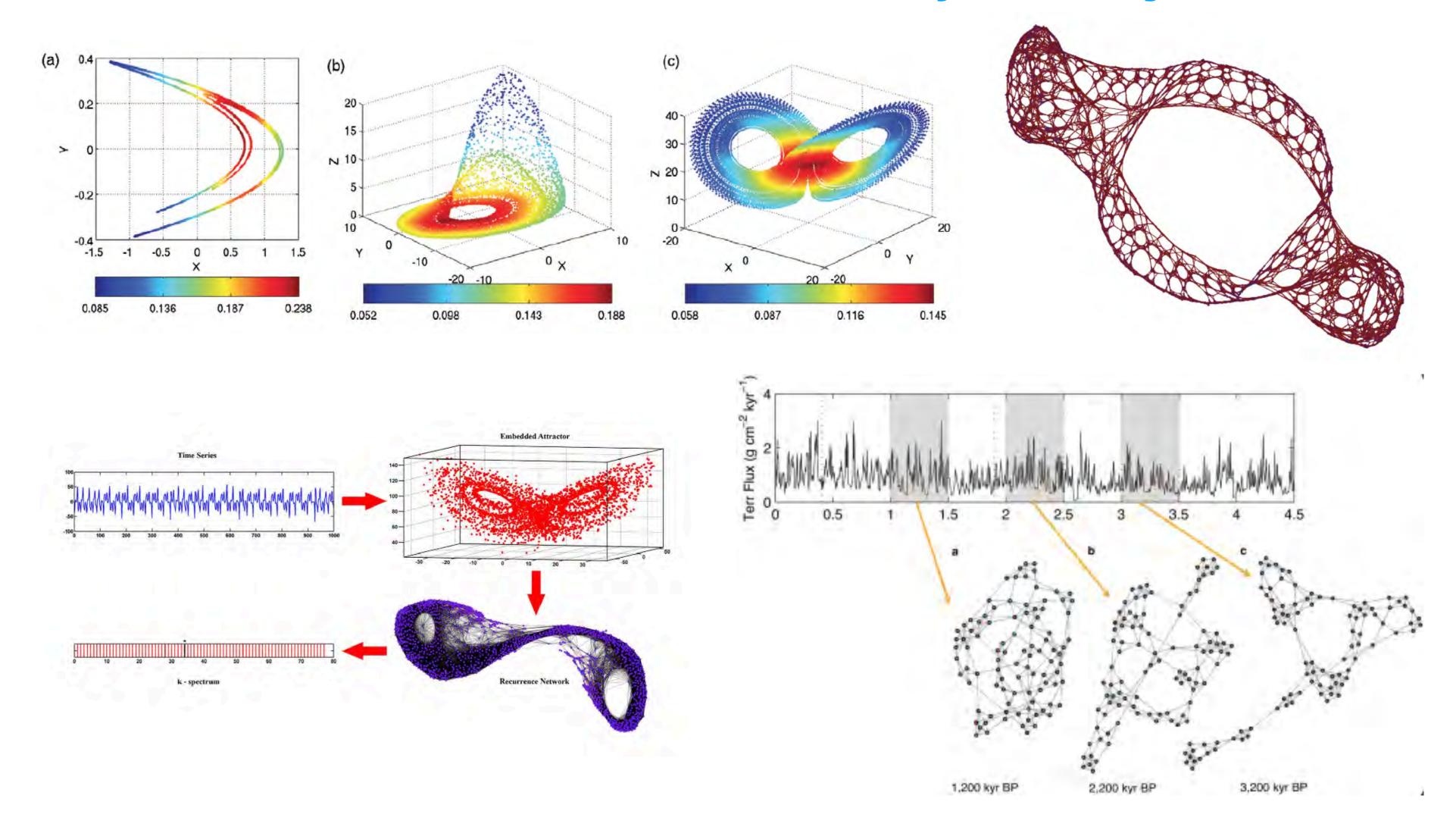
In the last decade, there has been a growing body of literature addressing the utilization of complex network methods for the characterization of dynamical systems based on time series. While both nonlinear time series analysis and complex network theory are widely considered to be established fields of complex systems sciences with strong links to nonlinear dynamics and statistical physics, the thorough combination of both approaches has become an active field of nonlinear time series analysis, which has allowed addressing fundamental questions regarding the structural organization of nonlinear dynamics as well as the successful treatment of a variety of applications from a broad range of disciplines. In this report, we provide an in-depth review of existing approaches of time series networks, covering their methodological foundations, interpretation and practical considerations with an emphasis on recent developments. After a brief outline of the state-of-the-art of nonlinear time series analysis and the theory of complex networks, we focus on three main network approaches, namely, phase space based recurrence networks, visibility graphs and Markov chain based transition networks, all of which have made their way from abstract concepts to widely used methodologies. These three concepts, as well as several variants thereof will be discussed in great detail regarding their specific properties, potentials and limitations. More importantly, we emphasize which fundamental new insights complex network approaches bring into the field of nonlinear time series analysis. In addition, we summarize examples from the wide range of recent applications of these methods, covering rather diverse fields like climatology, fluid dynamics, neurophysiology, engineering and economics, and demonstrating the great potentials of time series networks for tackling real-world contemporary scientific problems. The overall aim of this report is to provide the readers with the knowledge how the complex network approaches can be applied to their own field of real-world time series analysis.

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- Time points are nodes (vertices)
- Nodes are connected by lines (edges) if they recur at some later point in time
- Network measures can be interpreted as quantifying aspects of the temporal dynamics, some are equivalent to RQA measures... some are different (e.g. weighted and/or directed network measures)



Donges, J. F., Donner, R., Marwan, N., Breitenbach, S. F., Rehfeld, K., & Kurths, J. (2015). Non-linear regime shifts in Holocene Asian monsoon variability: potential impacts on cultural change and migratory patterns. *Climate of the Past*, 11(5), 709-741.

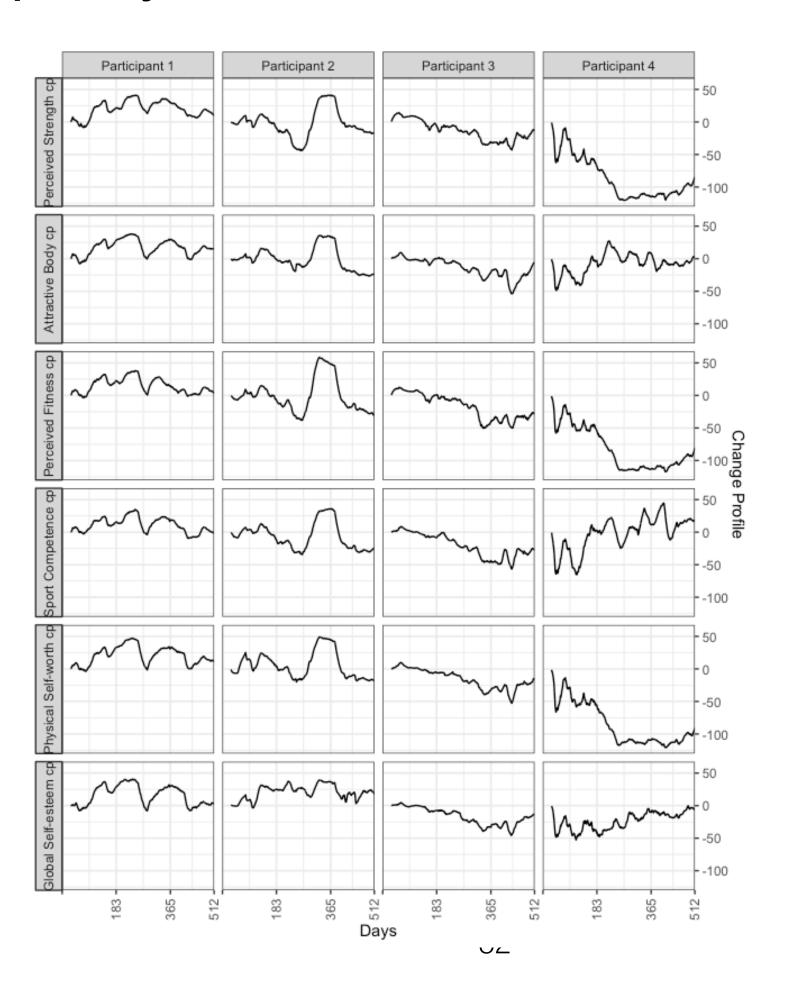


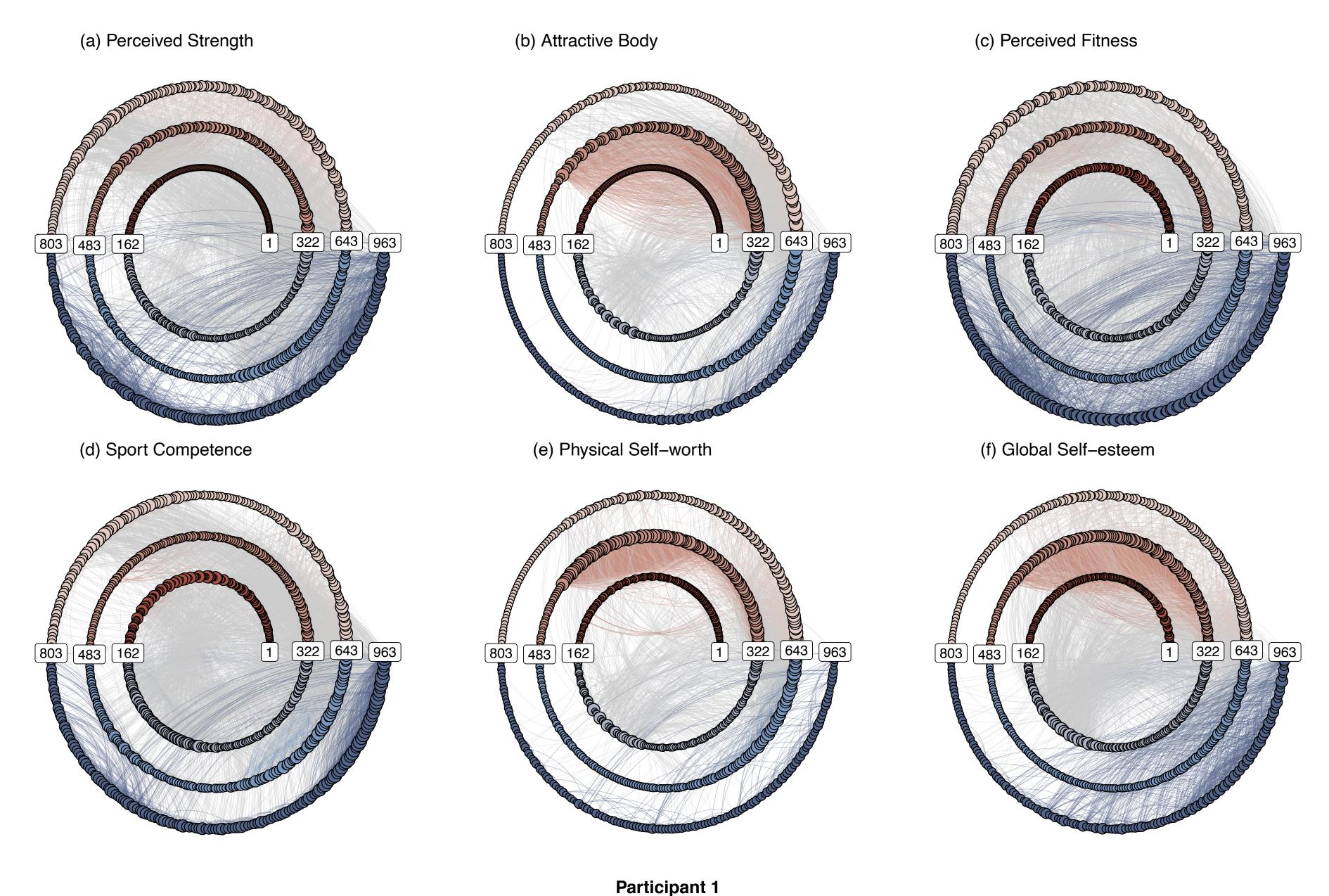
Small, M., Zhang, J., & Xu, X. (2009). Transforming time series into complex networks. Complex Sciences, 2078–2089.

Jacob, R., Harikrishnan, K. P., Misra, R., & Ambika, G. (2015). How does noise affect the structure of a chaotic attractor: A recurrence network perspective. arXiv preprint arXiv:1508.02724.

https://www.uu.nl/en/events/clue-training-7-pyunicorn-complex-network5and-recurrence-analysis-toolbox

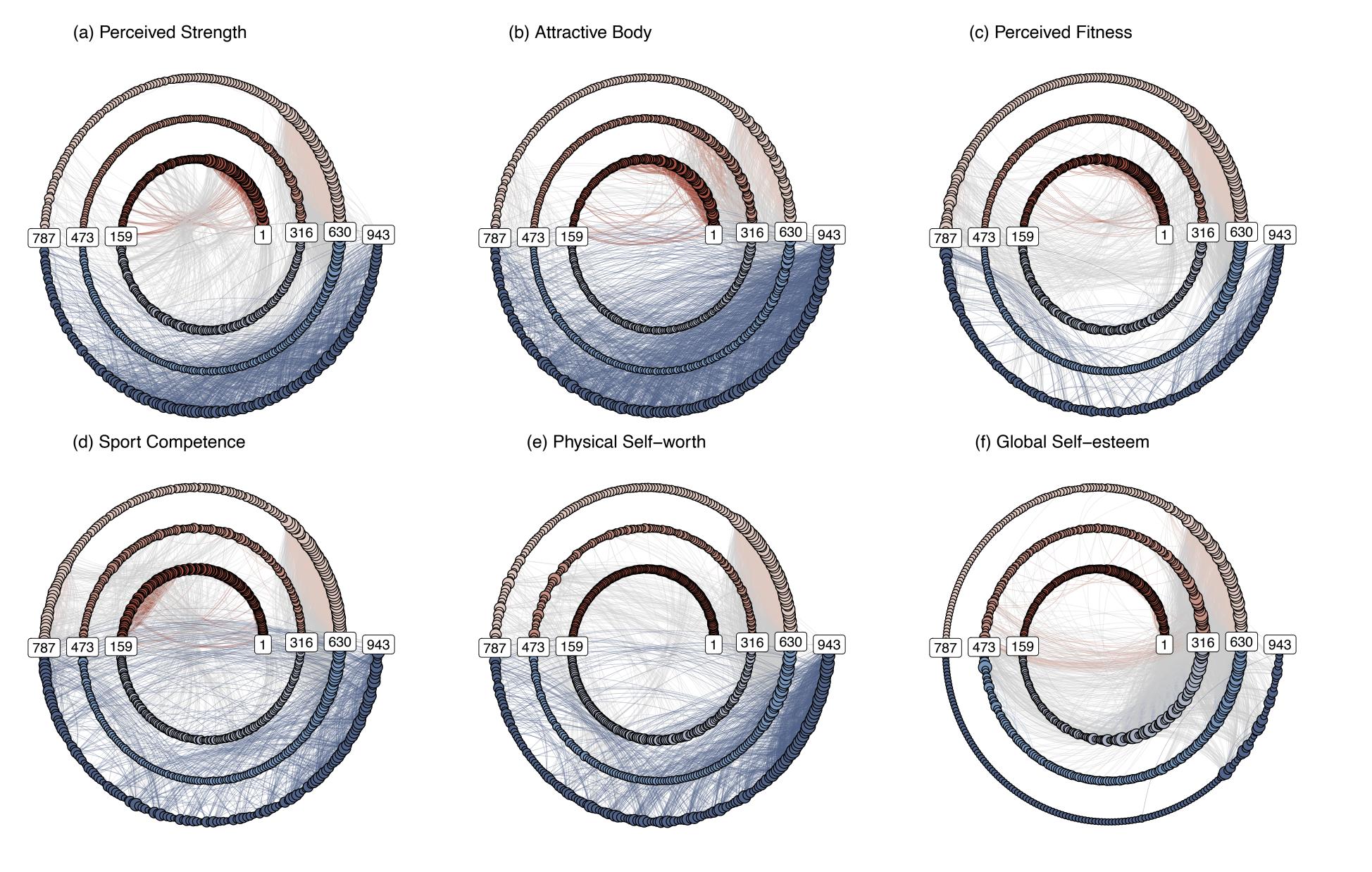
Find a graph layout that makes a bit more sense





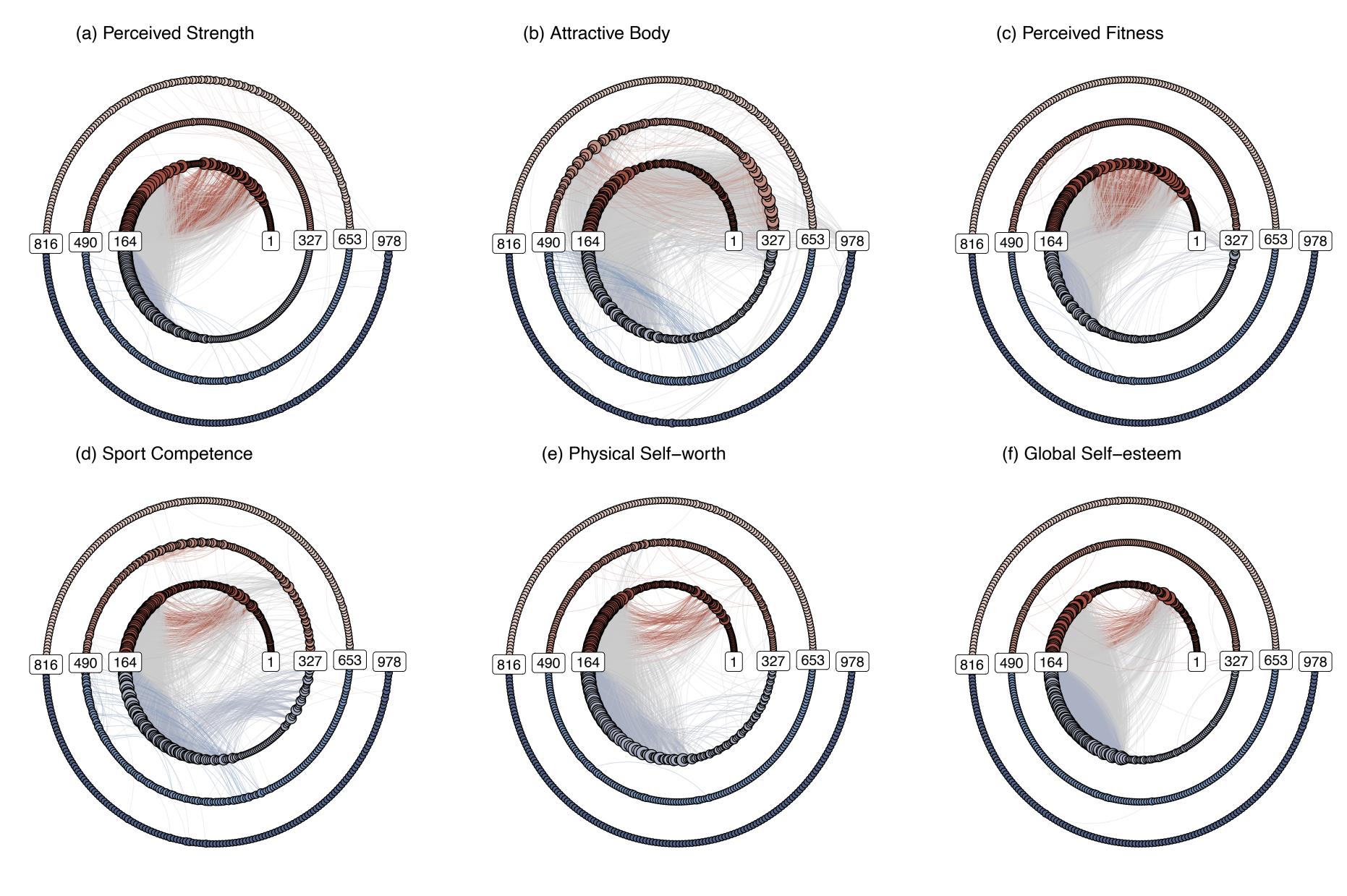
Participani

Hasselman, F. & Bosman, A.M.T. (submitted). Studying Complex Adaptive Systems with Internal States: A Recurrence-Based Analysis Strategy for Multivariate Time Series Data Representing Self-Reports of Human Experience. *Frontiers in Applied Mathematics and Statistics*.



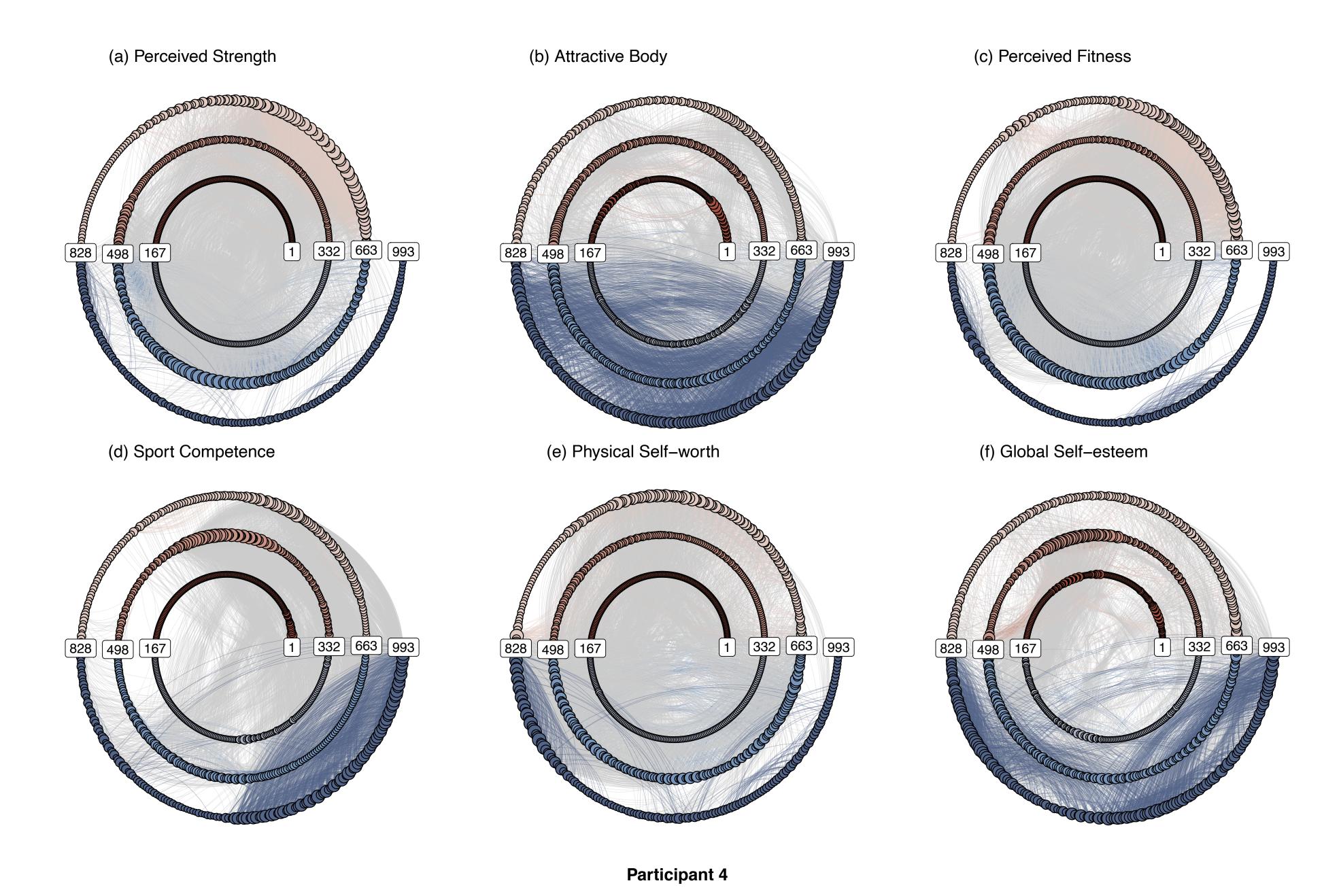
Participant 2

Hasselman, F. & Bosman, A.M.T. (submitted). Studying Complex Adaptive Systems with Internal States: A Recurrence-Based Analysis Strategy for Multivariate Time Series Data Representing Self-Reports of Human Experience. *Frontiers in Applied Mathematics and Statistics*.

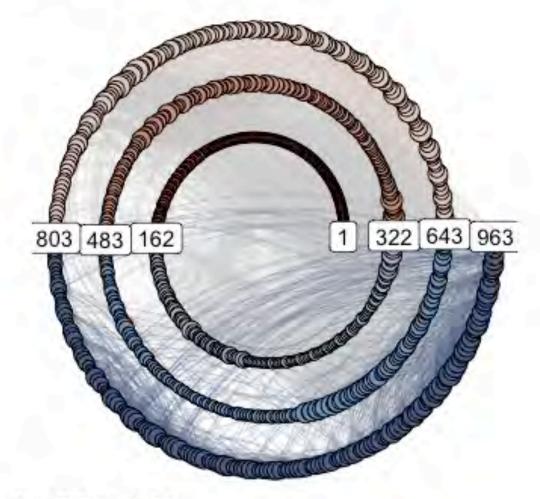


Participant 3

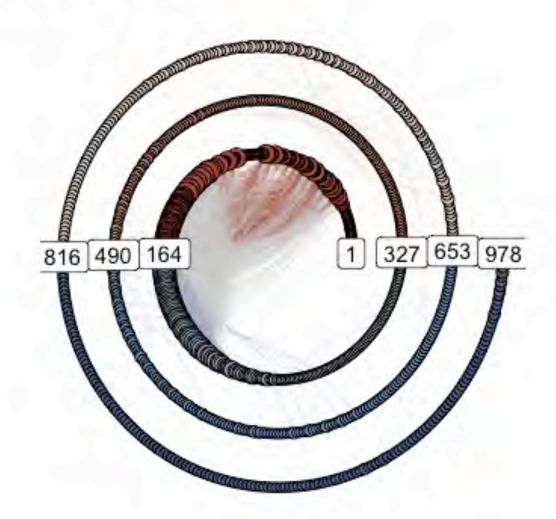
Hasselman, F. & Bosman, A.M.T. (submitted). Studying Complex Adaptive Systems with Internal States: A Recurrence-Based Analysis Strategy for Multivariate Time Series Data Representing Self-Reports of Human Experience. *Frontiers in Applied Mathematics and Statistics*.



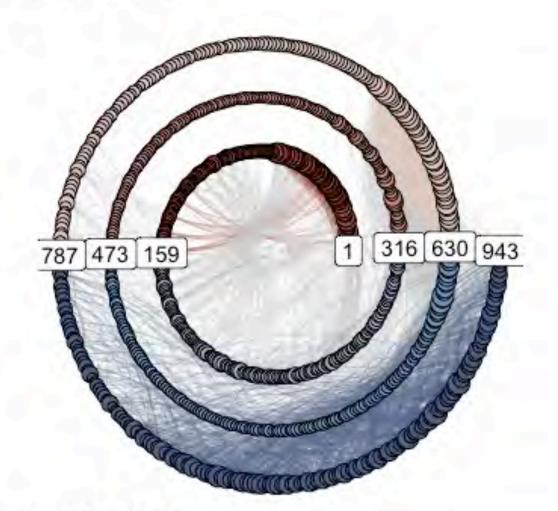
Hasselman, F. & Bosman, A.M.T. (submitted). Studying Complex Adaptive Systems with Internal States: A Recurrence-Based Analysis Strategy for Multivariate Time Series Data Representing Self-Reports of Human Experience. *Frontiers in Applied Mathematics and Statistics*.



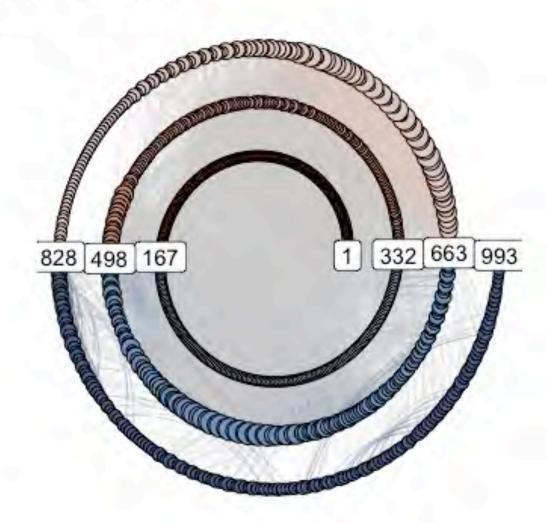
Participant 3 - FD = 1.18



Participant 2 - FD = 1.16



Participant 4 - FD = 1.19



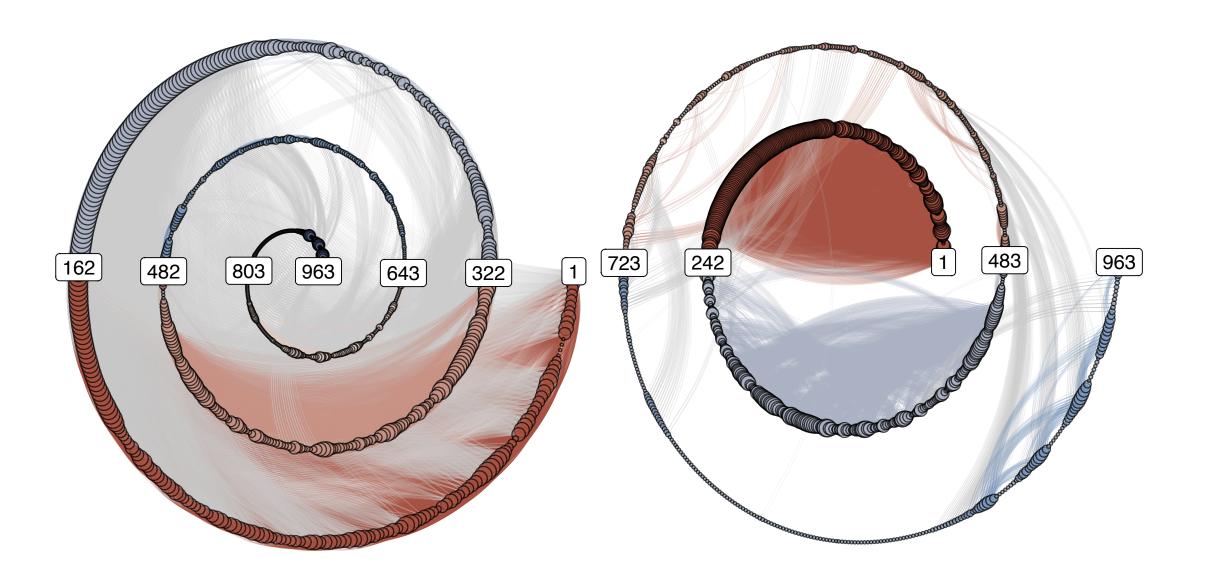
**Perceived Strength** 

Hasselman, F. & Bosman, A.M.T. (submitted). Studying Complex Adaptive Systems with Internal States: A Recurrence-Based Analysis Strategy for Multivariate Time Series Data Representing Self-Reports of Human Experience. *Frontiers in Applied Mathematics and Statistics*.



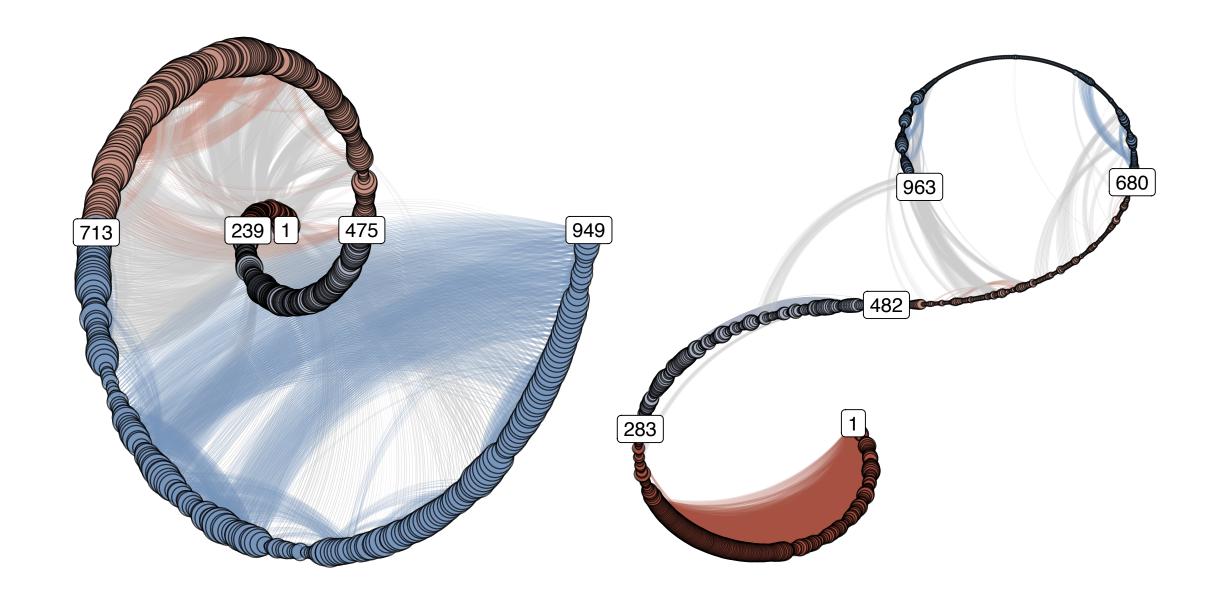
Bernoulli spiral

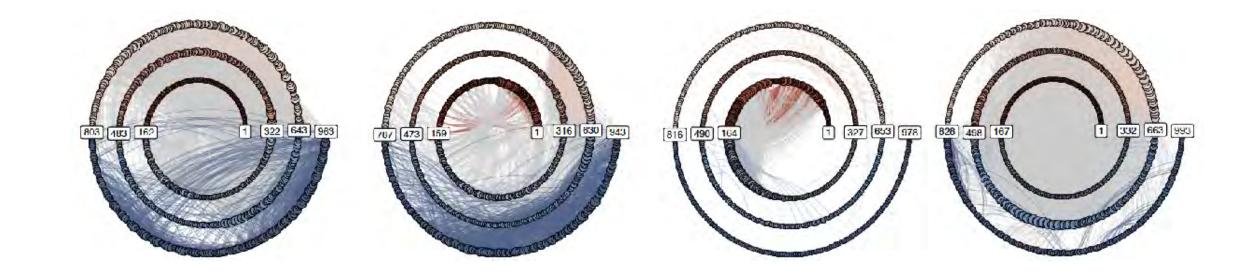
Participant 3
Global Self-Esteem



Fermat spiral

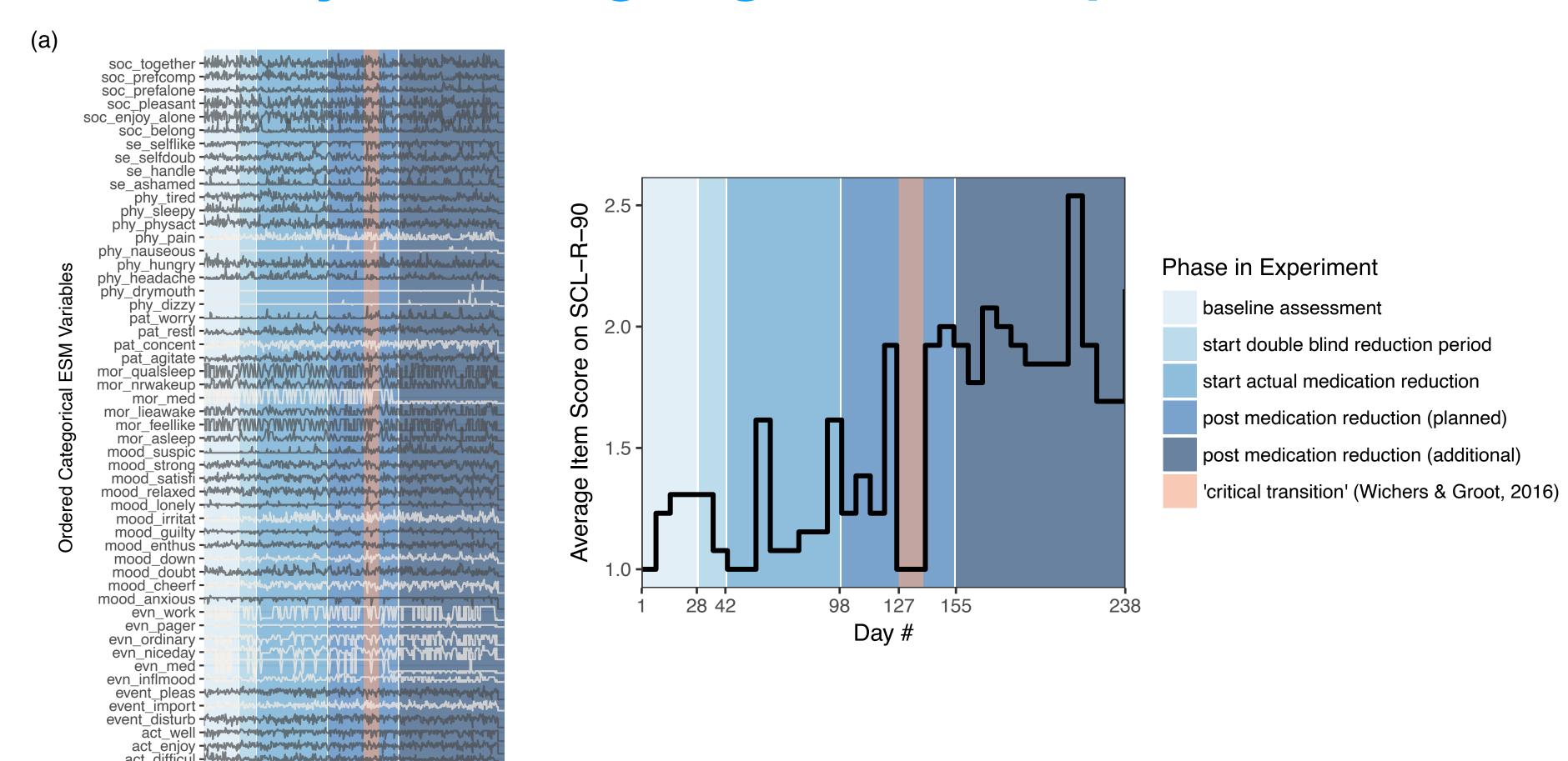
**Euler spiral** 





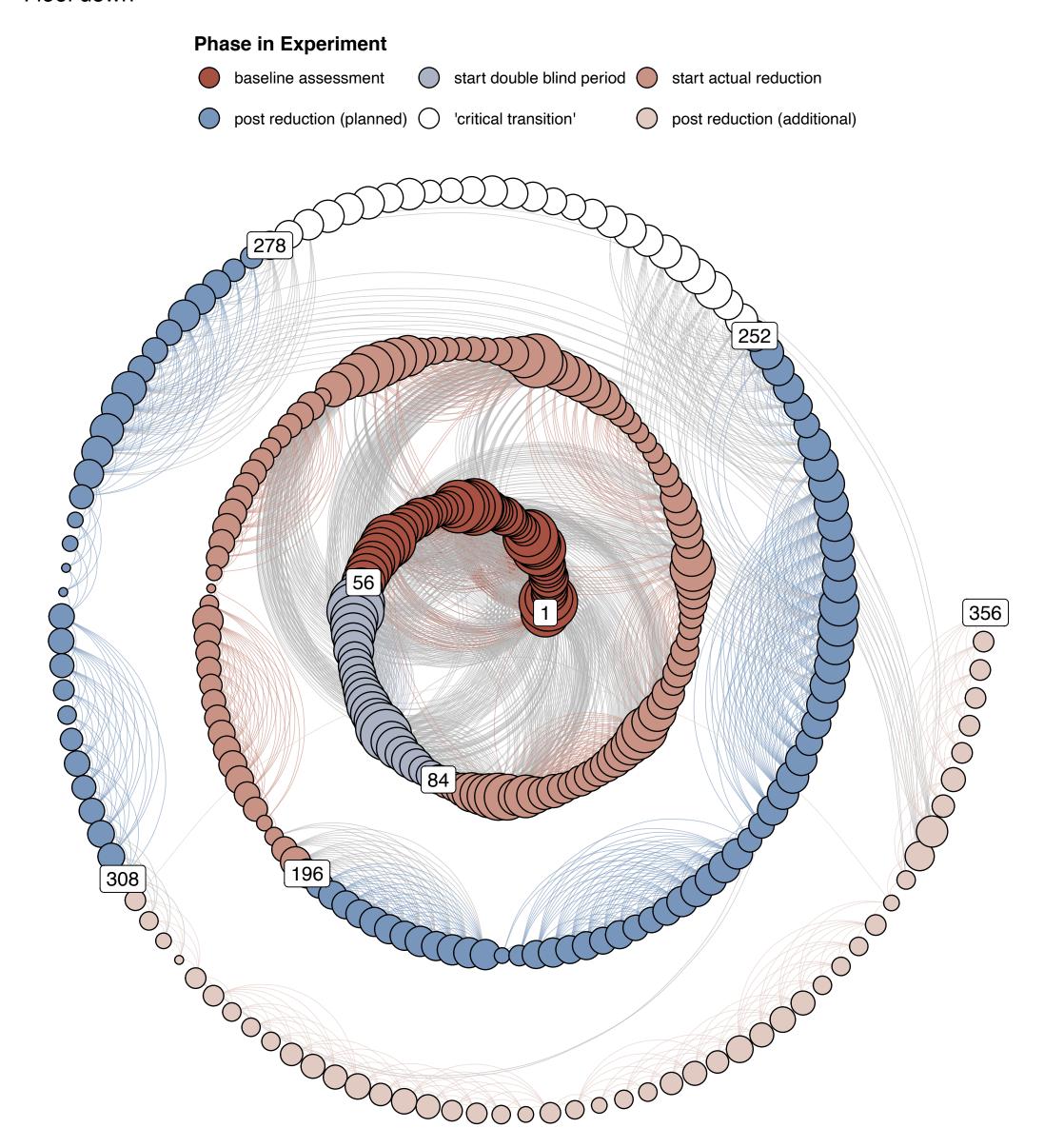
Perceived Strength	P1	P2	P3	P4
Centralization Degree	0.056	0.068	0.093	0.091
Centralization Betweenness	0.036	0.028	0.002	0.076
<b>Centralization Closeness</b>	0.002	0.001	0	0.001
Transitivity	0.387	0.528	0.783	0.51
<b>Assortativity Degree</b>	0.332	0.436	0.479	0.361
average Path Length	4.98	4.69	2.41	6.82
SWI	28.50	36.48	112.61	27.87
Diameter	12	36	9	22
Fractal Dimension	1.21	1.16	1.18	1.19

## "Critical Slowing Down as a Personalized Early Warning Signal for Depression"

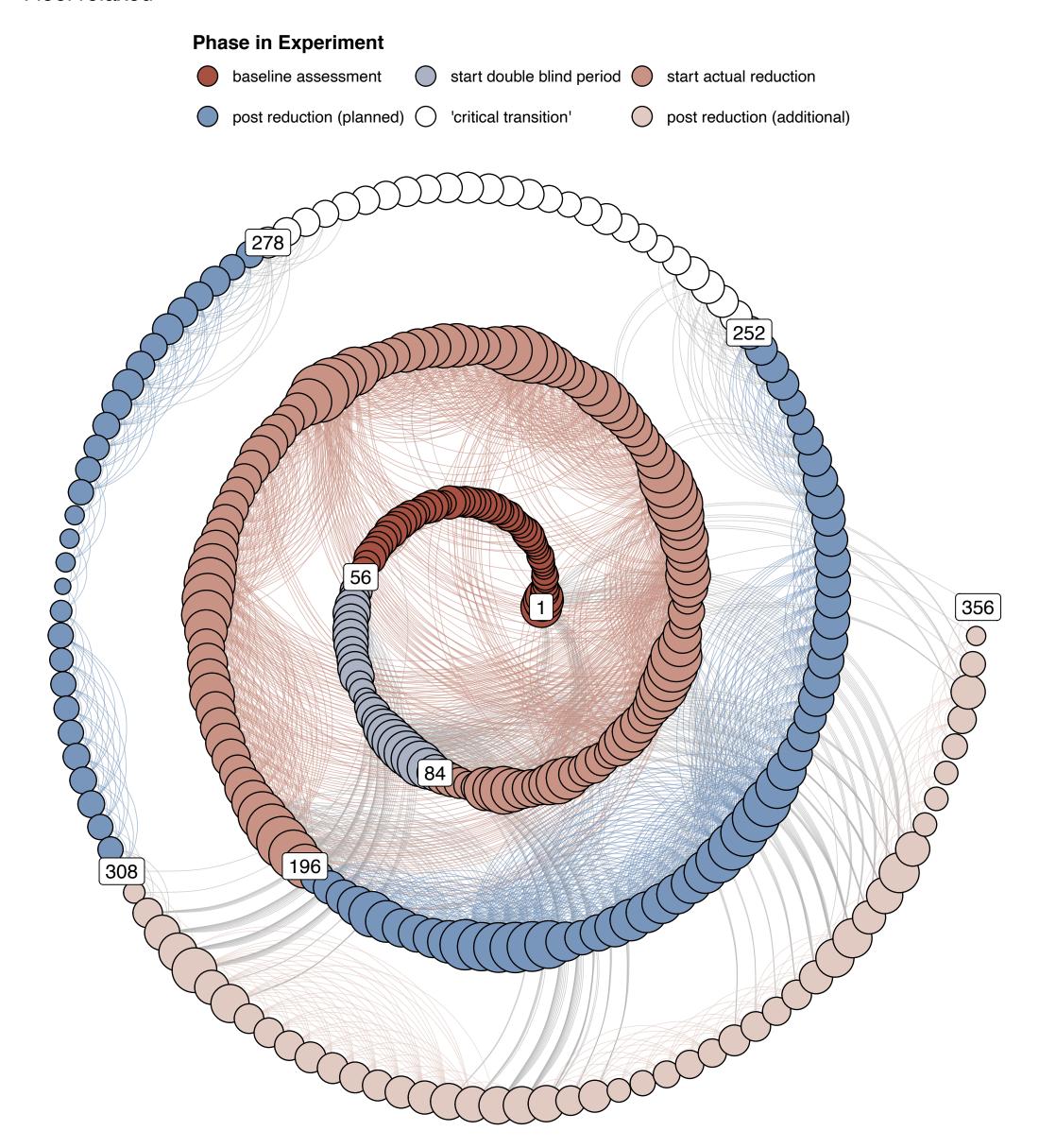


Wichers, M., Groot, P. C., Psychosystems, ESM Grp, & EWS Grp (2016). Critical Slowing Down as a Personalized Early Warning Signal for Depression. Psychotherapy and psychosomatics, 85(2), 114-116. DOI: 10.1159/000441458

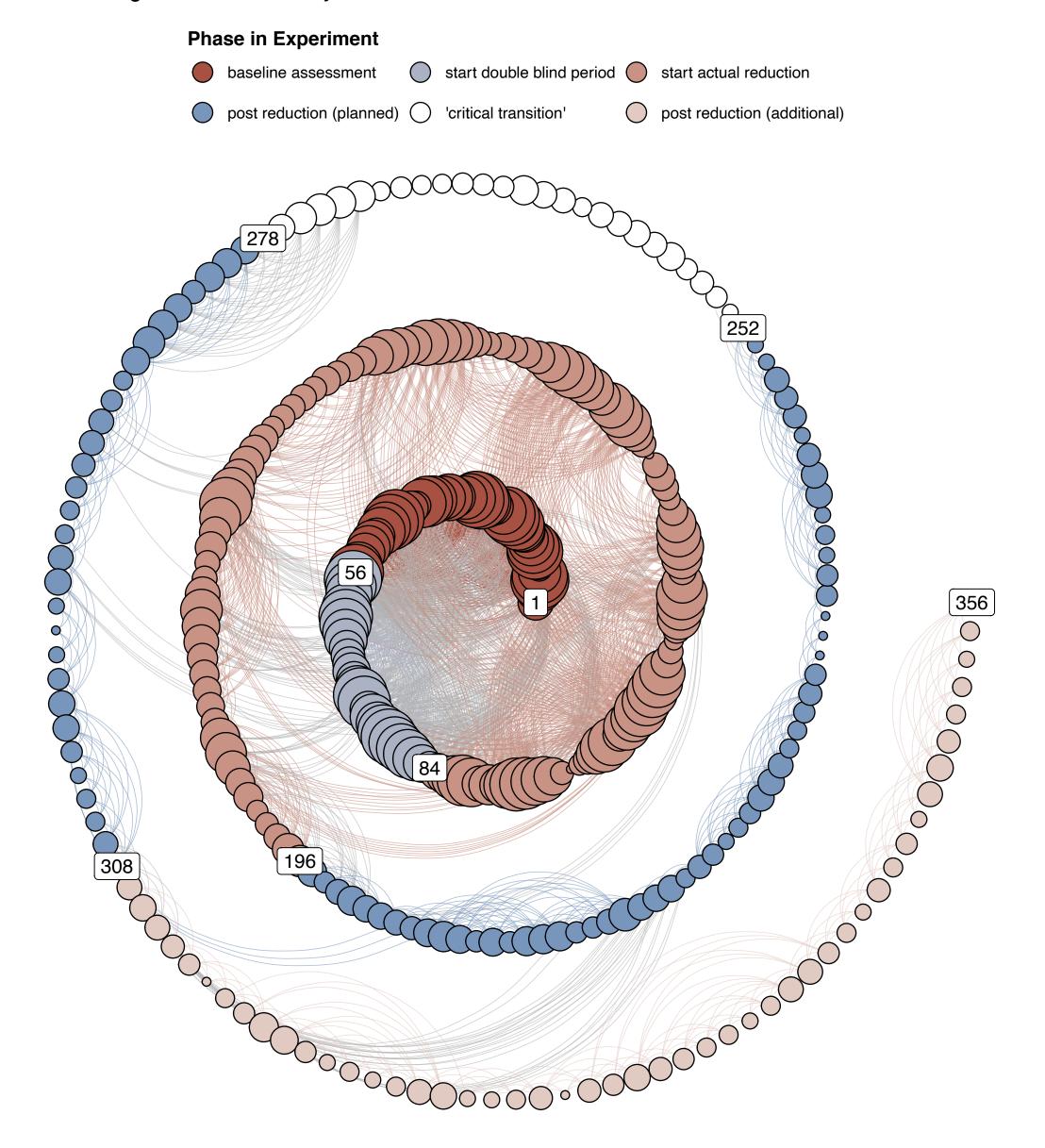
#### "I feel down"



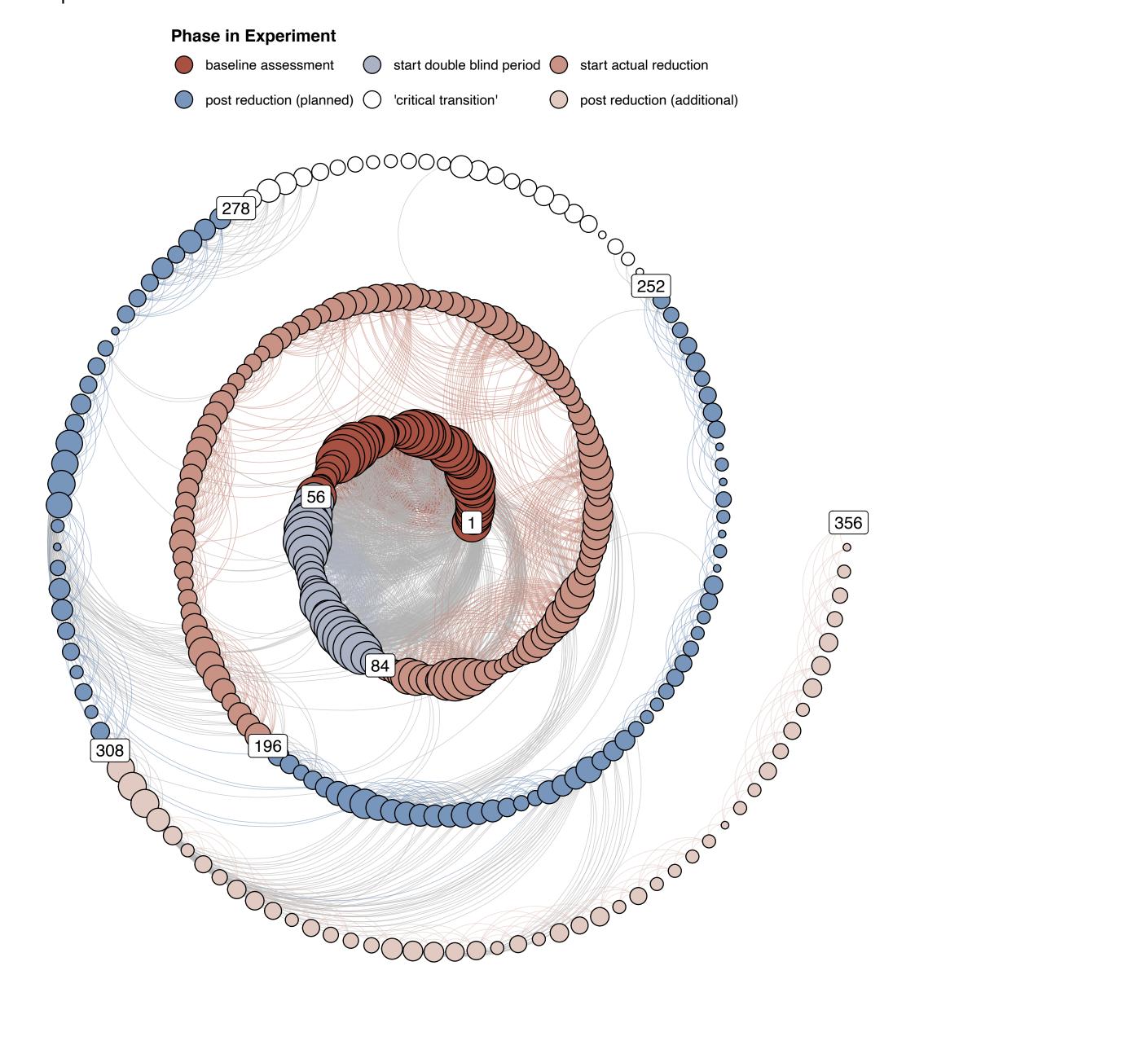
#### "I feel relaxed"



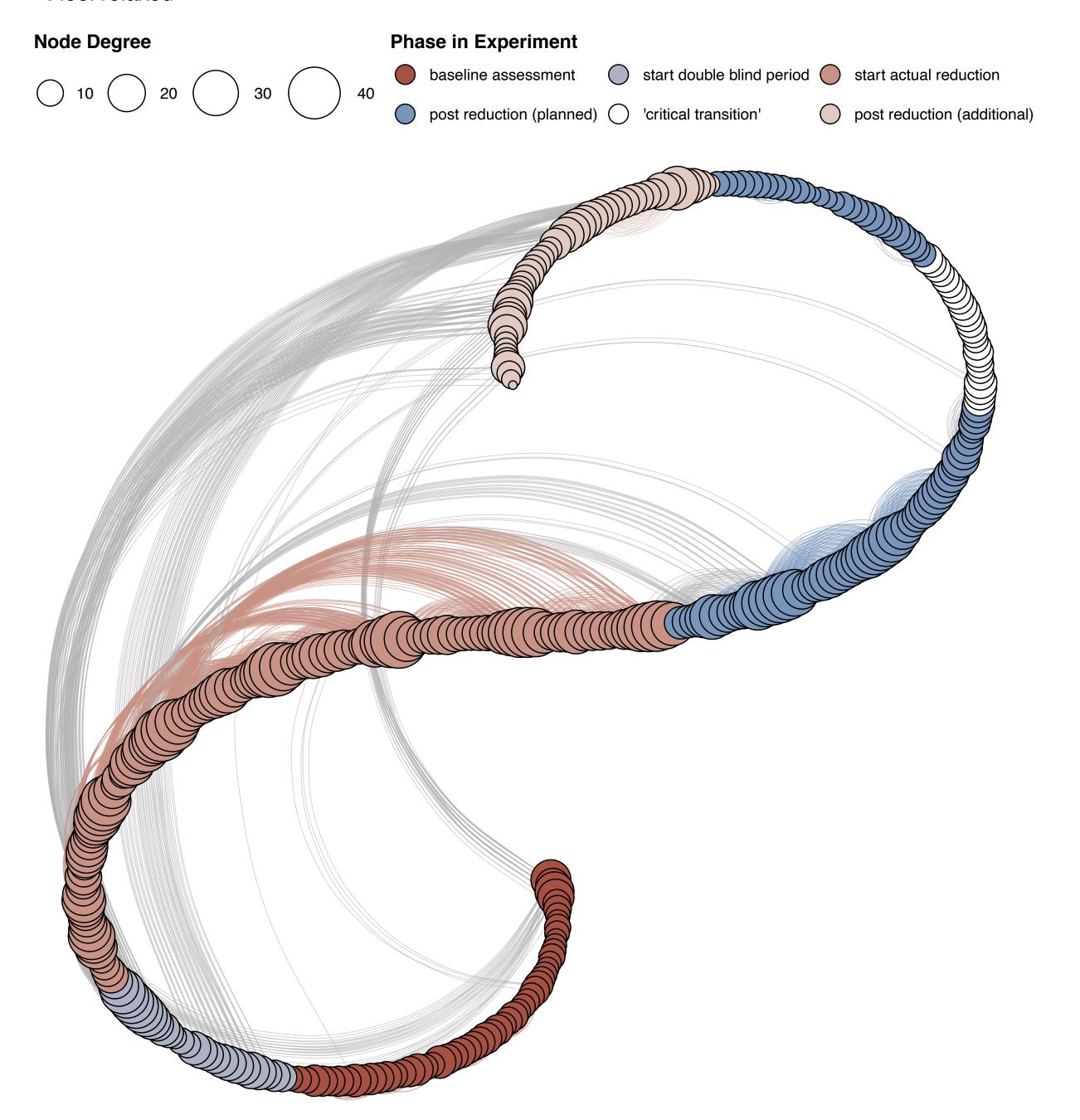
#### "I am looking forward to this day"



"I slept well"



"I feel relaxed"



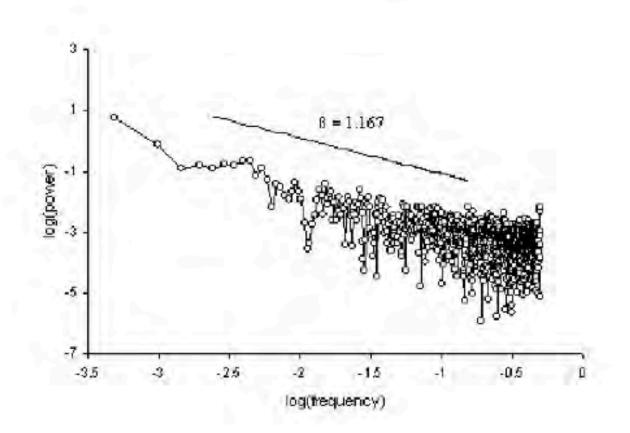
## Scaling of Network Strength vs. Scaling in Timeseries

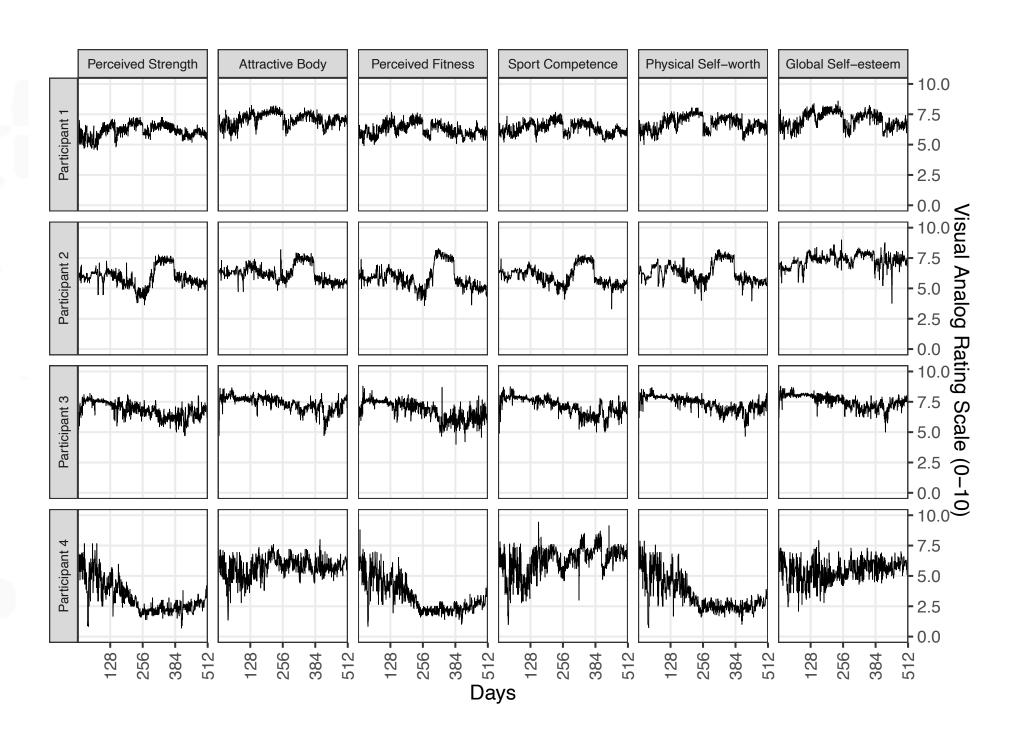
**Table 2.** Individual Moving Average Coefficients (0) Obtained through ARIMA Modeling.

Participant	GSE	PSW	PC	SC	APP	PS
1	0.58	0.65	0.70	0.66	0.63	0.69
2	0.35	0.46	0.48	0.50	0.45	0.46
3	0.58	0.65	0.75	0.63	0.56	0.68
4	0.66	0.56	0.60	0.59	0.64	0.53

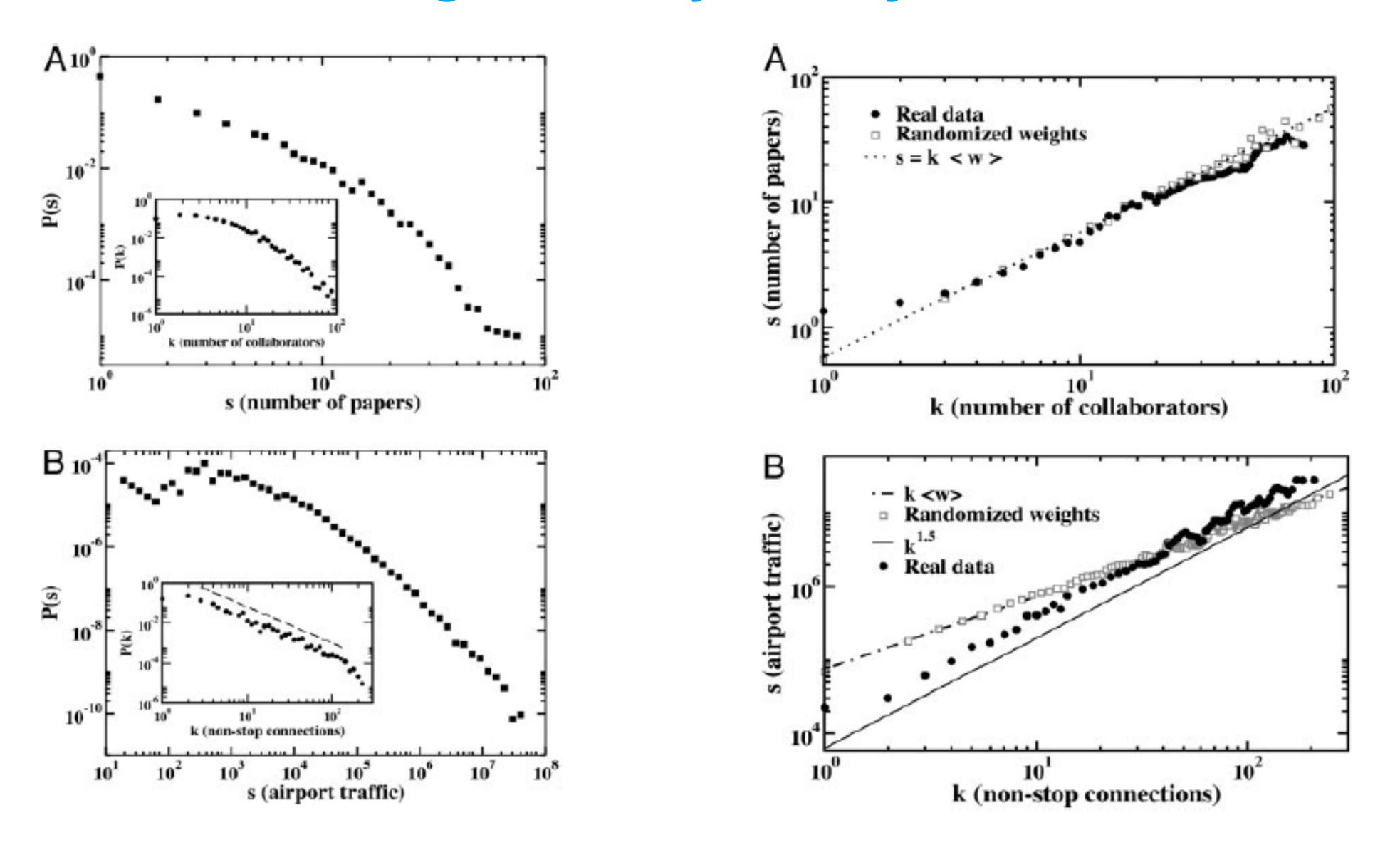
Table 3. Individual ß Exponents Obtained with Spectral Analysis.

Participant	GSE	PSW	PC	SC	APP	PS
1	1.17	1.15	0.95	1.00	1.15	0.95
2	1.13	1.39	1.36	1.24	1.27	1.23
3	1.09	1.05	0.96	1.34	1.12	1.11
4	0.96	1.14	1.02	1.18	0.95	1.05

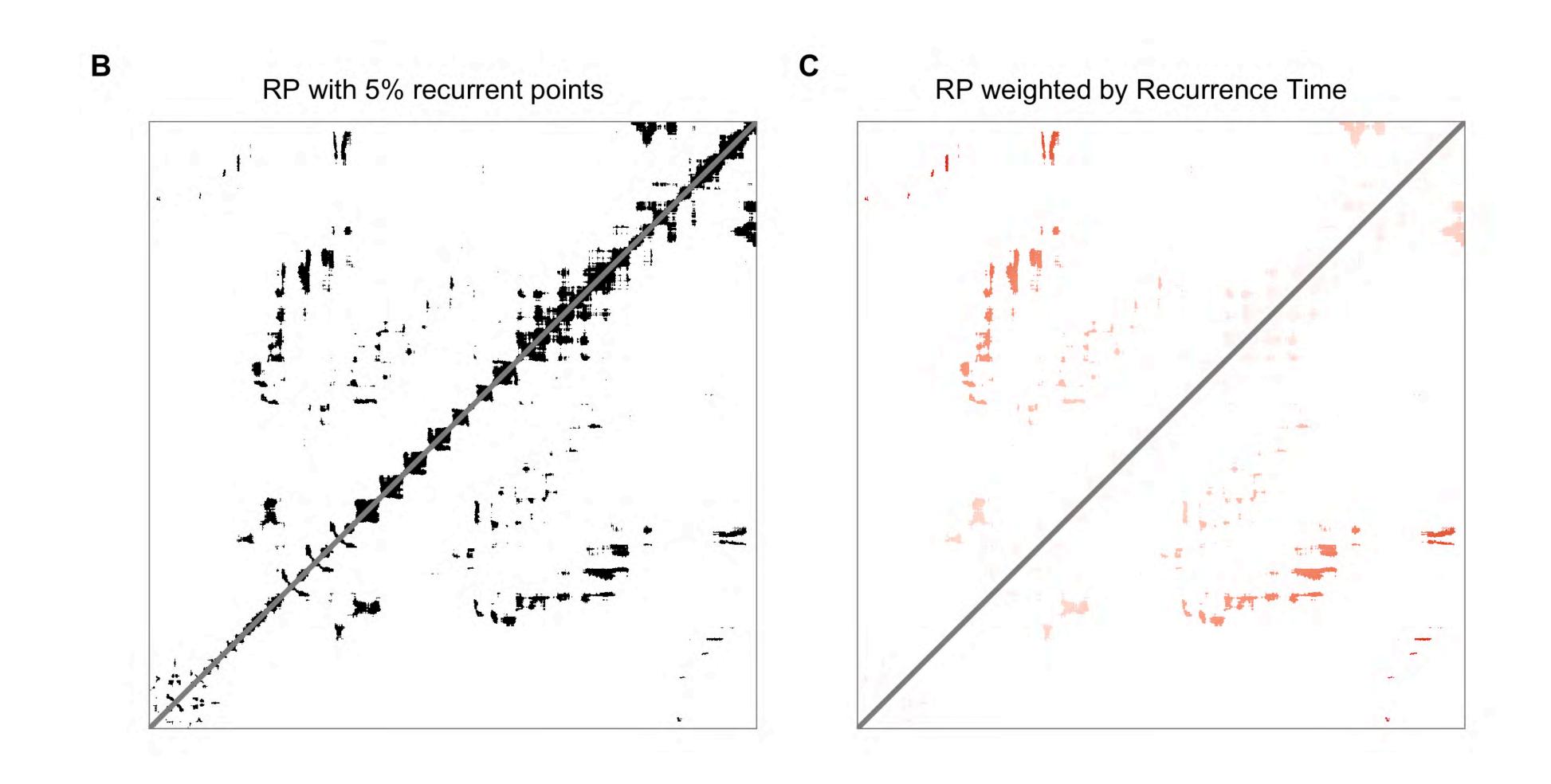


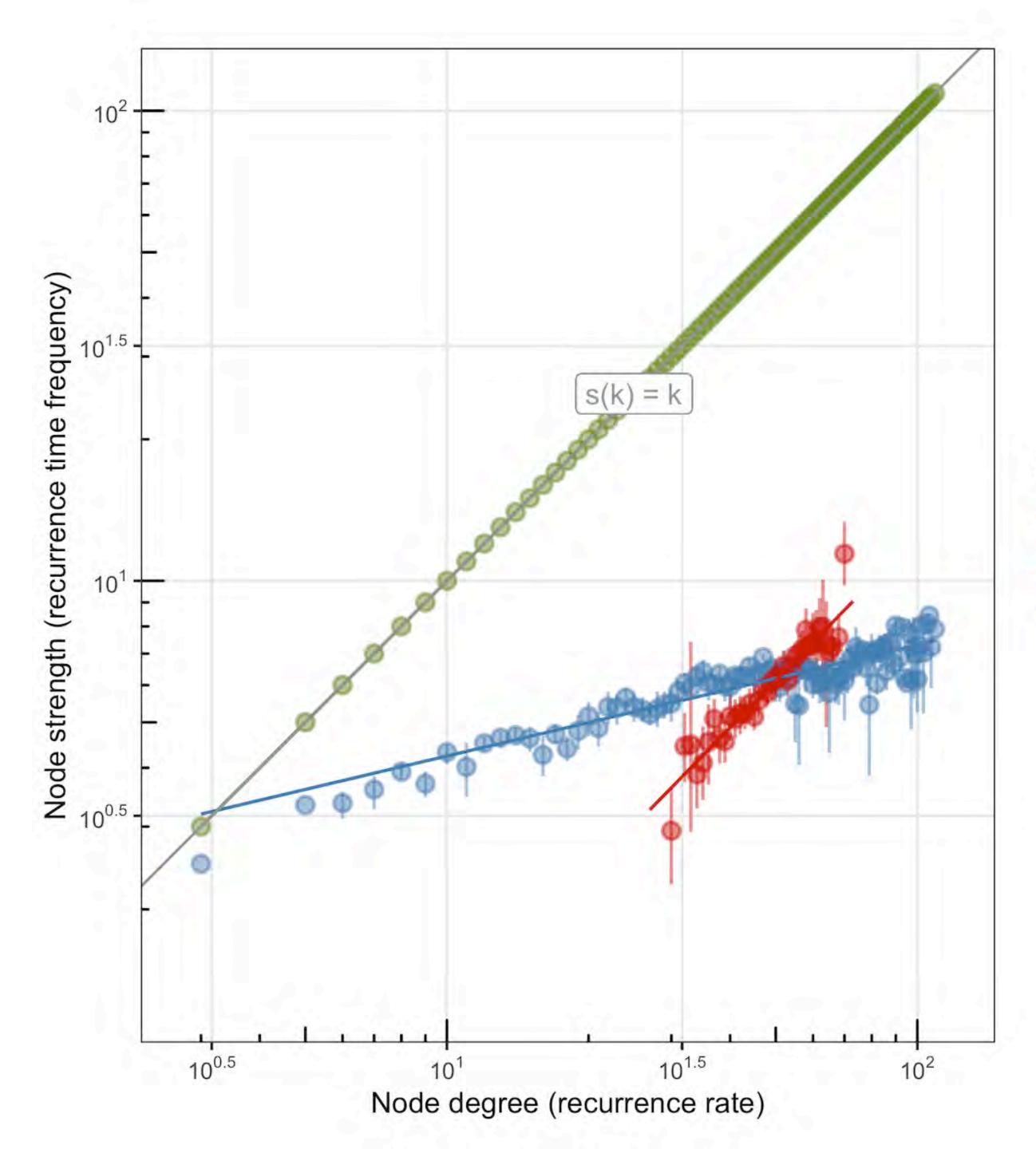


## Weighted Adjacency Matrix



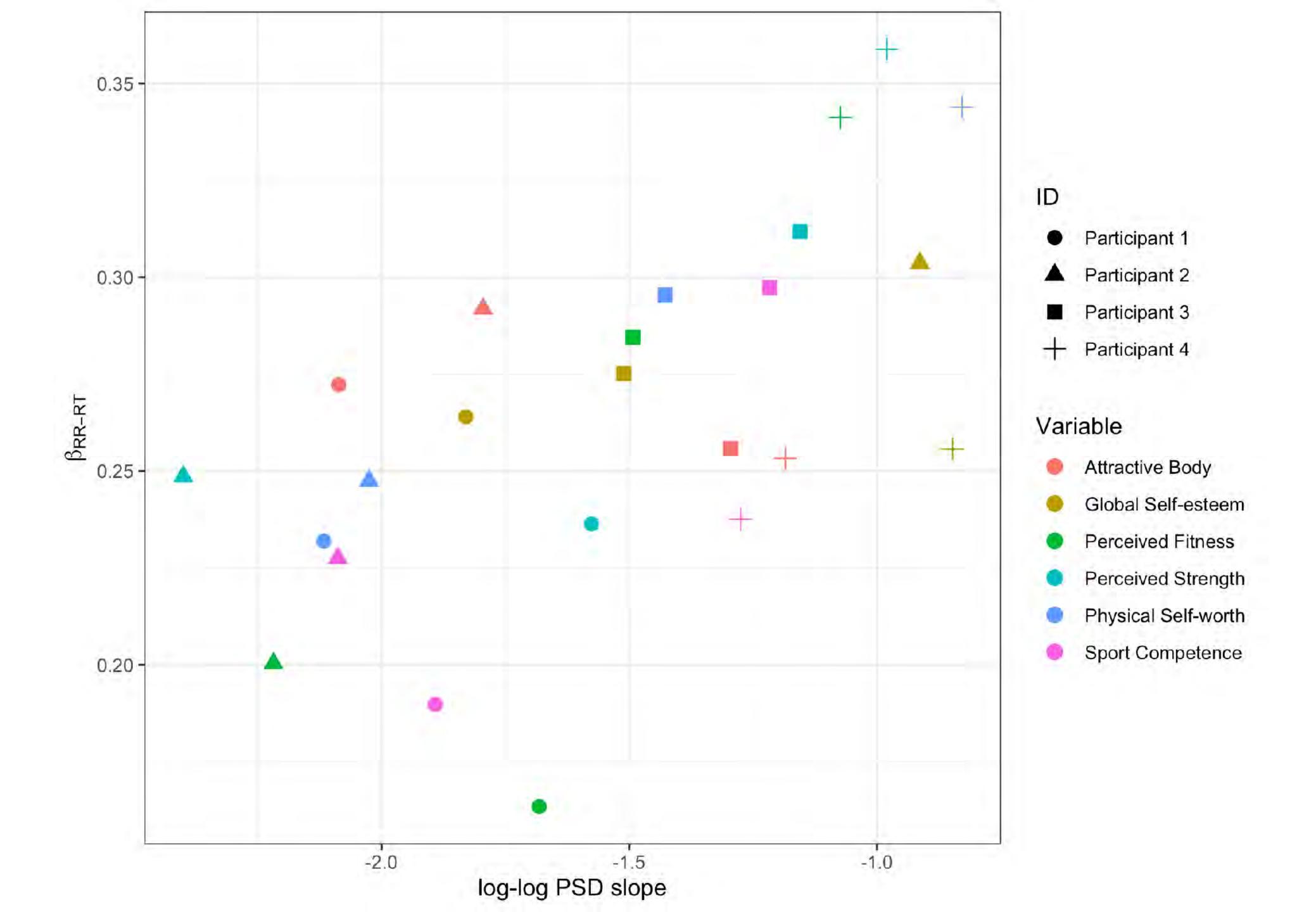
## Weighted Adjacency Matrix





#### Recurrence Network based on:

- Perceived Strength (participant 1)
- Random rewire (each edge)
  - Random rewire (keeping degree sequence)



## Multiplex Recurrence Networks

## MULTIPLEX RECURRENCE NETWORKS PHYSICAL REVIEW E 97, 012312 (2018) multiplex network multivariate time series weighted network of recurrence network recurrence networks time

FIG. 1. Illustration of the procedure for generating network structures from a multivariate time series: multivariate time series → recurrence networks → multiplex recurrence network → weighted network of recurrence networks. Dashed lines between multiplex networks' layers connect all layers to all.

#### **Interlayer Mutual Information**

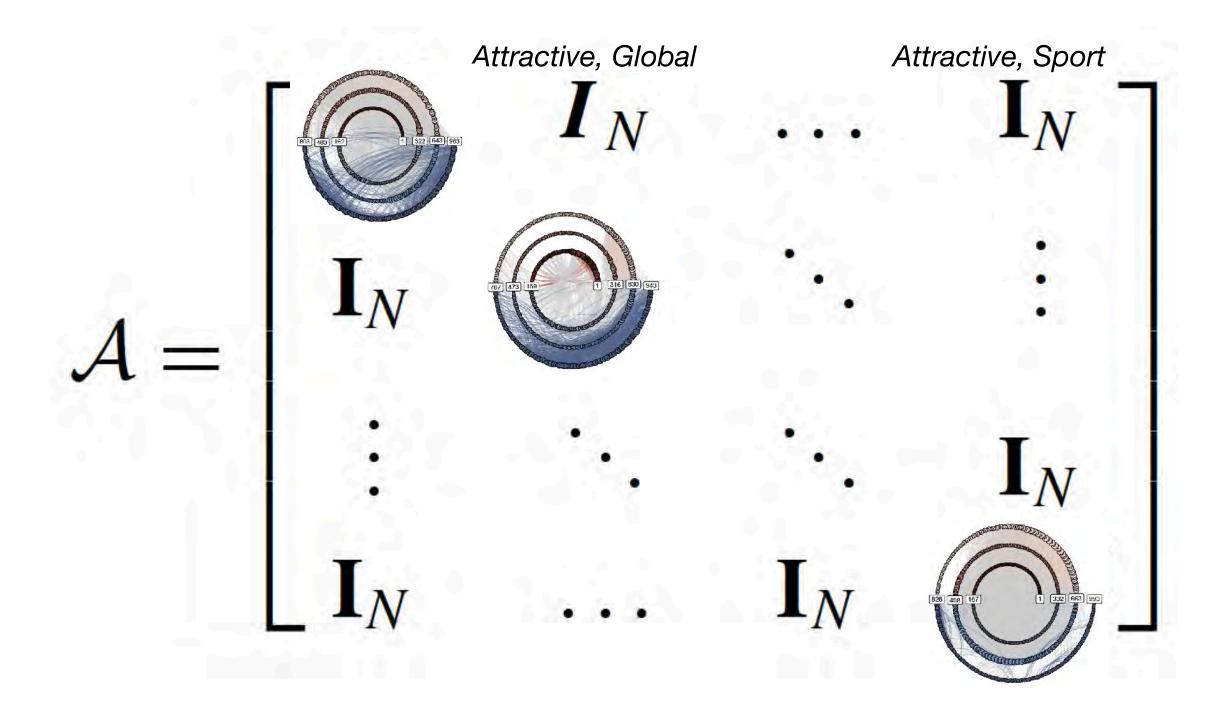
$$I_{\alpha,\beta} = \sum_{\kappa^{[\alpha]}} \sum_{\kappa^{[\beta]}} P\left(\kappa^{[\alpha]}, \kappa^{[\beta]}\right) \log \frac{P\left(\kappa^{[\alpha]}, \kappa^{[\beta]}\right)}{P\left(\kappa^{[\alpha]}\right), P\left(\kappa^{[\beta]}\right)}$$

Same number of nodes (time points)

Different degree, etc.

### **Interlayer Mutual Information**

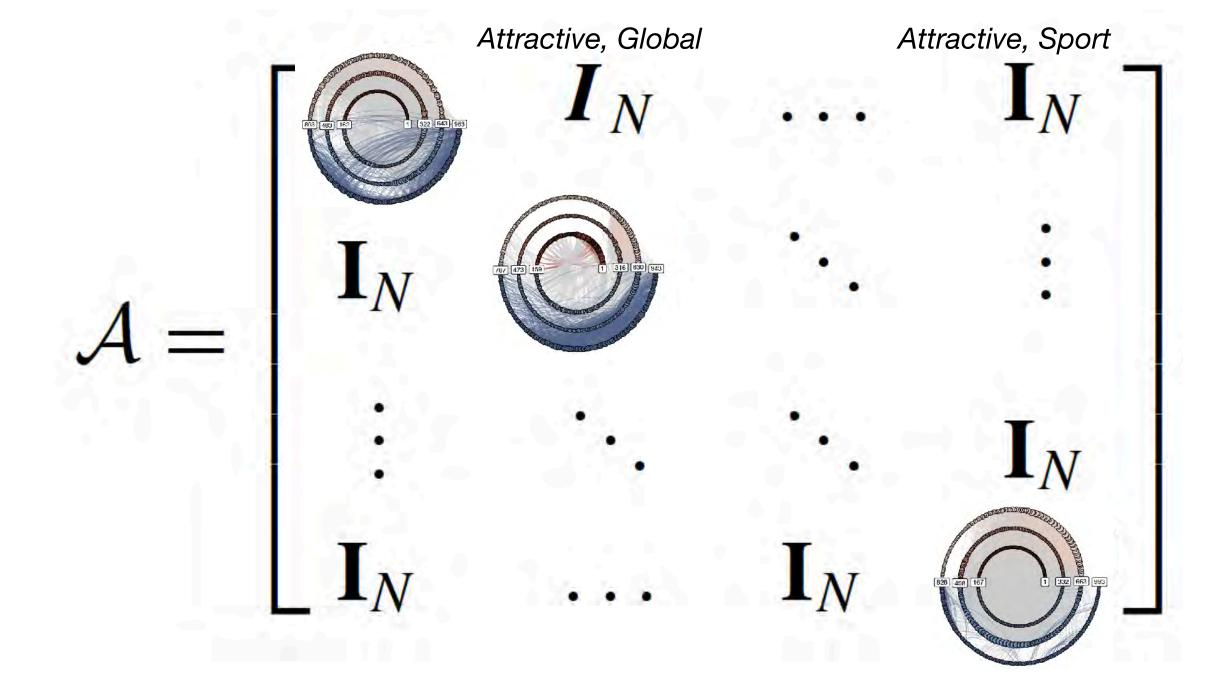
$$I_{\alpha,\beta} = \sum_{\kappa^{[\alpha]}} \sum_{\kappa^{[\beta]}} P\left(\kappa^{[\alpha]}, \kappa^{[\beta]}\right) \log \frac{P\left(\kappa^{[\alpha]}, \kappa^{[\beta]}\right)}{P\left(\kappa^{[\alpha]}\right), P\left(\kappa^{[\beta]}\right)}$$

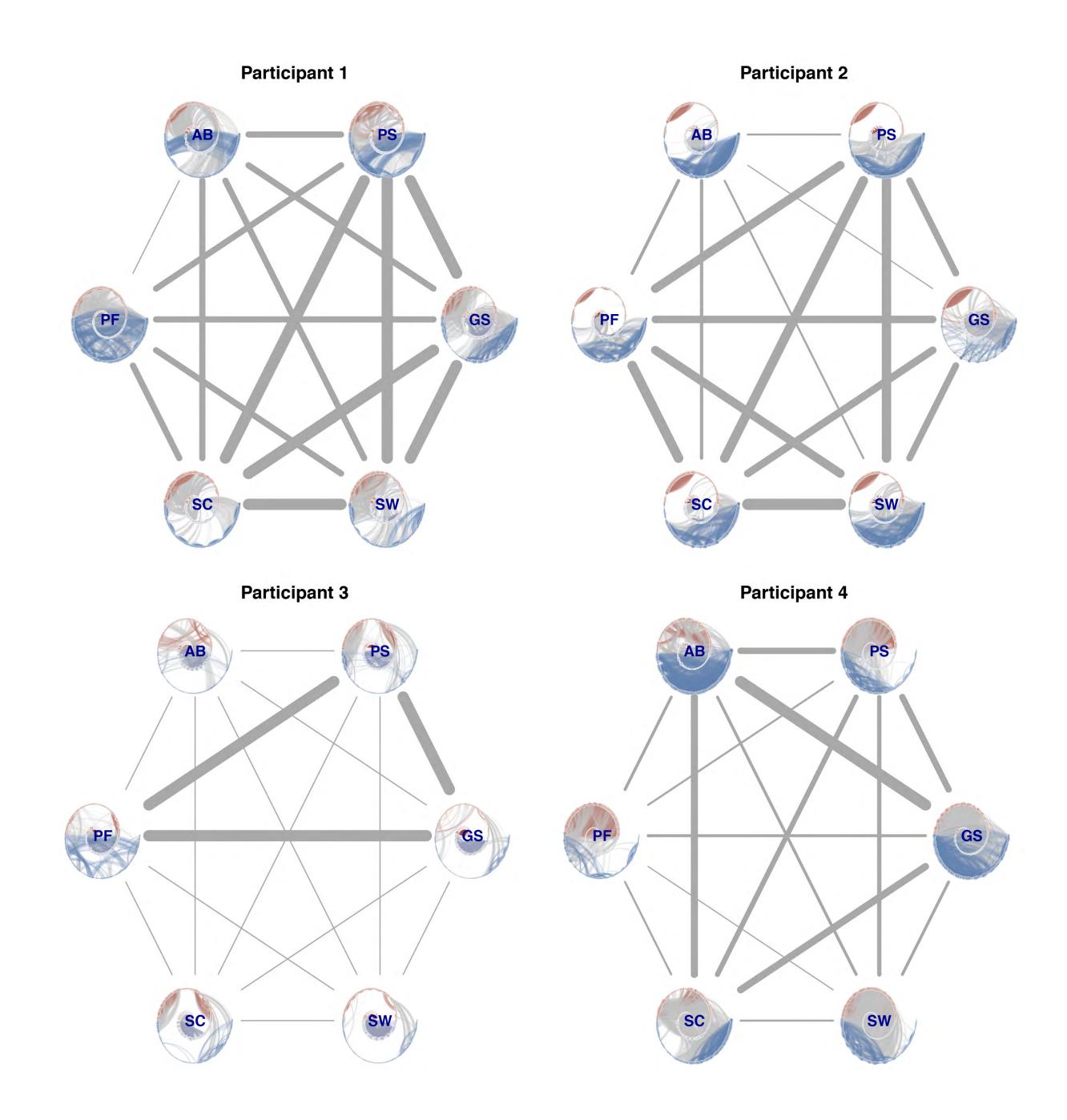


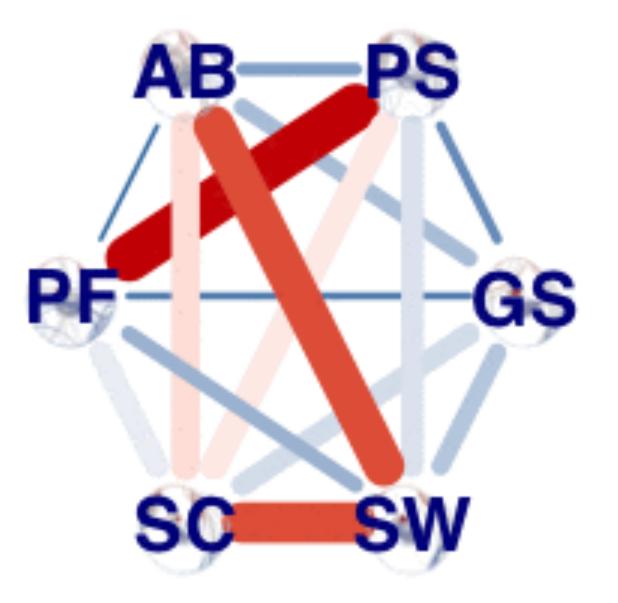
#### Interlayer Mutual Information based on Strength

$$I_{\alpha,\beta} = \sum_{\kappa^{[\alpha]}} \sum_{\kappa^{[\beta]}} P\left(\kappa^{[\alpha]}, \kappa^{[\beta]}\right) \log \frac{P\left(\kappa^{[\alpha]}, \kappa^{[\beta]}\right)}{P\left(\kappa^{[\alpha]}\right), P\left(\kappa^{[\beta]}\right)}$$

$$I_{\alpha,\beta} = \sum_{s(\kappa)^{[\alpha]}} \sum_{s(\kappa)^{[\beta]}} P(s(\kappa)^{[\alpha]}, s(\kappa)^{[\beta]}) \cdot log \frac{P(s(\kappa)^{[\alpha]}, s(\kappa)^{[\beta]})}{P(s(\kappa)^{[\alpha]}) P(s(\kappa)^{[\beta]})}$$

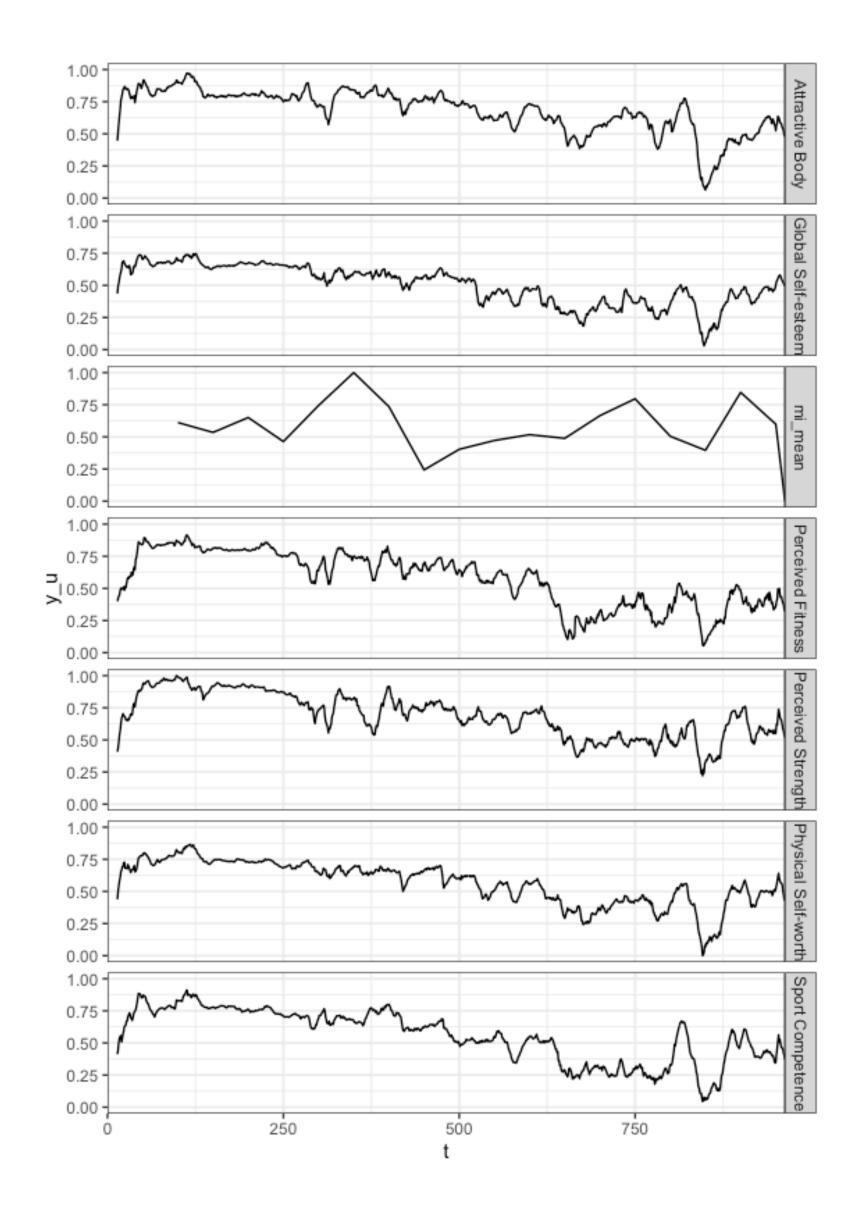




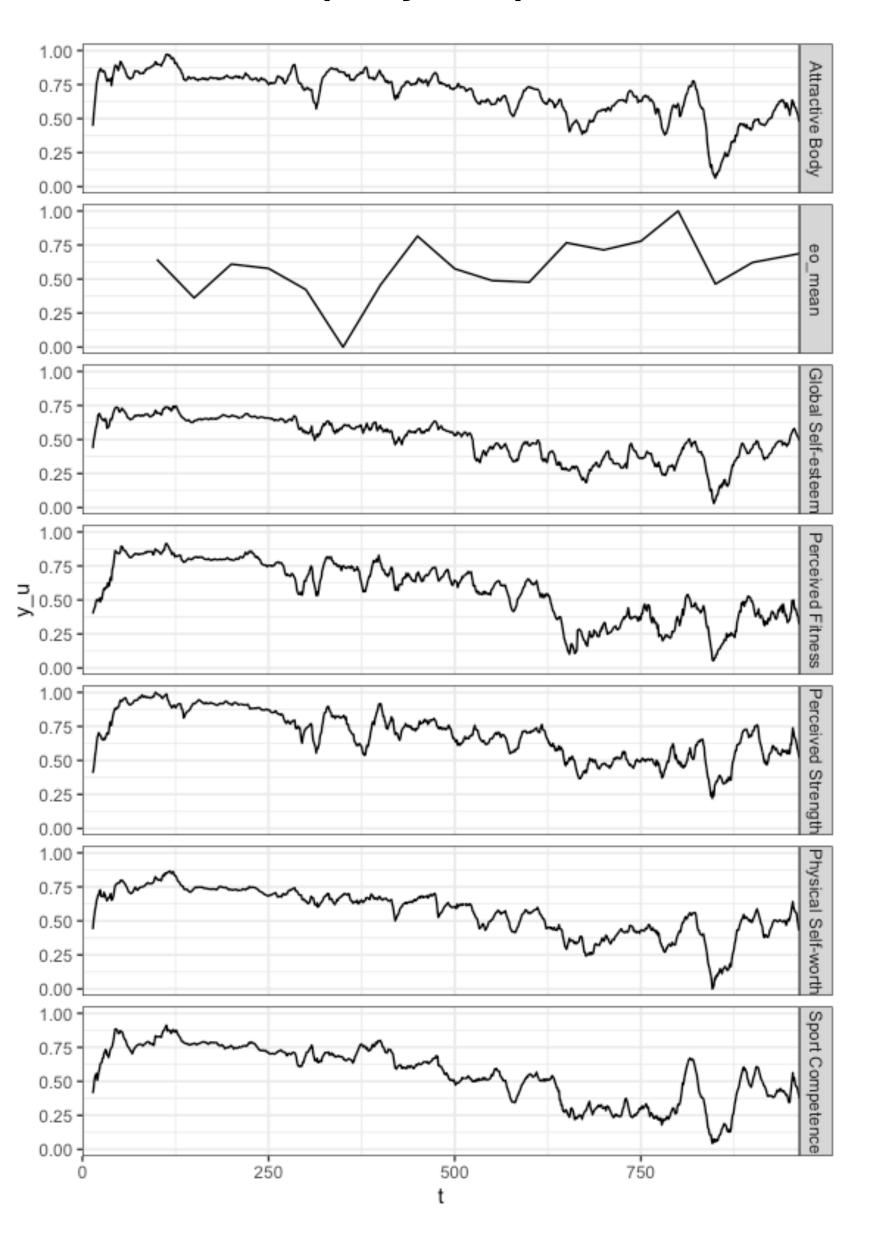


window: 01 | start: 1 | stop: 100

## Interlayer Mutual Information (subject 3)



## Edge Overlap (subject 2)



## Take Home Message

NO NEED TO REDUCE DIMENSION OF MULTIVARIATE
TIME SERIES DATA

USE MULTIPLEX RECURRENCE NETWORKS